

**Discovering and Testing
Dark Matter in the Lab**

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The Dark Matter Problem

- Two of the biggest mysteries in (astro)particle physics today

What, how and why breaks the electroweak gauge symmetry?

- SM answer: new particle, Higgs boson. Will be discovered and studied at the LHC and ILC. But... gauge hierarchy problem.
- Many models BSM were proposed to address this issue, collider experiments will tell us which one is right *in our lifetime*. Generic prediction: more new particles.

- With all due respect to the gauge hierarchy problem, dark matter is our best **experimental** evidence for new physics BSM.

What is the nature of the dark matter and the dark energy?

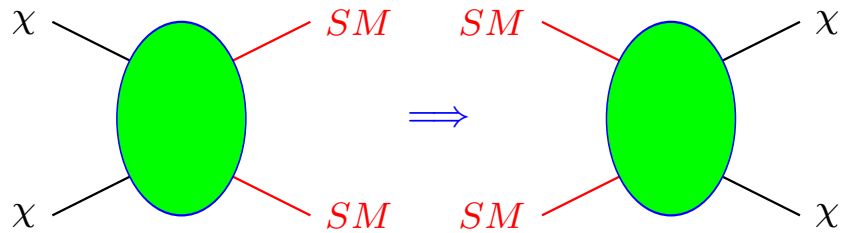
- Perhaps the two puzzles are related? \implies WIMPs?
- The advantage of cosmological WIMPs
 - Predicted in many particle physics scenarios BSM.
 - Give the right order of magnitude Ω_{DM} .

$$\Omega_{DM} h^2 \sim 0.1 \left(\frac{\sigma_{EW}}{\sigma_{ann}} \right)$$

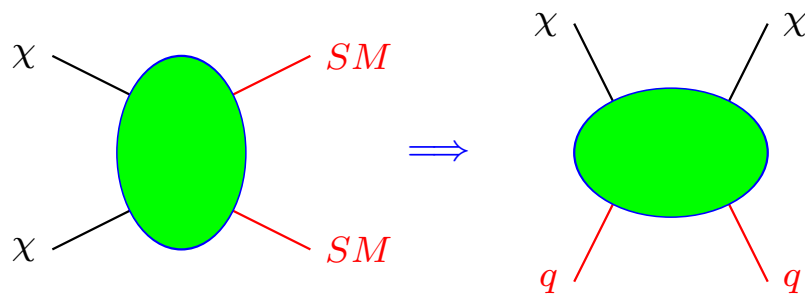
- Can be detected!
- Can be detected in different ways!

Avenues for WIMP detection

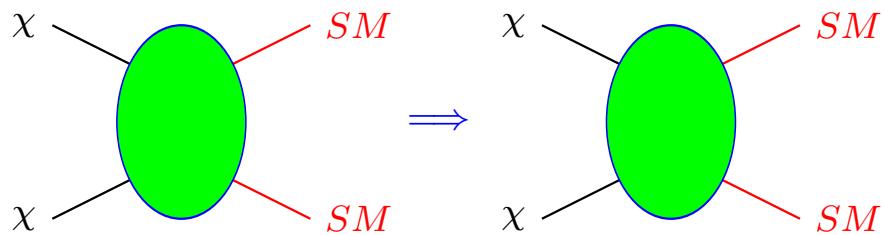
- Potentially observable signals at colliders



- Potentially observable signals of direct DM detection.



