

Cylindrical $\nabla \times \mathbf{A} = \left[\frac{1}{s} \frac{\partial A_z}{\partial \phi} - \frac{\partial A_\phi}{\partial z} \right] \hat{s} + \left[\frac{\partial A_s}{\partial z} - \frac{\partial A_z}{\partial s} \right] \hat{\phi} + \frac{1}{s} \left[\frac{\partial (sA_\phi)}{\partial s} - \frac{\partial A_s}{\partial \phi} \right] \hat{z}$ $\bar{\nabla} f = \hat{s} \frac{\partial f}{\partial s} + \hat{\phi} \frac{1}{s} \frac{\partial f}{\partial \phi} + \hat{z} \frac{\partial f}{\partial z}$
 $\nabla \cdot \mathbf{A} = \frac{1}{s} \frac{\partial (sA_s)}{\partial s} + \frac{1}{s} \frac{\partial A_\phi}{\partial \phi} + \frac{\partial A_z}{\partial z}$ $d\tau = s ds d\phi dz$ $da = s d\phi dz$ $dl = ds \hat{s} + s d\phi \hat{\phi} + dz \hat{z}$
 $\nabla^2 V = \frac{1}{s} \frac{\partial}{\partial s} \left(s \frac{\partial V}{\partial s} \right) + \frac{1}{s^2} \frac{\partial^2 V}{\partial \phi^2} + \frac{\partial^2 V}{\partial z^2}$ $dl = dr \hat{r} + r d\theta \hat{\theta} + r \sin\theta d\phi \hat{\phi}$ Polar (2d) $da = r dr d\theta$

Spherical $\bar{\nabla} = \hat{r} \frac{\partial f}{\partial r} + \hat{\theta} \frac{1}{r} \frac{\partial f}{\partial \theta} + \hat{\phi} \frac{1}{r \sin\theta} \frac{\partial f}{\partial \phi}$ $da = r^2 d\theta \sin\theta d\phi$ $d\tau = dr da = r^2 dr d\theta \sin\theta d\phi$
 $\nabla \times \mathbf{A} = \frac{1}{r \sin\theta} \left[\frac{\partial}{\partial \theta} \sin\theta A_\phi - \frac{\partial A_\theta}{\partial \phi} \right] \hat{r} + \frac{1}{r} \left[\frac{1}{\sin\theta} \frac{\partial A_r}{\partial \phi} - \frac{\partial}{\partial r} (rA_\phi) \right] \hat{\theta} + \frac{1}{r} \left[\frac{\partial (rA_\theta)}{\partial r} - \frac{\partial A_r}{\partial \theta} \right] \hat{\phi}$
 $\nabla \cdot \mathbf{A} = \frac{1}{r^2} \frac{\partial}{\partial r} (r^2 A_r) + \frac{1}{r \sin\theta} \frac{\partial}{\partial \theta} (\sin\theta A_\theta) + \frac{1}{r \sin\theta} \frac{\partial A_\phi}{\partial \phi}$ $\nabla^2 V = \frac{1}{r^2} \frac{\partial}{\partial r} (r^2 \frac{\partial V}{\partial r}) + \frac{1}{r^2 \sin\theta} \frac{\partial}{\partial \theta} (\sin\theta \frac{\partial V}{\partial \theta}) + \frac{1}{r^2 \sin^2\theta} \frac{\partial^2 V}{\partial \phi^2}$

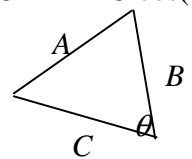
Cartesian $\nabla \cdot \mathbf{A} = \frac{\partial A_x}{\partial x} + \frac{\partial A_y}{\partial y} + \frac{\partial A_z}{\partial z}$ $\bar{\nabla} f = \hat{x} \frac{\partial f}{\partial x} + \hat{y} \frac{\partial f}{\partial y} + \hat{z} \frac{\partial f}{\partial z}$ $\nabla \times \mathbf{A} = \begin{vmatrix} \hat{x} & \hat{y} & \hat{z} \\ \partial/\partial x & \partial/\partial y & \partial/\partial z \\ A_x & A_y & A_z \end{vmatrix}$ $d\tau = dx dy dz$
 $dl = dx \hat{x} + dy \hat{y} + dz \hat{z}$ *Laplacian* $\nabla^2 V = \nabla \cdot (\nabla V)$

