PHY2054 Formulas: Sheet 1

Chapter 15 (Electric forces and fields, Gauss' law)

Coulomb's Law
$$\mathbf{F} = \frac{kQq}{r^2} \hat{\mathbf{r}} = \frac{Qq}{4\pi\varepsilon_0 r^2} \hat{\mathbf{r}}$$
 (point charge) $\hat{\mathbf{r}}$ = unit vector from Q to q .

Electric field
$$\mathbf{F} = q\mathbf{E}$$
 (general) $\mathbf{E} = \frac{kQ}{r^2}\hat{\mathbf{r}} = \frac{Q}{4\pi\varepsilon_0 r^2}\hat{\mathbf{r}}$ (single point charge Q)

$$\mathbf{E} = \sum_{i} \frac{kq_i}{r_i^2} \hat{\mathbf{r}}_i \text{ (sum over point charges)}$$

Gauss' law
$$\Phi_E = \sum_i \mathbf{E}_i \cdot \mathbf{A}_i = \frac{Q_{\text{encl}}}{\varepsilon_0} \quad \Phi_E = \text{"electric flux"}$$

Chapter 16 (Electric potential, capacitors)

Work
$$W = \mathbf{F} \cdot (\mathbf{x}_f - \mathbf{x}_i) = K_f - K_i = \frac{1}{2} m v_f^2 - \frac{1}{2} m v_i^2$$

Conservative force
$$U_f - U_i = -\mathbf{F} \cdot (\mathbf{x}_f - \mathbf{x}_i) = -(K_f - K_i) \rightarrow U_i + K_i = U_f + K_f$$
 (energy conservation)

Electric potential
$$V = \frac{U}{q}$$
 (general) $V = \frac{kQ}{r} \equiv \frac{Q}{4\pi\varepsilon_0 r}$ (point charge Q)

Potential difference
$$\Delta V \equiv V_f - V_i = -\mathbf{E} \cdot (\mathbf{x}_f - \mathbf{x}_i)$$

Capacitors
$$C = \frac{\varepsilon_0 A}{d}$$
 $q = CV$ $U_E = \frac{1}{2}CV^2 = \frac{q^2}{2C}$ (energy) $u_E = \frac{1}{2}\varepsilon_0 E^2$ (energy density)

Capacitors (cont)
$$E \rightarrow \frac{E}{\kappa} \quad V \rightarrow \frac{V}{\kappa} \quad C \rightarrow \kappa C \quad C_{eq} = C_1 + C_2 \text{ (parallel)} \quad \frac{1}{C_{eq}} = \frac{1}{C_1} + \frac{1}{C_2} \text{ (series)}$$

Chapter 17 – 18 (Electric current, circuits)

Current
$$i = \frac{\Delta q}{\Delta t}$$
 (basic def) $i = Aen_e v_d$ (drift velocity)

Resistance
$$V = iR$$
 $R = \frac{\rho L}{A}$ $R_{\text{eq}} = R_1 + R_2$ (series) $\frac{1}{R_{\text{eq}}} = \frac{1}{R_1} + \frac{1}{R_2}$ (parallel)

Temp dependence
$$\rho - \rho_0 = \rho_0 \alpha (T - T_0)$$

RC circuits
$$au_{RC} = RC \quad q = q_{\max} \left(1 - e^{-t/\tau_{RC}} \right) \text{ (charging)} \quad q = q_{\max} e^{-t/\tau_{RC}} \quad \text{(discharging)}$$

Circuits (1) Current entering junction = current leaving junction (2)
$$\sum_{i} V_{i} = 0$$
 (over loop)

Power in circuit
$$P = iV$$
 (general power eqn) $P = i^2R$ (power lost in resistor)