# Detecting Additional Polarization Modes with eLISA



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Within the frame of Einstein's General Relativity, gravitational waves are expected to possess two tensorial polarizations, namely the well-known  $h_+$  and  $h_{\times}$  modes. Other metric theories of gravity however allow the existence of additional modes (two vector and/or two scalar modes), and the (non-)observation of those additional polarizations could put constraints on the validity of all existing theories, which would consequently provide a further test for General Relativity.

In its 2-arm-planned-configuration, eLISA only consists of one detector orbiting around the Sun, and we therefore investigate if there is a possibility to still detect and separate additional modes of a given gravitational wave signal.

#### Polarization modes

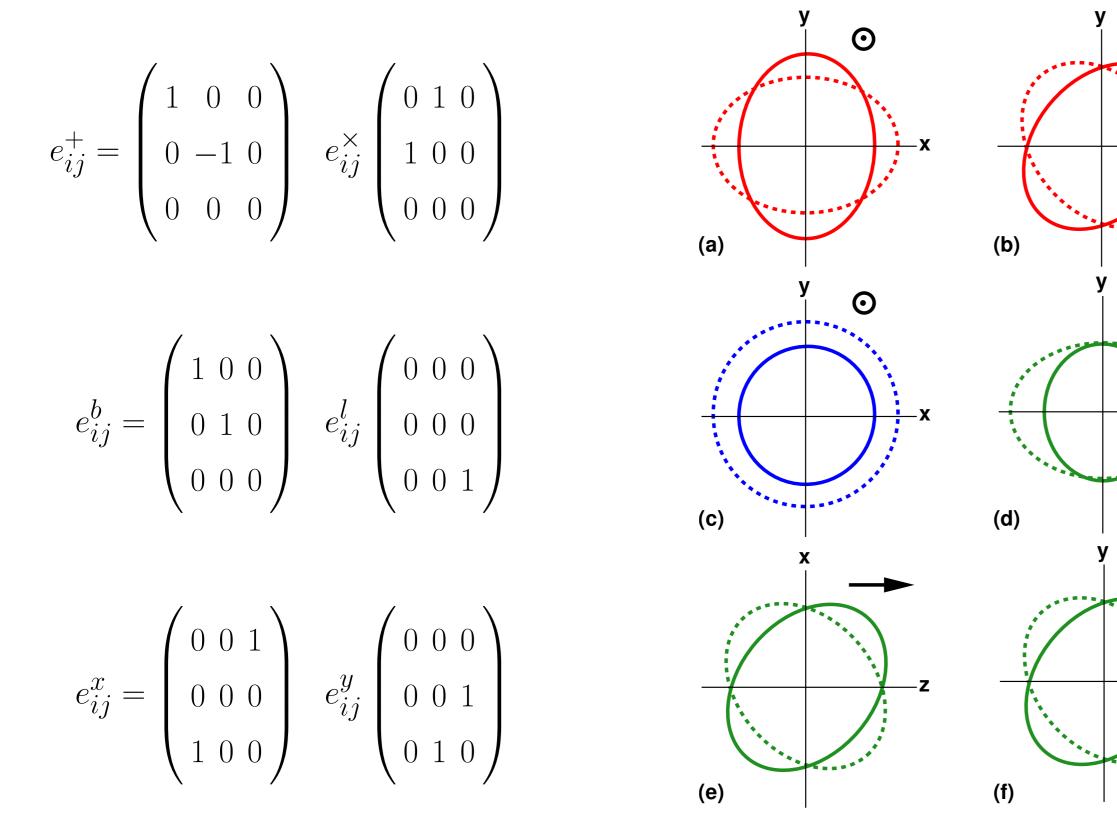
Perturbed metric corresponding to a propagating gravitational wave:

