

**Constants:**  $e = 1.6 \times 10^{-19} \text{ C}$     $m_p = 1.67 \times 10^{-27} \text{ kg}$     $m_e = 9.1 \times 10^{-31} \text{ kg}$     $c = 3 \times 10^8 \text{ m/s}$     $\text{micro} = 10^{-6}$   
 $\epsilon_o = 8.85 \times 10^{-12} \text{ C}^2/\text{N} \cdot \text{m}^2$     $k = 1/(4\pi\epsilon_o) = 9 \times 10^9 \text{ N} \cdot \text{m}^2/\text{C}^2$     $\mu_o = 4\pi \times 10^{-7} \text{ T} \cdot \text{m/A}$     $\text{nano} = 10^{-9}$

**Coulomb's Law:**  $|\vec{F}| = \frac{|q_1||q_2|}{4\pi\epsilon_o r^2}$  (point charge)

**Electric field:**  $\vec{E} = \frac{\vec{F}}{q}$     $\vec{E} = \frac{q}{4\pi\epsilon_o r^2} \hat{r}$  (point charge)    $\vec{E} = \int \frac{dq}{4\pi\epsilon_o r^2} \hat{r}$  (general)    $E = \frac{\sigma}{2\epsilon_o}$  (plane)

**Gauss' law:**  $\Phi = \hat{n} \cdot \vec{E} A = \oint \hat{n} \cdot \vec{E} dA = \frac{q_{enc}}{\epsilon_o}$

**Energy:**  $W = \int \vec{F} \cdot d\vec{s} = \frac{1}{2}mv_f^2 - \frac{1}{2}mv_i^2 = K_f - K_i$

For conservative forces  $U_f - U_i = - \int \vec{F} \cdot d\vec{s} \rightarrow K_i + U_i = K_f + U_f$

**Electric potential:**  $V = \frac{U}{q}$     $V = \frac{q}{4\pi\epsilon_o r}$  (point charge)    $V = \int \frac{dq}{4\pi\epsilon_o r}$  (general)

$V_b - V_a = - \int_a^b E_x dx = - \int_a^b \vec{E} \cdot d\vec{s}$     $E_x = -\frac{\partial V}{\partial x}$ ,    $E_y = -\frac{\partial V}{\partial y}$ ,    $E_z = -\frac{\partial V}{\partial z}$

**Capacitors:**  $q = CV$     $C = \frac{K\epsilon_o A}{d}$  (parallel-plate)    $C = C_1 + C_2$  (parallel)

$U = \frac{q^2}{2C}$     $u = \frac{1}{2}\epsilon_o E^2$     $\frac{1}{C} = \frac{1}{C_1} + \frac{1}{C_2}$  (series)

**Resistors:**  $i = \frac{dq}{dt} = jA$     $R = \frac{V}{i}$     $R = \frac{\rho L}{A}$  (wire)    $P = iV$     $R = R_1 + R_2$  (series)

$q = CV(1 - e^{-t/RC})$  (charging)    $q = q_o e^{-t/RC}$  (discharging)    $\frac{1}{R} = \frac{1}{R_1} + \frac{1}{R_2}$  (parallel)

**Magnetism:**  $\vec{F} = q\vec{v} \times \vec{B}$     $\vec{F} = i\vec{L} \times \vec{B}$     $\mu = NiA$     $\vec{\tau} = \vec{\mu} \times \vec{B}$     $U = -\vec{\mu} \cdot \vec{B}$     $\frac{F}{l} = \frac{\mu_o i_1 i_2}{2\pi r}$

$d\vec{B} = \frac{\mu_o i d\vec{s} \times \hat{r}}{4\pi r^2}$     $\oint \vec{B} \cdot d\vec{s} = \mu_o i_{enc}$     $B = \frac{\mu_o i}{2\pi R}$ , (wire)    $\frac{\mu_o i}{2R}$  (loop center),    $\frac{\mu_o iN}{L}$  (solenoid)

**Induction:**  $\Phi_B = \hat{n} \cdot \vec{B} A = \oint \hat{n} \cdot \vec{B} dA$     $\mathcal{E} = \oint \vec{E} \cdot d\vec{s} = -\frac{d\Phi_B}{dt}$

