

HOMEWORK 6, Due date 3/27 (you can always hand it in early!)

1. A galaxy has cylindrical symmetry and looks like a pancake of fixed thickness  $t$ . Its density, however, is a function of  $r$ , such that  $\rho = Ar(R-r)$ , where  $R$  is the radius of the galaxy and  $A$  is a constant. Calculate its rotational inertia (around its axis of symmetry) as a function of its mass.
2. Sketch the Lissajous patterns that will be obtained using  $x(t)$  and  $y(t)$  with the same amplitude, and  $\omega_y = 0.4 \omega_x$  and phase difference between  $x$  and  $y$  of 0, 45 and 90 degrees. Feel free to use an applet such as:

<http://www.surendranath.org/Applets/Oscillations/Lissajous/LissajousApplet.html>

or <http://www.angelfire.com/falcon/geodoubek/>

3. The amplitude of a particular damped oscillator decreases to  $1/e$  of its initial value after 10 periods. Find the frequency (using appropriate approximations) of the oscillator. Give answer in terms of the frequency of the corresponding undamped oscillator.