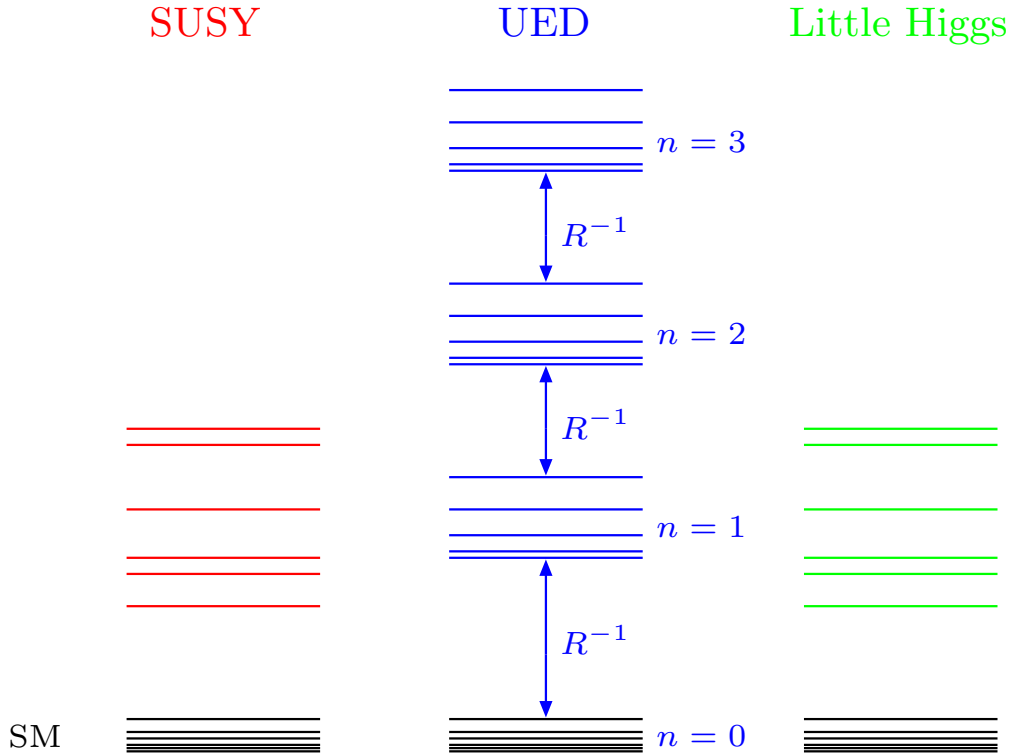
- Potentially observable signals of indirect DM detection.



New physics models with DM WIMPs

- Recipe for BSM dark matter
 - invent a model with new particles
 - invent a symmetry which guarantees a stable new particle
 - fudge parameters until the lightest new stable particle is neutral and has the correct relic density
- Three generic examples of new physics with a DM WIMP
 - supersymmetry: DM = lightest superpartner.
 - extra dimensions: DM = lightest Kaluza-Klein mode.
 - Little Higgs: DM = LPOP, LZOP? (billion, gatesino, ...)
- Brief review, discovery prospects
- How can we distinguish the different scenarios?
 - at high energy colliders
 - in astroparticle physics experiments
- How well can we test cosmology at the LHC/ILC?
- A model independent framework for discussing DM signals
 - at high energy colliders
 - in astroparticle physics experiments

Model Summary



	SUSY	UED	Little Higgs
Symmetry	R -parity	KK-parity	T -parity
DM particle	LSP	LKP	LTP
Spin	1/2	1	0
Mass range	50-200 GeV	600-800 GeV	400-800 GeV

Supersymmetry

- Supersymmetry is an extra dimension theory with new **anticommuting** coordinates $\theta_\alpha \implies$ superspace $\{x^\mu, \theta\}$:

$$\Phi(x^\mu, \theta) = \phi(x^\mu) + \psi^\alpha(x^\mu)\theta_\alpha + F(x^\mu)\theta^\alpha\theta_\alpha$$

- SUSY relates **SM particles** and their **superpartners** ($\phi \leftrightarrow \psi$)
 - quarks, leptons \Leftrightarrow squarks, sleptons
 - gauge bosons: $g, W^\pm, W_3^0, B^0 \Leftrightarrow$ gauginos: $\tilde{g}, \tilde{w}^\pm, \tilde{w}^0, \tilde{b}^0$
 - Higgs bosons: $h^0, H^0, A^0, H^\pm \Leftrightarrow$ higgsinos: $\tilde{h}^\pm, \tilde{h}_u^0, \tilde{h}_d^0$
 - graviton: $G \Leftrightarrow$ gravitino: \tilde{G}
- The superpartners have
 - spins differing by 1/2
 - identical couplings
 - unknown masses (model-dependent)
- Prove discovery of SUSY \iff prove the above
- The superpartners are charged under a conserved R -parity
 - **SM particles**: $R = +1$
 - **superpartners**: $R = -1 \implies$ stable LSP (DM?).
- No tree-level contributions to precision electroweak data