$L = N\Phi_B/i$  (definition)    $L = \mu_o n^2 Al$  (solenoid)    $\mathcal{E} = -L \frac{di}{dt}$     $\mathcal{E}_1 = -M \frac{di_2}{dt}$     $L = L_1 + L_2$  (series)

$U_B = \frac{1}{2}Li^2$     $u_B = \frac{B^2}{2\mu_o}$     $i = i_o e^{-t/\tau_L}$     $\tau_L = L/R$     $\frac{V_s}{V_p} = \frac{N_s}{N_p}$     $\frac{1}{L} = \frac{1}{L_1} + \frac{1}{L_2}$  (parallel)

**AC Circuits:**  $\omega = \frac{1}{\sqrt{LC}}$  (LC circuit)    $\mathcal{E} = \mathcal{E}_m \sin(\omega t)$     $i = I \sin(\omega t - \phi)$  (driven RLC)    $P_{avg} = \frac{1}{2}I\mathcal{E}_m \cos \phi$

$\tan \phi = \frac{X_L - X_C}{R}$     $I = \frac{\mathcal{E}_m}{Z}$     $Z = \sqrt{R^2 + (X_L - X_C)^2}$     $X_L = \omega L$ ,    $X_C = \frac{1}{\omega C}$ ,    $v_L = L \frac{di}{dt}$ ,    $v_C = \frac{q}{C}$

$q = Q_o e^{-Rt/(2L)} \cos(\omega't + \phi)$     $\omega' = (\omega^2 - (R/(2L))^2)^{1/2}$

**Last 2 Maxwell's Eqs.:**  $\oint \vec{B} \cdot \hat{n} dA = 0$     $\oint \vec{B} \cdot d\vec{s} = \mu_o \epsilon_o \frac{d\Phi_E}{dt} + \mu_o i_{enc}$     $i_d = \epsilon_o \frac{d\Phi_E}{dt}$

**EM Waves:**  $c = \frac{E}{B} = \frac{1}{\sqrt{\mu_0 \epsilon_0}}$      $\vec{S} = \frac{1}{\mu_0} \vec{E} \times \vec{B}$      $I = S_{avg} = \frac{1}{c\mu_0} E_{rms}^2$      $E_{rms} = \frac{E_m}{\sqrt{2}}$      $I = \frac{P_s}{4\pi r^2}$

$I = I_o \cos^2 \theta$      $n_1 \sin \theta_1 = n_2 \sin \theta_2$      $\theta_c = \sin^{-1} \frac{n_2}{n_1}$      $\theta_B = \tan^{-1} \frac{n_2}{n_1}$      $p_r = \frac{I}{c}$  (absorp.),  $\frac{2I}{c}$  (refl.)

$\vec{E} = \vec{E}_m \sin(\vec{k} \cdot \vec{r} - \omega t)$      $\vec{B} = \vec{B}_m \sin(\vec{k} \cdot \vec{r} - \omega t)$      $\vec{E}_m \perp \vec{B}_m \perp \vec{k}$      $c = \omega/k = f\lambda$

**Images:**  $\frac{1}{p} + \frac{1}{i} = \frac{1}{f} = \frac{2}{r}$      $\frac{n_1}{p} + \frac{n_2}{i} = \frac{n_2 - n_1}{r}$      $\frac{1}{p} + \frac{1}{i} = \frac{1}{f} = (n-1)\left(\frac{1}{r_1} - \frac{1}{r_2}\right)$      $m = -\frac{i}{p}$

**Interference:**  $\Delta L = m\lambda_n$  (constructive)     $\Delta L = (m + \frac{1}{2})\lambda_n$  (destructive)     $\lambda_n = \lambda/n$      $n = 1$  in air

$\Delta L = d \sin(\theta)$  (2-slit),  $2L_1 - 2L_2$  (interferometer),  $2t$  (thin film) with extra  $\lambda/2$  when reflecting off higher index

**Diffraction:**  $d \sin(\theta) = m\lambda$  (grating)     $2d \sin(\theta) = m\lambda$  (X-ray)     $\sin \theta = 1.22\lambda/d$  (aperture)