



if $\rho_{\text{object}} \neq \rho_{\text{fluid}}$ then

$$P_2 A - P_1 A - mg \neq 0$$

$$P_2 A - P_1 A = B \quad (\text{Buoyant force})$$

(points up)

From lecture 25

$$P_2 A - P_1 A = \text{weight of fluid}$$

$$= \rho_{\text{fluid}} V_{\text{fluid}} g$$

where V_{fluid} is the volume of fluid displaced by the object.

$$\Rightarrow \boxed{B = \rho_{\text{fluid}} V_{\text{fluid}} g}$$

Always true for buoyant force.

for completely submerged object:

$$V_{\text{fluid}} = V_{\text{object}}$$

for floating object:

$$V_{\text{fluid}} \neq V_{\text{object}}$$

But since it's floating, it is in equilibrium.

$$\Rightarrow B - mg = 0 \Rightarrow B = mg$$

$$\Rightarrow \rho_{\text{fluid}} V_{\text{fluid}} g = \rho_{\text{object}} V_{\text{object}} g$$

$$\Rightarrow \frac{\rho_{\text{object}}}{\rho_{\text{fluid}}} = \frac{V_{\text{fluid}}}{V_{\text{object}}}$$