SUSY WIMPs

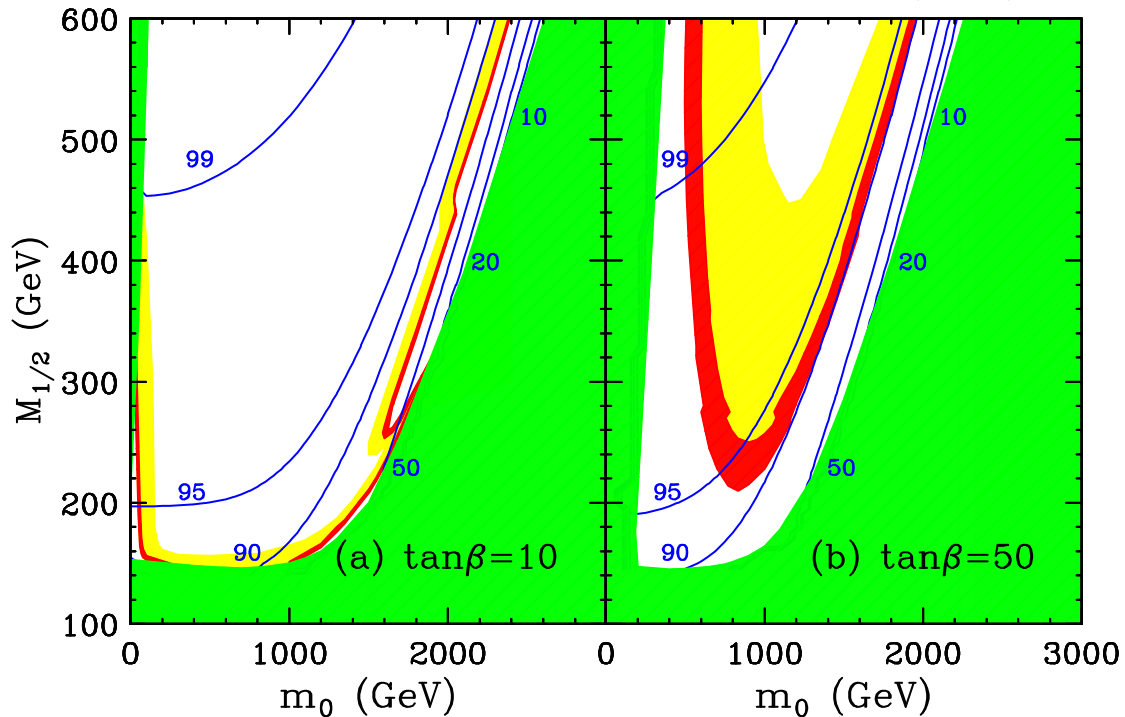
- The lightest neutralino $\tilde{\chi}_1^0$ is a mixture of \tilde{b}^0 , \tilde{w}^0 , \tilde{h}_u^0 , \tilde{h}_d^0 :

$$\tilde{\chi}_1^0 = a_1 \tilde{b}^0 + a_2 \tilde{w}^0 + a_3 \tilde{h}_u^0 + a_4 \tilde{h}_d^0$$

- Gaugino fraction R_χ of the LSP:

$$R_\chi \equiv |a_1|^2 + |a_2|^2 \approx |a_1|^2.$$

Feng, KM, Wilczek (2000)



- Focus point region: large m_0 , mixed LSP.
- Coannihilation region: small m_0 , $\tilde{\tau} - \tilde{\chi}_1^0$ degeneracy.

Universal Extra Dimensions

Appelquist, Cheng, Dobrescu, hep-ph/0012100

- Universal Extra Dimensions is an extra dimension theory with new bosonic coordinates y (spanning a circle of radius R):

$$\Phi(x^\mu, y) = \phi(x^\mu) + \sum_{i=1}^{\infty} \phi^n(x^\mu) \cos(ny/R) + \chi^n(x^\mu) \sin(ny/R)$$

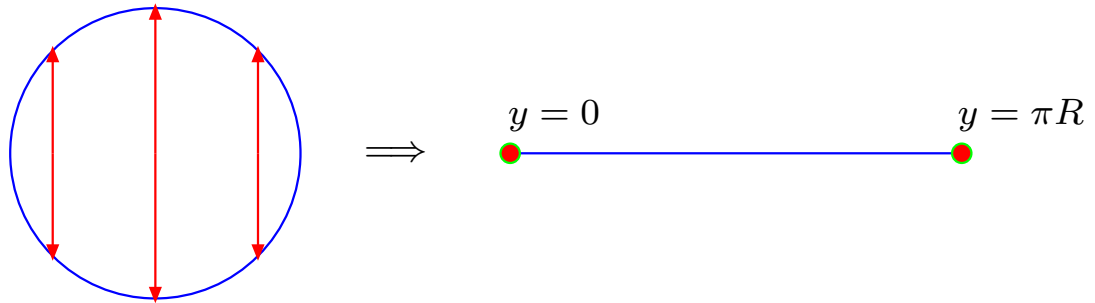
- Each SM field ϕ ($n = 0$) has an infinite tower of Kaluza-Klein (KK) partners ϕ^n and χ^n with
 - identical spins
 - identical couplings
 - unknown masses of order n/R
- Prove discovery of UED \iff prove the above
- KK number $n \iff$ units of p_y .
- Bulk interactions: conserve KK number $\iff p_y$ conservation.

$$S = \int d^4x dy \mathcal{L}_{SM}$$

- Problem: chiral fermions.

