

Relationships involving the thermodynamic potentials.

Thermodynamic Potential	Independent Variables	Reciprocity Relations	Maxwell Relations
Internal energy U	S, V $dU = T dS - P dV$	$T = \left(\frac{\partial U}{\partial S}\right)_V$ $-P = \left(\frac{\partial U}{\partial V}\right)_S$	$\left(\frac{\partial T}{\partial V}\right)_S = -\left(\frac{\partial P}{\partial S}\right)_V$ $= \frac{\partial^2 U}{\partial V \partial S}$
Enthalpy $H = U + PV$	S, P $dH = T dS + V dP$	$T = \left(\frac{\partial H}{\partial S}\right)_P$ $V = \left(\frac{\partial H}{\partial P}\right)_S$	$\left(\frac{\partial T}{\partial P}\right)_S = \left(\frac{\partial V}{\partial S}\right)_P$ $= \frac{\partial^2 H}{\partial P \partial S}$
Helmholtz function $F = U - TS$	T, V $dF = -S dT - P dV$	$S = -\left(\frac{\partial F}{\partial T}\right)_V$ $-P = \left(\frac{\partial F}{\partial V}\right)_T$	$\left(\frac{\partial S}{\partial V}\right)_T = \left(\frac{\partial P}{\partial T}\right)_V$ $= -\frac{\partial^2 F}{\partial V \partial T}$
Gibbs function $G = U - TS + PV$ $= H - TS$	T, P $dG = -S dT + V dP$	$S = -\left(\frac{\partial G}{\partial T}\right)_P$ $V = \left(\frac{\partial G}{\partial P}\right)_T$	$\left(\frac{\partial S}{\partial P}\right)_T = -\left(\frac{\partial V}{\partial T}\right)_P$ $= -\frac{\partial^2 G}{\partial P \partial T}$