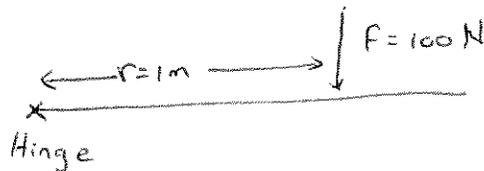


## PHY2053 Health, Summer C 2016

## Quiz 4

Date: Wednesday, June 30, 2016

**Problem 1:** A person opens a door by applying a constant force of 100 N perpendicular to it, at a distance of 1 m from the hinge. After rotating by  $60^\circ$ , the door has an angular velocity of 0.8 rad/s. Find the moment of inertia of the door.



$$\Delta\theta = 60^\circ = \frac{60}{360} \times 2\pi \text{ rad} = \frac{\pi}{3} \text{ rad}$$

$$\text{Work done} = \tau \Delta\theta$$

$$\text{Also Work done} = \frac{1}{2} I (\omega_f^2 - \omega_i^2) \quad [KE_f - KE_i]$$

$$\text{So, } \tau \Delta\theta = \frac{1}{2} I \omega_f^2$$

$$\tau = 100 \text{ N} \times 1 \text{ m} = 100 \text{ Nm}$$

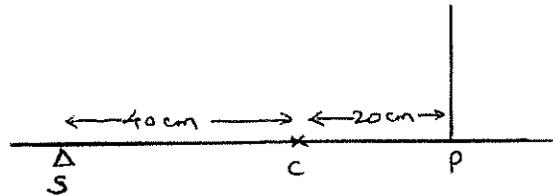
Plugging in all the values, we get

$$I = \frac{2 \tau \Delta\theta}{\omega_f^2} = 327.2 \text{ kg m}^2$$

$$\boxed{I = 327.2 \text{ kg m}^2}$$

**Problem 2:** A stick of mass 3 kg is suspending by a rope as shown. To prevent the toppling of the stick, a support is placed under the stick to the left of the point of suspension. Calculate the force of tension exerted on the stick by the rope.

On the diagram: P = point of suspension, S = support, C = center of mass of the stick.



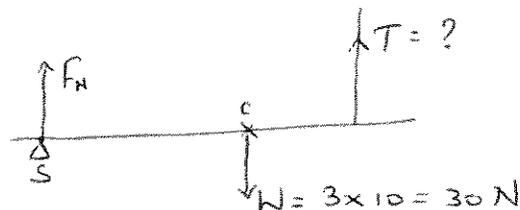
The weight of the stick effectively acts through C.

The two other forces are tension at P and normal force at S. We can find both these forces using the equations

for equilibrium  $\Sigma F = 0$ ;  $\Sigma \tau = 0$ .

If we only need the tension, by picking S to be the pivot, we can ~~find~~ avoid having to use  $\Sigma F = 0$ .

Pivot at S:



$$\tau_W = -(30 \text{ N} \times 0.4 \text{ m}) = -12 \text{ N}\cdot\text{m}$$

$$\tau_T = +[T \times (0.4 + 0.2) \text{ m}] = T \cdot 0.6 \text{ m}$$

$$\tau_{F_N} = 0$$

$$\Sigma \tau = 0 \quad \text{gives} \quad -12 \text{ N}\cdot\text{m} + T \cdot 0.6 \text{ m} = 0$$

$$\text{or} \quad T = \frac{12 \text{ N}}{0.6} = 20 \text{ N}$$

Using  $\Sigma F = 0$ , we can also find that  $F_N = 10 \text{ N}$