Electrostatics $\mathbf{E} = \frac{q}{4\pi\epsilon_0} \frac{\hat{r}}{r^2}$ $\nabla^2 V = -\frac{\rho}{\epsilon_0}$ $\mathbf{E} = -\nabla V$ $\mathbf{E} = \frac{1}{4\pi\epsilon_0} \int \frac{\hat{\zeta}}{\zeta^2} \rho(r') d\tau'$ where $\vec{\zeta} = \mathbf{r} - \mathbf{r}'$
 $V(\mathbf{r}) = \frac{1}{4\pi\epsilon_0} \int_{\text{surface}} \frac{\sigma(\mathbf{r}')}{|\mathbf{r} - \mathbf{r}'|} da'$ $V(\mathbf{r}) = \frac{1}{4\pi\epsilon_0} \int_{\text{volume}} \frac{\rho(\mathbf{r}')}{|\mathbf{r} - \mathbf{r}'|} d\tau'$ $V(r, \theta) = \sum_{l=0}^{\infty} \left(A_l r^l + \frac{B_l}{r^{l+1}} \right) P_l(\cos\theta)$
 $\nabla^2 V = 0 \Rightarrow \frac{1}{X} \frac{d^2 X}{dx^2} + \frac{1}{Y} \frac{d^2 Y}{dy^2} + \frac{1}{Z} \frac{d^2 Z}{dz^2} = 0$ $dq = \rho d\tau = \sigma da = \lambda dx$ $W = \frac{\epsilon_0}{2} \int_{\text{all space}} E^2 d\tau$
Gauss's Law: $\nabla \cdot \mathbf{E} = \frac{\rho}{\epsilon_0}$ $V(r_b) - V(r_a) = -\int_{r_a}^{r_b} \mathbf{E} \cdot d\mathbf{l}$ $E_{\perp}^{\text{above}} - E_{\perp}^{\text{below}} = \frac{\sigma}{\epsilon_0}$

Magnetostatics $\mathbf{I} = \lambda \mathbf{v}$ $\mathbf{K} = \sigma \mathbf{v}$ $\mathbf{J} = \rho \mathbf{v}$ $\mathbf{K}_b = \mathbf{M} \times \mathbf{n}$ $\mathbf{J}_b = \text{curl}(\mathbf{M})$ $\mathbf{B} = \nabla \times \mathbf{A}$ $\mathbf{H} = \frac{\mathbf{B}}{\mu_0} - \mathbf{M}$ $\nabla \times \mathbf{H} = \mathbf{J}_{\text{free}}$
 $\mathbf{B}(\mathbf{r}) = \frac{\mu_0}{4\pi} \int \frac{\mathbf{J}(\mathbf{r}') \times \hat{\zeta}}{\zeta^2} = \frac{\mu_0}{4\pi} \int \frac{\mathbf{J} \times \hat{\zeta}}{\zeta^2} d\tau'$ where $\vec{\zeta} = \mathbf{r} - \mathbf{r}'$ $\nabla^2 \mathbf{A} = -\mu_0 \mathbf{J}$ $I_{\text{enc}} = \int \mathbf{J} \cdot d\mathbf{a}$
 $\nabla \times \mathbf{B} = \mu_0 \mathbf{J} \rightarrow \oint \mathbf{B} \cdot d\mathbf{l} = \mu_0 I_{\text{enc}}$ $\nabla \cdot \mathbf{B} = 0$ $\mathbf{B}_{\text{dip}} = \frac{\mu_0 m}{4\pi r^3} (2 \cos\theta \hat{r} + \sin\theta \hat{\theta})$
 $\mathbf{F} = q\mathbf{v} \times \mathbf{B}$ $d\mathbf{F} = I d\mathbf{l} \times \mathbf{B} = da \mathbf{K} \times \mathbf{B} = d\tau \mathbf{J} \times \mathbf{B}$

