

Summary of Material Covered on Exam 1

1 Relativistic kinematics

Natural units, expressing momentum and mass as energies

Putting in factors of \hbar and c to make formulae correct

Definition of $\alpha = e^2 / 4\pi\epsilon_0\hbar c \approx 1/137$

Relations between E , p , v and m : $E^2 = p^2 + m^2$, $v = p / E$, $\gamma = E / m = 1 / \sqrt{1 - v^2}$

Transforming energy and momentum between reference frames

Lifetime: time dilation and average decay distance of moving particle

4-vectors and 4-momentum, definition of p^2 and $p_1 \cdot p_2$ Lorentz invariants

Two body kinematics: determining energy and momentum from masses

Center of mass and lab (fixed target) frames

Shrinking of angles wrt beam for large incident momenta in lab frame

Calculating threshold energy for particle production

2 Leptons, Quarks and fundamental forces

Fundamental forces and unification

Force carriers for each force

Leptons and quarks

Which forces are felt by charged leptons, neutrinos, quarks, hadrons?

Organization of quarks and leptons into doublets covering three generations

Lepton quantum numbers

Quark quantum numbers (S, C, B, T); baryon number

Hadrons: mesons and baryons

Particle multiplets, similar masses for particles differing by u and d quark

EM splitting within a multiplet

Composite particles (mesons, baryons) vs point particles (leptons and quarks)

Approximate masses of basic hadrons and leptons

Spin 1/2 baryons and spin 3/2 baryons:

Quark content

Which decay strongly and which decay weakly. Special case of the Ω^-

Diagram of particles by charge and strangeness

Spin 0 and spin 1 mesons:

Quark content

Which decay strongly and which decay weakly.

Diagram of particles by charge and strangeness

Which decays are allowed or forbidden by strong, E&M, weak forces

3 Quantum mechanics

Schrodinger's equation and the wavefunction $\psi(x,t)$ (1-D) and $\psi(\mathbf{x},t)$ (3-D)

Stationary states: $\psi(x,t) = \psi(x)e^{-iEt/\hbar}$

Quantization of energy and ang. momentum in QM from boundary conditions and normalization

Operators in QM

Special operators such as momentum, energy, angular momentum (L^2, L_z)

Eigenstates and eigenvalues of operators

Special potentials:

$U = 0$ everywhere; free particle wavefunctions

Infinite square well and its solutions (1-D, 3-D)

Energy levels for 1-D and 3-D systems, degeneracy

Hydrogen atom quantum numbers, energies, degeneracies

Uncertainty principle

Using the uncertainty principle to establish minimum kinetic energies of bound systems of a specified size (atomic, nuclear, etc).

4 Cross sections and luminosity

Particle flux, total particle flux

Luminosity, integrated luminosity, cross section and scattering rates

Calculating luminosity from beam and target information

Exponential decrease of flux intensity inside target, scattering length $\lambda = 1/\sigma n_t$

Nuclear collision length, nuclear interaction length (including density adjusted value)

Solid angle differential $d\Omega = d\cos\theta d\phi = \sin\theta d\theta d\phi$

Using basic Feynman diagrams to represent fundamental processes

Exchanging heavy particles, range of interaction $r \approx 1/m$, for exchange particle mass m

Weak interactions and W exchange

Basics of Rutherford scattering