

PHY2053 Health, Summer C 2016

Quiz 7

Date: Thursday, July 28, 2016

Problem 1: An organ pipe is closed at one end. When a particular key on the organ is pressed, the pipe resonates with a frequency of 870 Hz. If you are told that this frequency is the *second* overtone of the pipe, what is the pipe's length? Assume that the temperature in the organ room is 10° Celsius.

Second overtone is the 3rd harmonic

For pipe open at one end and closed at the other,
this corresponds to $n = 5$

$$\lambda_5 = \frac{4L}{5}$$

$$f_5 = \frac{v}{\lambda_5} = \frac{5v}{4L}$$

$$f_5 = 870 \text{ Hz}$$

$$v = (331 + 0.606 \times 10) \text{ m/s}$$
$$= 337 \text{ m/s}$$

Find L

$$L = \frac{5v}{4f_5} = \frac{5 \times 337}{4 \times 870} \text{ m} = 0.48 \text{ m}$$

$$\boxed{L = 48 \text{ cm}}$$

Problem 2: You stand in a room full of clocks. Whenever a new hour begins, all of the clocks start to chime, with each clock producing sound with the same intensity $I = 4.0 \times 10^{-4} \text{ W/m}^2$. Assume the threshold of human hearing is $I_0 = 10^{-12} \text{ W/m}^2$.

- (a) What is the intensity level of the sound produced by one chiming clock?
- (b) How many clocks would need to chime to produce an intensity level of 130 dB (the intensity level you would experience standing 30 m away from a jet engine). Round your answer up to the nearest integer. [Hint: it's a lot of clocks!]

$$\begin{aligned} \text{a)} \quad \beta &= 10 \text{ dB} \log_{10} \left(\frac{I}{I_0} \right) \\ &= 10 \text{ dB} \log_{10} \left(\frac{4 \times 10^{-4}}{10^{-12}} \right) \\ &= 10 \text{ dB} \times 8.60 = 86.0 \text{ dB} \end{aligned}$$

b) $I_{\text{tot}} = n \times I$ (since the waves are incoherent, intensities add up).
where n is the number of clocks

$$\beta_{\text{tot}} = 130 \text{ dB} = 10 \text{ dB} \log_{10} \left(\frac{I_{\text{tot}}}{I_0} \right)$$

$$\text{So, } \log_{10} \left(\frac{I_{\text{tot}}}{I_0} \right) = 13$$

$$\begin{aligned} \text{(or)} \quad I_{\text{tot}} &= I_0 \times 10^{13} = 10^{-12} \text{ W/m}^2 \times 10^{13} \\ &= 10 \text{ W/m}^2. \end{aligned}$$

25000 clocks
86 dB each
only produce
130 dB.
That's how loud
130 dB is

$$I = 4 \times 10^{-4} \text{ W/m}^2.$$

$$\Rightarrow n = \frac{I_{\text{tot}}}{I} = \frac{10}{4 \times 10^{-4}} = 25,000$$

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25,000 clocks will be needed to produce a 130 dB noise. Sound intensity level doesn't add up!