#### Sensitivity to additional modes

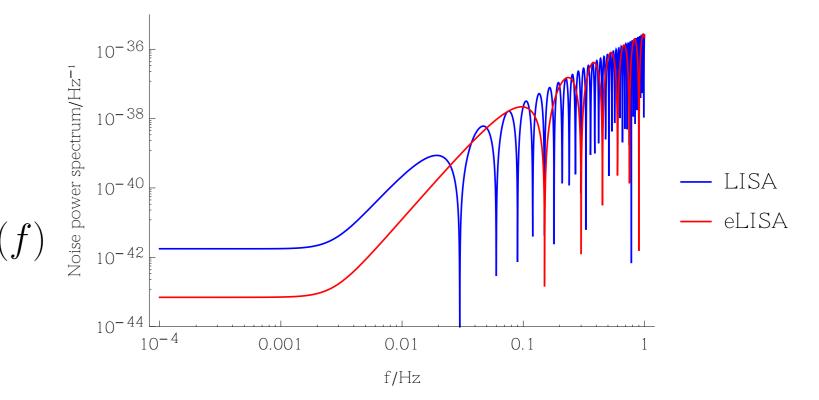
• Time-delay interferometric combinations,

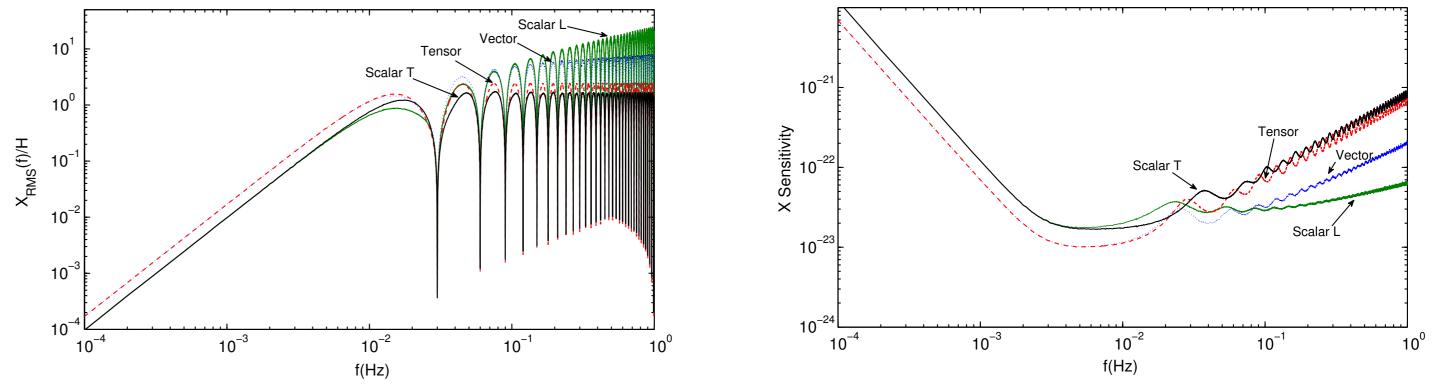
$$h_{ij}(\omega t - \mathbf{k} \cdot \mathbf{x}) = \sum_{A} h_A(\omega t - \mathbf{k} \cdot \mathbf{x}) e_{ij}^A$$

with  $A = \times, +, b, l, x, y$  the six possible polarization modes and the following tensors (tensor, scalar and vector modes)



• Thic-delay interferometric combinations, 2-arm configuration (4 beams) • Noise power spectrum :  $S_X(f)$ • Root-mean squared GW response :  $X_{\text{RMS}}(f)$ • Sensitivity :  $\text{SNR} \cdot \sqrt{S_X(f)B}/X_{\text{RMS}}(f)$ B : 1 cycle/year, SNR=5





- Similar behaviour between LISA and eLISA in the high-frequency regime (where they are more sensitive to (longitudinal) scalar modes)
- $X_{\text{RMS}}(f)$  and the sensitivity are given for LISA (similar results expected with shorter arms; to be confirmed)
- Stochastic GW background : network of detectors [1]

• GW stochastic background in the low frequency limit

$$h(t, \mathbf{x}) = \sum_{A} \int_{S^2} \mathrm{d}\hat{\boldsymbol{\Omega}} \int_{-\infty}^{\infty} \mathrm{d}f \ \tilde{h}_A(f, \hat{\boldsymbol{\Omega}}) e^{2\pi i f(t - \hat{\boldsymbol{\Omega}} \mathbf{x}/c)} F_A(\hat{\boldsymbol{\Omega}})$$

with  $A = +, \times, x, y, b, l$  all possible polarizations,  $F_A$  the antenna pattern function.