KK number versus KK parity

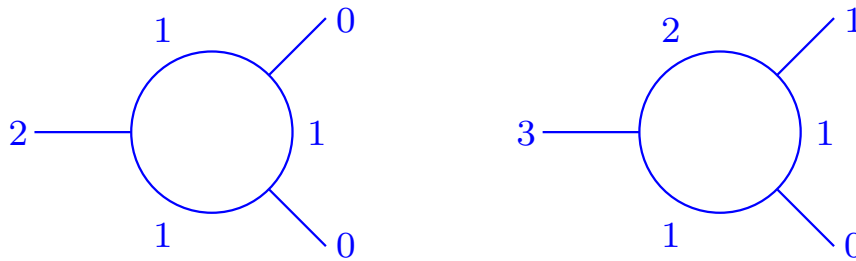
- The ED is not really a circle, but orbifold S_1/Z_2 :



- Loop corrections generate boundary terms

$$S = \int d^4x dy \left[\delta(y) + \delta(y - \pi R) \right] \left\{ F_4(\mu) \bar{\Psi} i \not{D} \Psi + \dots \right\}$$

which break KK number n down to KK parity $(-1)^n$

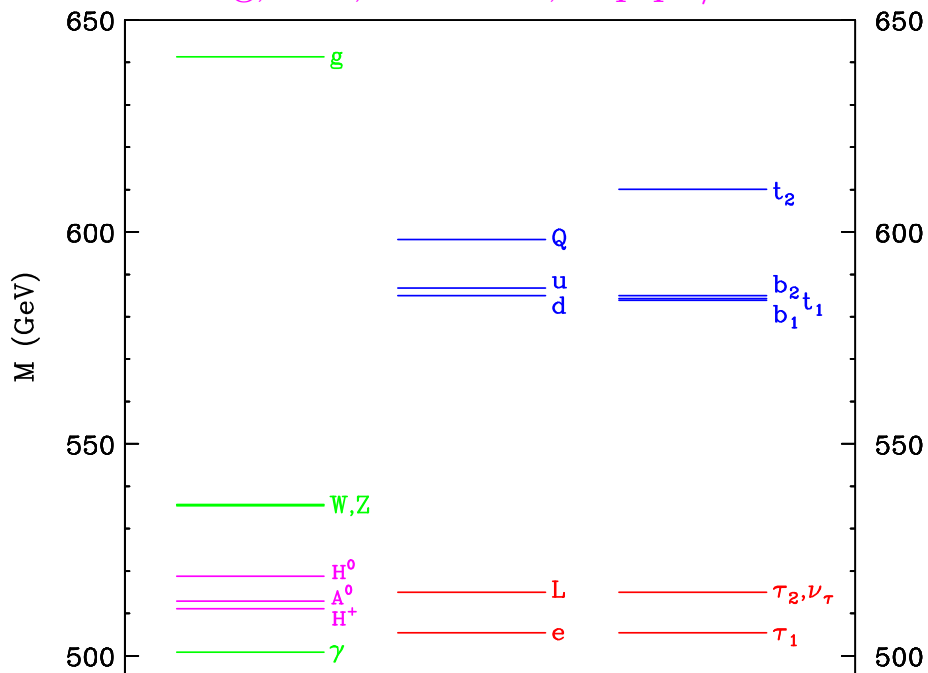


- Additional allowed decays: $2 \rightarrow 00$, $3 \rightarrow 10$, ...
- The lightest KK partner at level 1 (LKP) is stable. (DM?)
- No tree-level contributions to precision EW observables

UED spectrum at 1 loop

- Including radiative corrections, the mass spectrum of level 1 KK modes looks something like this:

