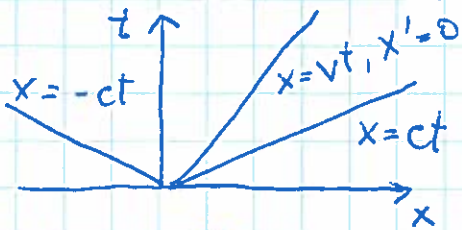


Postulates of SR

- inertial frame is any reference frame $(x, y, z, t) = S$ where all the laws of physics hold in their usual form.
 - Any rel. frame (x', y', z', t') that moves with constant velocity relative to S , is also inertial frame.
 - Light in vacuum has the same speed c in every direction. in all inertial frames
- Michelson - Morley experiment.

Problem with Galilean relativity.



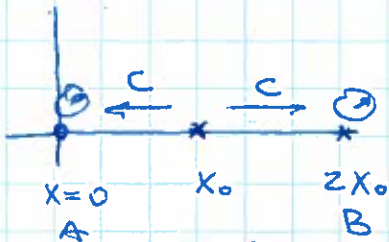
$$x' = x - vt \quad t' = t$$

for light ray $x = ct$

$$x' = (c - v)t' \quad \text{but } c \pm v \neq c$$

for light moving $-c \quad x' = -(c + v)t'$

- simultaneous event in a single frame.



light from event.
light between obs A & B
will reach them at the same time.

Chief observer can send a light signal to other observers so they can sync their clocks knowing their distance x from origin.



time dilation.

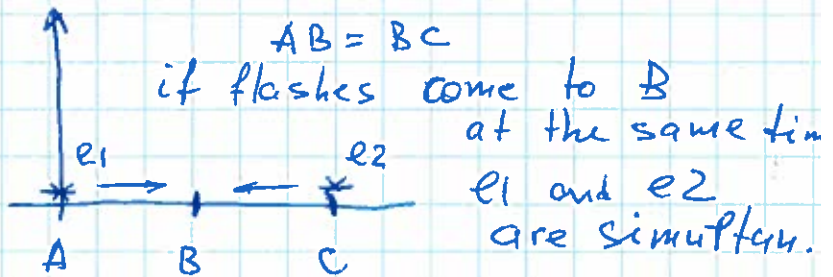
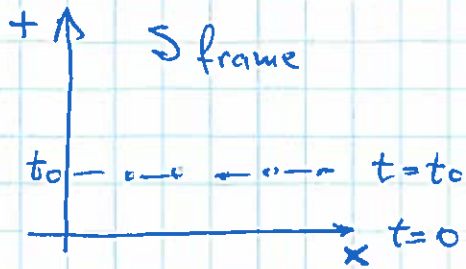
in S' $\Delta t' = \frac{2h}{c}$

in S $(c \Delta t / 2)^2 = h^2 + (v \Delta t / 2)^2 \quad \Delta t = \frac{2h}{c} \frac{1}{\sqrt{1 - v^2/c^2}}$

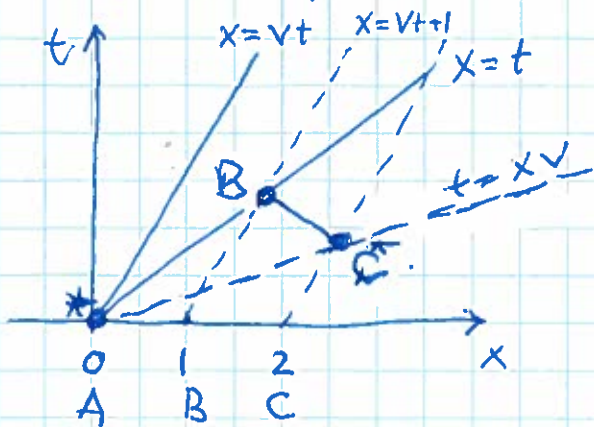
$$\Delta t = \Delta t' \cdot \frac{1}{\sqrt{1 - v^2/c^2}}$$

L27

Simultaneous events in a moving frame.



moving frame S'



use $c=1$
lets find the line of simultaneous events for observers in S'

events in A & C are simultaneous when observer B gets flashes at the same time.

flash from observer A: $\left. \begin{matrix} x = t \\ x = vt + 1 \end{matrix} \right\} \begin{matrix} t = \frac{1}{1-v} \\ x = \frac{1}{1-v} \end{matrix}$

flash from observer B:

$$\left. \begin{matrix} x_B + t_B = \frac{2}{1-v} \\ x_B = vt_B + 2 \end{matrix} \right\} \begin{matrix} t_B = \frac{2v}{1-v^2} \\ x_B = \frac{2}{1-v^2} \end{matrix} \quad t_B = vx_B$$

$t = vx \rightarrow$ line of simultaneous events.

So $\begin{matrix} x' = (x - vt) f(v) \\ t' = (t - xv) g(v) \end{matrix}$

using $x = t$ & $x' = t'$ for light ray obtain $f(v) = g(v)$
 $x' = x(1-v)f$
 $t' = t(1-v)g$ $f \neq g$

but $\begin{matrix} x = (x' + vt') f(v) \\ t = (t' + vx') f(v) \end{matrix}$

or $(x - vt)f^2 + v(t - xv)f^2 = x \Rightarrow f = \frac{1}{\sqrt{1-v^2}}$

$x' = \frac{(x - vt)}{\sqrt{1-v^2}} \quad t' = \frac{(t - xv)}{\sqrt{1-v^2}}$ Lorents transformation