

## Dimensional Analysis

**ALL** units are expressed in terms of three basic quantities, mass **M**, length **L**, and time **T**, expressed in Kilogram, Meter, and Second, respectively.

**Dimensional Analysis:** good physics equations (**and** good students) balance their MLT's.

- Velocity ( $v$ ):  $\mathbf{LT}^{-1}$  (meters per second)
- Acceleration ( $a$ ):  $\mathbf{LT}^{-2}$  (meters per second squared)
- Frequency ( $f$ ):  $\mathbf{T}^{-1}$  – **HERZ** (per second)
- Momentum ( $mv$ ):  $\mathbf{MLT}^{-1}$  (Kg-meters per second)
- Force ( $\mathcal{F}$ ):  $\mathbf{MLT}^{-2}$ – **NEWTON** (Kg-meter per second squared; remember “ $f = ma$ ”)
- Energy ( $\mathcal{E}$ ):  $\mathbf{ML}^2\mathbf{T}^{-2}$ – **JOULE** (Kg-meter squared per second squared; remember “ $\mathcal{E} = mc^2$ ”)
- Power ( $\mathcal{P}$ ):  $\mathbf{ML}^2\mathbf{T}^{-3}$ – **WATT** (Kg-meter squared per second cubed; energy per unit time)
- Electric Charge ( $\mathcal{Q}$ ):  $\mathbf{M}^{\frac{1}{2}}\mathbf{L}^{\frac{3}{2}}\mathbf{T}^{-1}$ – **COULOMB** (derived by balancing Coulomb's law)
- Electric Field ( $\mathcal{E}$ ):  $\mathbf{M}^{\frac{1}{2}}\mathbf{L}^{-\frac{1}{2}}\mathbf{T}^{-1}$  (force per unit charge)
- Magnetic Field ( $\mathcal{B}$ ):  $\mathbf{M}^{\frac{1}{2}}\mathbf{L}^{-\frac{3}{2}}\mathbf{T}^{-1}$  – **TESLA** (“force=charge times velocity times  $\mathcal{B}$ ”)
- Voltage ( $\mathcal{V}$ ):  $\mathbf{M}^{\frac{1}{2}}\mathbf{L}^{\frac{1}{2}}\mathbf{T}^{-1}$ – **VOLT** (Coulomb per meter)
- Current ( $\mathcal{I}$ ):  $\mathbf{M}^{\frac{1}{2}}\mathbf{L}^{\frac{3}{2}}\mathbf{T}^{-2}$  – **AMPERE** (Coulomb per second)
- Resistance ( $\mathcal{R}$ ):  $\mathbf{L}^{-1}\mathbf{T}$  – **OHM** (seconds per meter; remember “ $V = \text{current times resistance}$ ”)
- Capacitance ( $\mathcal{C}$ ):  $\mathbf{L}$  – **FARAD** (inverse meter; remember the shopping network: “charge = voltage times capacitance”)  $\mathcal{RC}$  has units of time
- Inductance ( $\mathcal{L}$ ):  $\mathbf{L}^{-1}\mathbf{T}^2$ – **HENRY** ( $\mathcal{LC}$  has units of  $\mathbf{T}^2$ )