• Overlap reduction function (how much degree of correlation is preserved between detectors)

 $\gamma_{IJ}^{M}(f) = \frac{1}{\sin^{2}\chi} \left( \rho_{1}^{M}(\alpha) D_{I}^{ij} D_{ij}^{J} + \rho_{2}^{M}(\alpha) D_{I,k}^{i} D_{J}^{kj} \hat{d}_{i} \hat{d}_{j} + \rho_{3}^{M}(\alpha) D_{I}^{ij} D_{J}^{kl} \hat{d}_{i} \hat{d}_{j} \hat{d}_{k} \hat{d}_{l} \right)$ 

with  $\rho_i^M = f(j_0(\alpha), j_2(\alpha), j_4(\alpha)), \hat{d}_i = \frac{\mathbf{x}}{|\mathbf{x}|}, \alpha = \frac{2\pi f |\mathbf{x}|}{c}, M = T, V, S$ • GW background energy density  $\Omega_{gw}^T = \Omega_{gw}^+ + \Omega_{gw}^{\times}$  (similar for  $\Omega_{gw}^V$  and  $\Omega_{gw}^S$ ), related to the one-sided power spectral density  $S(|f|) \propto \langle \tilde{h}_A^*(f, \hat{\Omega}) \tilde{h}_{A'}(f', \hat{\Omega'}) \rangle$  by  $\Omega_{gw}^M(f) \propto f^3 S_h^A(f)$ 

 $\bullet$  The tensor, vector and scalar modes can then be separately detected via

$$SNR^{M} \propto \int_{0}^{\infty} \mathrm{d}f \left[ \frac{(\Omega_{\mathrm{gw}}^{M}(f))^{2} \det \mathbf{F}(f)}{f^{6} \mathcal{F}_{M}(f)} \right]^{(1/2)}$$
  
here the elements of the (3 × 3)-matrix **F** are given by  $F_{MM'} = \sum_{\mathrm{det}\,\mathrm{gain}} \mathrm{d}t \frac{\gamma_{IJ}^{M}(t,f)\gamma_{i}^{M'}(t,f)}{P_{I}(f)P_{J}(f)}$ 

## Stochastic GW background : single detector [7]

• If the output data of the single detector is written as h(t) + n(t), with n(t) the noise, the autocorrelation of the signal reads

 $\langle \tilde{h}(f)\tilde{h}^*(f')\rangle = \frac{1}{2}\delta(f-f')S_h(|f|)$ 

with  $S_h(|f|)$  the one-sided power spectral density; one can define  $S_n$  in a similar way for the noise.

 $\bullet$  The maximum SNR given by this process is

$$SNR^{2} = \frac{T}{2} \int_{-\infty}^{\infty} \mathrm{d}f \, \frac{S_{h}(|f|)^{2}}{\left[S_{h}(|f|) + S_{n}(|f|)\right]^{2}}$$

 $\Rightarrow$  Also valid in the high-frequency limit, for a single detector, but for an unpolarized GWB

### Possible solutions for eLISA

- Cross-correlating the TDI combinations of a LISA-like single detector also correlates the noise
- $\bullet$  The separation of all modes however requires a network of detectors
- Work in progress

det pairs

⇒ Valid for a network of independant detectors in space (3 LISA-like detectors would be sufficient), in the low frequency limit, and for a full polarized GWB

 $\Rightarrow$  "Static" system (the relative position of the detectors in the network doesn't change)

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-Letting eLISA evolve on its orbit and correlating the signals at different time

-Correlating eLISA signal with future earth-based detectors around 1Hz

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[2] Nishizawa A. et al., Phys. Rev. D **79**, 082002 (2009)

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