Dipoles etc. $\mathbf{p} = \int_{\text{volume}} \mathbf{r}' \rho(\mathbf{r}') d\tau' = \sum_i \mathbf{r}_i q_i$ $V(\mathbf{r}) = \frac{1}{4\pi\epsilon_0} \sum_{n=0}^{\infty} \frac{1}{r^{n+1}} \int_{\text{volume}} d\tau' (r')^n P_n(\cos(\theta')) \rho(\mathbf{r}')$ $V_{\text{dipole}}(\mathbf{r}) = \frac{1}{4\pi\epsilon_0} \frac{\mathbf{p} \cdot \hat{r}}{r^2}$
 $\sigma_b = \mathbf{P} \cdot \hat{\mathbf{n}}$ $\rho_b = -\nabla \cdot \mathbf{P}$ $V(\mathbf{r}) = \frac{1}{4\pi\epsilon_0} \sum_{n=0}^{\infty} \frac{1}{r^{n+1}} \sum_{\text{charges } i} dq_i r_i^n P_n(\cos(\theta_i))$
 $\mathbf{E}_{\text{dip}} = \frac{p}{4\pi\epsilon_0 r^3} (2 \cos\theta \hat{r} + \sin\theta \hat{\theta})$ $\mathbf{N} = \mathbf{p} \times \mathbf{E}$ or $\mathbf{N} = \mathbf{m} \times \mathbf{B}$, $\mathbf{F} = \nabla(\mathbf{p} \cdot \mathbf{E})$ or $\nabla(\mathbf{m} \cdot \mathbf{B})$
Linear dielectric: $\mathbf{P} = \chi_e \epsilon_0 \mathbf{E}$, where $\mathbf{p} = \mathbf{P} d\tau$
 $\mathbf{D} = \epsilon_0 \mathbf{E} + \mathbf{P}$ $\nabla \cdot \mathbf{D} = \rho_{\text{free}}$ $\mathbf{P} = \epsilon_0 \chi_e \mathbf{E}$ (*linear dielectrics*) $\mathbf{D} = \epsilon_0 (1 + \chi_e) \mathbf{E} = \epsilon \mathbf{E}$

Theorems, constants, etc. $\epsilon_0 = 8.85 \times 10^{-12} \text{ C}^2/\text{Nm}^2$ $\mu_0 = 4\pi \times 10^{-7} \text{ N/A}^2$ $A^2 = B^2 + C^2 - 2BC \cos(\theta)$
Stokes Theorem $\rightarrow \int (\nabla \times \mathbf{A}) \cdot d\mathbf{a} = \oint \mathbf{A} \cdot d\mathbf{l}$ $\int_{\text{volume}} \nabla \cdot \mathbf{A} d\tau = \oint_{\text{surface}} \mathbf{A} \cdot d\mathbf{a}$
 $P_0(x) = 1$, $P_1(x) = x$, $P_2(x) = \frac{1}{2}(3x^2 - 1)$, ... *Divergence Theorem*



Some integrals.

$$\int_0^{\pi} d(\cos \theta) P_m(\cos \theta) P_l(\cos \theta) = \begin{cases} 0 & \text{if } m \neq l \\ \frac{2}{2m+1} & \text{if } m = l \end{cases}$$

$$\int \sin^3 x \, dx = \frac{-1}{3} \cos(x)(\sin^2 x + 2) \quad \int \sin^4 x = \frac{3x}{8} - \frac{\sin(2x)}{4} + \frac{\sin(4x)}{32}$$

$$\int \frac{dx}{(x^2 + a^2)^{3/2}} = \frac{x}{a^2 \sqrt{x^2 + a^2}} \quad \int_0^a \sin\left(\frac{n\pi x}{a}\right) \sin\left(\frac{m\pi x}{a}\right) dx = \begin{cases} 0 & \text{if } n \neq m \\ a/2 & \text{if } n = m \end{cases}$$

$$\int \sin(kx) dx = \frac{-1}{k} \cos(kx) \quad \int \frac{\sin(\theta) d\theta}{\sqrt{1 - \cos(\theta)}} = 2\sqrt{1 - \cos(\theta)} \quad \int \cos(kx) dx = \frac{1}{k} \sin(kx)$$