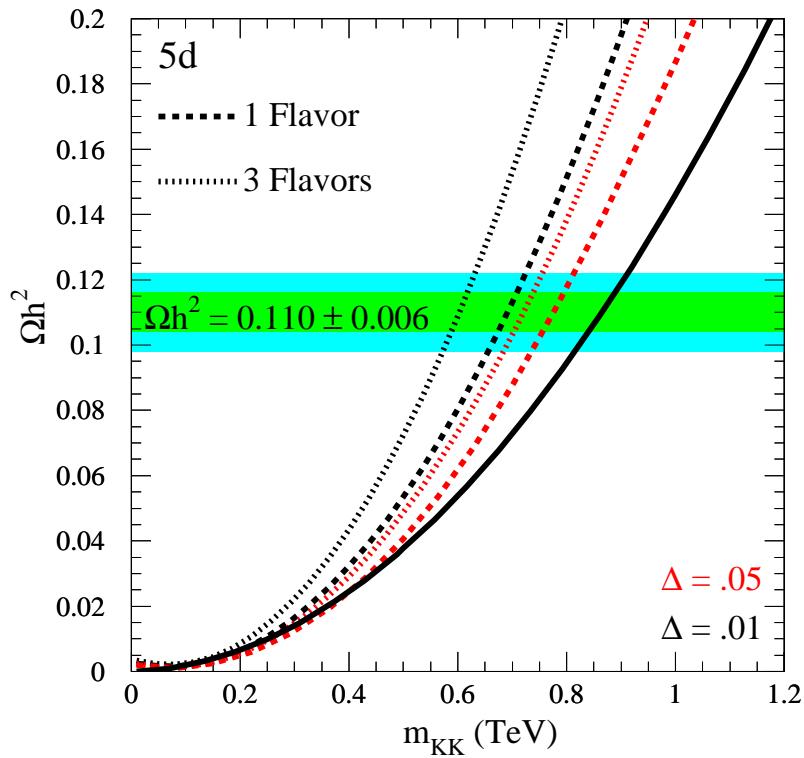
Cheng, KM, Schmaltz, hep-ph/0204342



- Mimics supersymmetry: prompt decays!
- Seems difficult to discover at the LHC, but...
- W_1^\pm, Z_1 have pure leptonic branchings!
- $\sin^2 \theta_W^1 \approx 0 \implies \gamma^1 \approx B^1$, similar to \tilde{B} in SUSY.

KK dark matter relic density

- Relic density: G.Servant, T.Tait, hep-ph/0206071



- Unlike supersymmetry: no helicity suppression

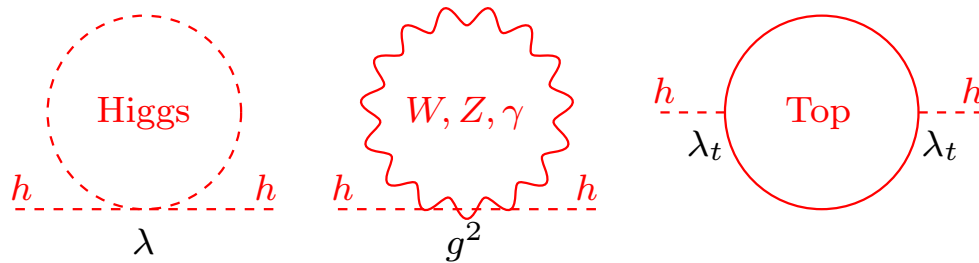
$$\Omega h^2 = \frac{1.04 \cdot 10^9 \text{ GeV}^{-1}}{M_P \sqrt{g_*}} \frac{x_F}{a + 3b/x_F}; \quad x_F = \frac{M_{KK}}{T_F}$$

$$a = \frac{\alpha_1^2}{M_{KK}^2} \frac{380\pi}{81}; \quad b = -\frac{\alpha_1^2}{M_{KK}^2} \frac{95\pi}{162}.$$

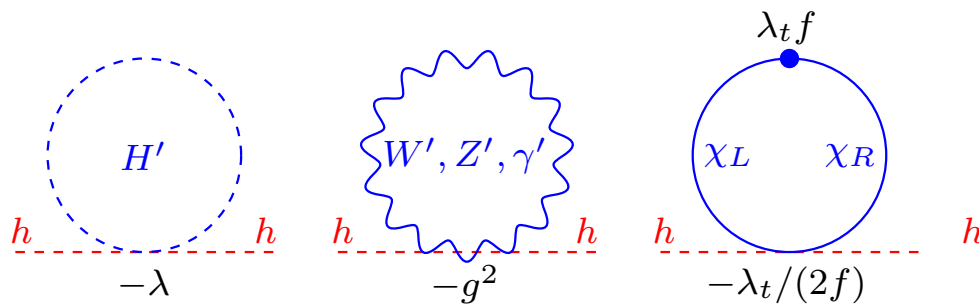
- Unlike supersymmetry: coannihilation lowers the bound

Little Higgs models

- The hierarchy problem in the SM



- Introduce new particles at TeV scale to cancel the one-loop quadratic divergences



