## PHY 2060 Fall 2005 - Exam 1

Instructions: Attempt all ten questions, each of which carries a maximum of 10 points. You will receive credit only for knowledge and understanding that you demonstrate in your written solutions. To maximize your score, you should briefly explain your reasoning and show all working. Give all final answers in terms of variables defined in the problem (and possibly also $g$, the acceleration due to gravity). Please try to write neatly!

During this exam, you may use a single formula sheet. You are not permitted to consult any other books, notes, or papers, to use calculators or any other electronic device, or to communicate with anyone other than the proctor. In accordance with the UF Honor Code, by turning in this exam to be graded, you affirm the following pledge: On my honor, I have neither given nor received unauthorized aid in doing this assignment.

1. An object moving in one dimension is observed to have a position $x$ that varies with time $t$ according to $x(t)=x_{0} \cos (2 \pi t / \tau)$, where $x_{0}=10 \mathrm{~cm}$ and $\tau=3$ seconds.
(a) Determine the particle's velocity $v(t)$ and acceleration $a(t)$.
(b) What is the maximum velocity, and at what position(s) does it occur?
(c) What is the maximum acceleration, and at what position(s) does it occur?
2. Two blocks rest on a horizontal, frictionless surface, and are connected by an ideal string, which is also horizontal. Mass $m_{1}$ is subjected to a force of magnitude $F_{1}$, and mass $m_{2}$ is subjected to a force of magnitude $F_{2}$, directed as shown in the figure.
(a) What is the acceleration of mass $m_{1}$ ?
(b) What is the tension in the string?

3. A plane flying at a constant airspeed of $120 \mathrm{~km} / \mathrm{hr}$ has enough fuel to power the engine for only another 17 minutes. The pilot hopes to reach a landing strip located 32 km due north of the plane's current position. The pilot is initially unaware that there is a $30 \mathrm{~km} / \mathrm{hr}$ wind heading due west. However, after 12 minutes of steering due north, the pilot realizes that the plane is being blown off course and corrects the plane's heading to properly take the wind into account.
(a) At the moment the plane corrects course, how far is it from the landing strip?
(b) Still flying at an airspeed of $120 \mathrm{~km} / \mathrm{hr}$, can the plane reach the landing strip before the fuel runs out? Explain your answer.

You should be able to do all necessary arithmetic without the aid of a calculator. It may be helpful to recall that $60 \mathrm{~km} / \mathrm{hr}=1 \mathrm{~km} / \mathrm{min}$ and that $3^{2}+4^{2}=5^{2}$.
4. A construction worker stands in a crane bucket that is being lowered vertically downward at a constant speed $v_{b}$. The worker throws a pebble vertically upward at a speed $v_{p}$ relative to the bucket. If the pebble is released at a height $h$ above the ground, what is the greatest distance above the ground that the pebble reaches during its subsequent motion? You may ignore drag forces and the possibility that the pebble hits anything else before reaching the ground.
5. A block of mass $m$ rests on a plane inclined at an angle $\theta$ above the horizontal. To prevent the block sliding down the incline, a horizontal force of minimum magnitude $F$ must be applied to the block.
(a) Find the magnitude of the normal force exerted on the block by the plane.

(b) Find the coefficient of static friction between the block and the plane.
6. Two beads $A$ and $B$, of masses $m_{A}$ and $m_{B}$, are attached at different points to an ideal string, which is then twirled in a horizontal plane so that the beads pursue circular motion about point $O$ with radii $r_{A}$ and $r_{B}$, respectively. The outer bead $(A)$ is observed to have a constant speed $v_{A}$.
(a) Find the tension $T_{1}$ in the string between $A$ and $B$.
(b) Find the tension $T_{2}$ in the string between $B$ and $O$.

7. Three blocks $\left(A, B, C\right.$ of masses $m_{A}, m_{B}$, $m_{C}$, respectively) are connected by two ideal strings (1, 2) running over massless pulleys, as shown in the diagram. There is no friction in the system. Find the mass $m_{C}$ that causes block $B$ to ...
(a) move up the incline with a constant speed $v$.
(b) move up the incline with a constant acceleration $a=g / 2$.

8. You want to fire a dart from a blowgun pointing at a fixed angle $\phi_{0}$ above the horizontal ground. Your goal is for the dart to pass over the top of a wall of height $h$ that stands with its base a distance $d$ from the firing point. By blowing harder or more softly, you can vary the initial speed $v_{0}$ with which the dart leaves the blowgun.
(a) What is the minimum initial speed with which the dart must be launched in order for it to pass over the top of the wall?
(b) What is the maximum height of wall that it is possible for the projectile to pass over (for fixed $d$, $\phi_{0}$, and $\left.g\right)$ ?

9. A runaway railway locomotive traveling at a steady speed $v_{r}$ is spotted passing through a station. After a delay time $T$, a pursuit party sets off from the station on a track parallel to the runaway's. The pursuit locomotive undergoes a constant acceleration $a_{p}$ from rest until it reaches its top speed $v_{p}$ (where $v_{p}>v_{r}$ ), which it then maintains until it catches up with the runaway. How far along the tracks from the station does the pursuit locomotive overhaul the runaway?
10. Two identical slabs of polished granite sit on top of one another on a concrete ramp, which is inclined at an angle $\theta$ to the horizontal. The upper slab starts sliding downward along the top of the lower slab, which in turn starts sliding down the ramp. The coefficient of kinetic friction between the two slabs is $\mu_{g}$, while the coefficient of ki-
 netic friction between the granite and concrete surfaces is $\mu_{c}$ (where $\mu_{c}>\mu_{g}$ ).
Find the acceleration (a) $a_{u}$ of the upper slab, (b) $a_{l}$ of the lower slab.

