

Ohm's law on a lattice:

$$j_i = \sigma_{ij} E_j$$

Conductivity tensor

$$\hat{\sigma} = \begin{pmatrix} \sigma_{xx} & \sigma_{xy} \\ \sigma_{yx} & \sigma_{yy} \end{pmatrix} \quad (1)$$

How many independent components does an oblique lattice have?

The only symmetry operation is the 180 rotation about z .

Matrix of rotation about z by θ :

$$U_\theta = \begin{pmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{pmatrix} \Rightarrow \quad (2)$$

$$U_{180} = \begin{pmatrix} -1 & 0 \\ 0 & -1 \end{pmatrix} = -1 \times \mathbb{1} \quad (3)$$

Transformation of the Ohm's law under rotation

$$\hat{U} \vec{j} = \hat{U} \hat{\sigma} \hat{U}^{-1} \hat{U} \vec{E} \Rightarrow \hat{\sigma} \rightarrow \hat{U} \hat{\sigma} \hat{U}^{-1} \quad (4)$$

For rotations, $\hat{U} \hat{=} U^{-1} \Rightarrow$

$$\hat{\sigma} = \hat{U} \hat{\sigma} \hat{U} \quad (5)$$