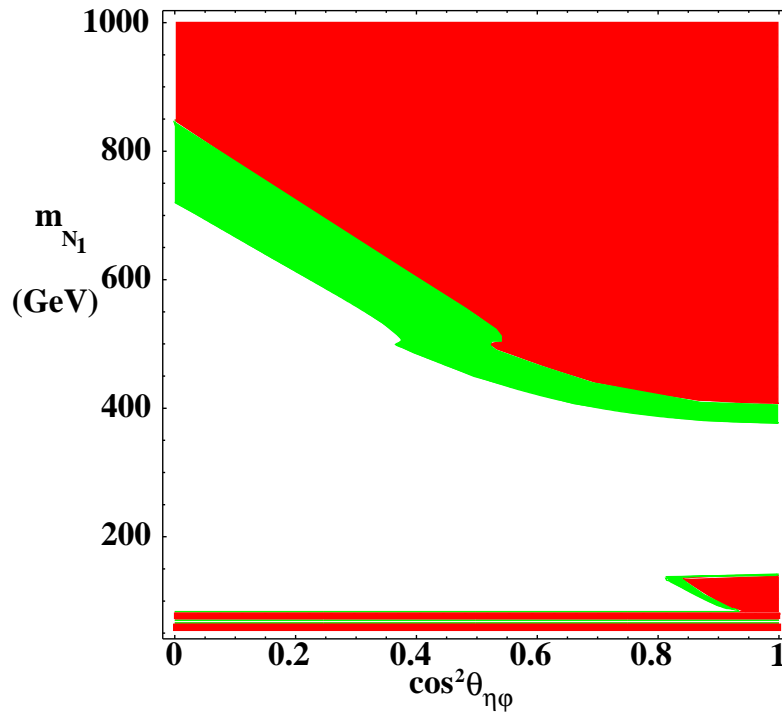
- Conserved T -parity (Cheng, Low hep-ph/0308199)
 - $T = +1$ for SM particles, $T = -1$ for new particles.
 - the lightest T -odd particle is stable.
- No tree-level contributions to precision EW observables

Relic density in LH models

- If the lightest T -odd particle is a scalar, it can be a mixture of an SU(2)-triplet ϕ_3^0 and an SU(2)-singlet η_1^0 :

$$N_1 = \cos \theta_{\eta\phi} \eta_1^0 + \sin \theta_{\eta\phi} \phi_3^0$$

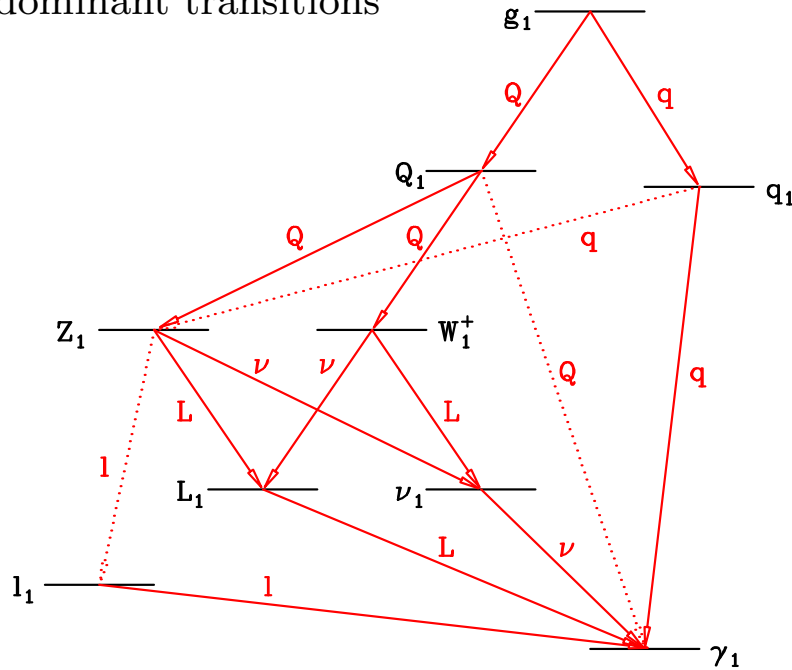
Birkedal, Wacker hep-ph/0306161



- The absence of helicity suppression requires large masses for the WIMP case.
- For $150 \text{ GeV} < m_{N_1} < 350 \text{ GeV}$, annihilation into $t\bar{t}$ and hh is very efficient.

