

PLEASE PRINT and box final results. Show all work for full credit.

Work must be clear and unambiguous for credit.

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Verify that the eigenfunction ψ_{211} and the associated eigenvalue E_2 satisfy the time-independent Schrödinger equation for a one-electron atom with $Z = 1$.

$$\psi_{211} = \frac{1}{8\sqrt{\pi}} \left(\frac{Z}{a_o}\right)^{3/2} \frac{Zr}{a_o} e^{-Zr/2a_o} \sin\theta e^{i\phi}$$

$$E_n = - \left(\frac{kZe^2}{\hbar}\right)^2 \frac{\mu}{2n^2} \quad \text{and} \quad a_o = \frac{\hbar^2}{(ke^2\mu)}$$

$$\nabla^2 = \frac{1}{r^2} \frac{\partial}{\partial r} \left(r^2 \frac{\partial}{\partial r} \right) + \frac{1}{r^2 \sin\theta} \frac{\partial}{\partial \theta} \left(\sin\theta \frac{\partial}{\partial \theta} \right) + \frac{1}{r^2 \sin^2\theta} \frac{\partial^2}{\partial \phi^2}$$