Collider phenomenology of UED

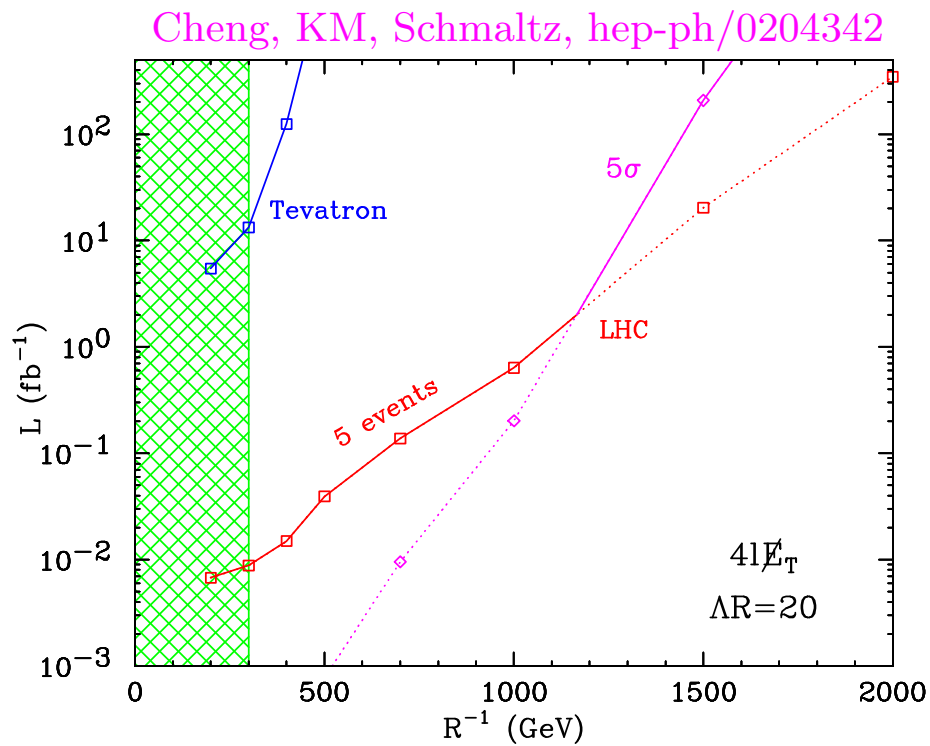
- Allowed dominant transitions



- KK gluon: $B(g_1 \rightarrow Q_1 Q_0) \simeq B(g_1 \rightarrow q_1 q_0) \simeq 50\%$.
- SU(2)-singlet KK quarks: preferentially $q_1 \rightarrow \gamma_1 q_0$
- SU(2)-doublet KK quarks: preferentially to W_1 and Z_1
- KK W^- and Z -bosons: only leptonic decays!
- KK leptons: 100% directly to the LKP.
- At hadron colliders we want: **strong** production, **weak** decays!
- Cleanest signature at LHC: $4\ell + \cancel{E}_T$.

UED discovery reach at the Tevatron and LHC

- Discovery reach in the $pp \rightarrow Q_1 Q_1 \rightarrow 4\ell \cancel{E}_T$ channel.

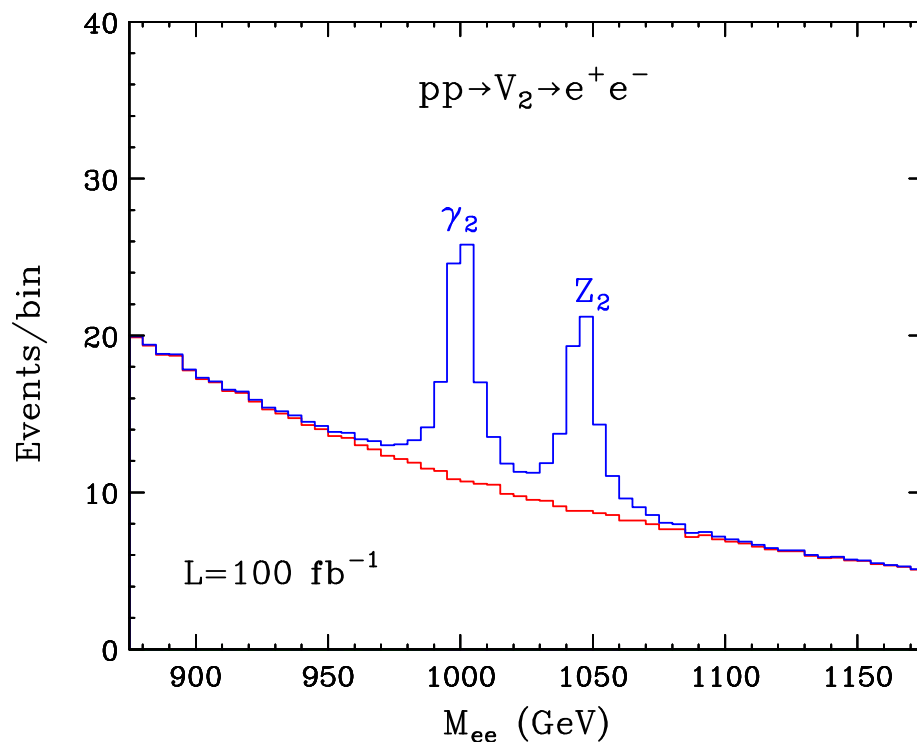


- Other typical signatures include:
 - soft leptons, soft jets, not a lot of \cancel{E}_T
 - a lot of missing mass (unobservable at hadron colliders)
- The “good” dark matter region is covered

Bosonic or fermionic supersymmetry?

- How does one tell SUSY from UED?
- Look for the higher states of the KK tower: e.g. Z_2, γ_2 resonances.

Datta, Kong, KM (preliminary)



- Still... could be SUSY with extra (degenerate) Z' 's.
- Measure the spins of the superpartners (KK-partners)!

SUSY versus UED at a LC

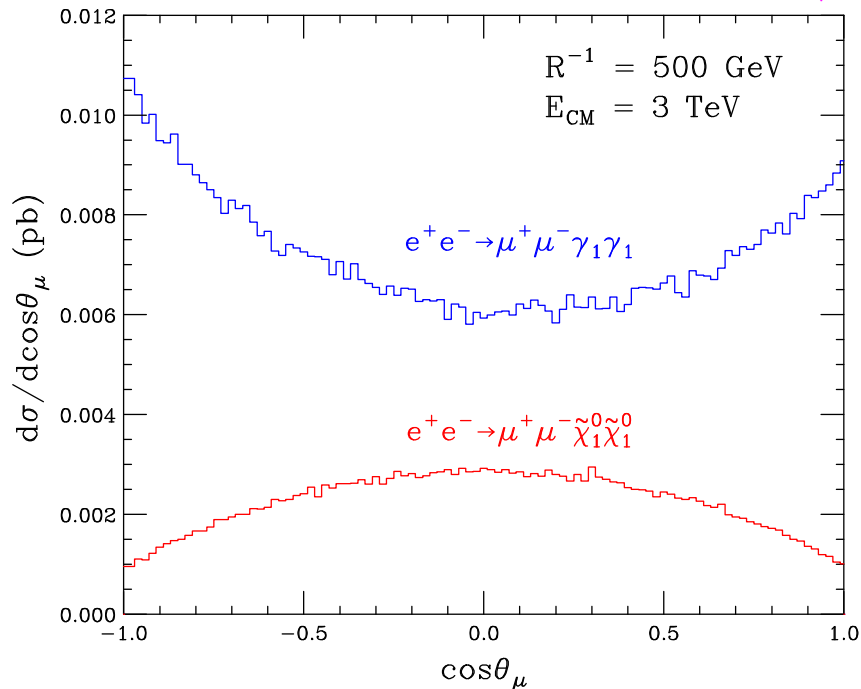
- The spin information is encoded in the angular distributions!

SUSY $e^+e^- \rightarrow \tilde{\mu}^+\tilde{\mu}^- \rightarrow \mu^+\mu^-\tilde{\chi}_1^0\tilde{\chi}_1^0$	UED $e^+e^- \rightarrow \mu_1^+\mu_1^- \rightarrow \mu^+\mu^-\gamma_1\gamma_1$
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$$\frac{d\sigma}{d\cos\theta} \sim 1 - \cos^2\theta$$

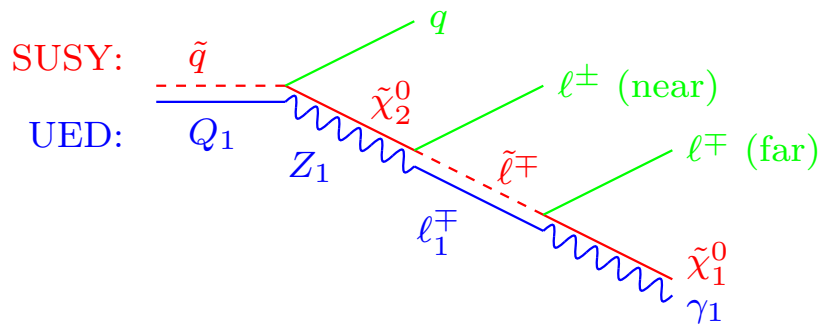
$$\frac{d\sigma}{d\cos\theta} \sim 1 + \cos^2\theta$$

Battaglia,Datta,De Roeck,Kong,KM hep-ph/0502041



- Significant difference in the total cross-section as well!
- The masses can be extracted from the E_μ distribution.
- Threshold scan would confirm the spins.

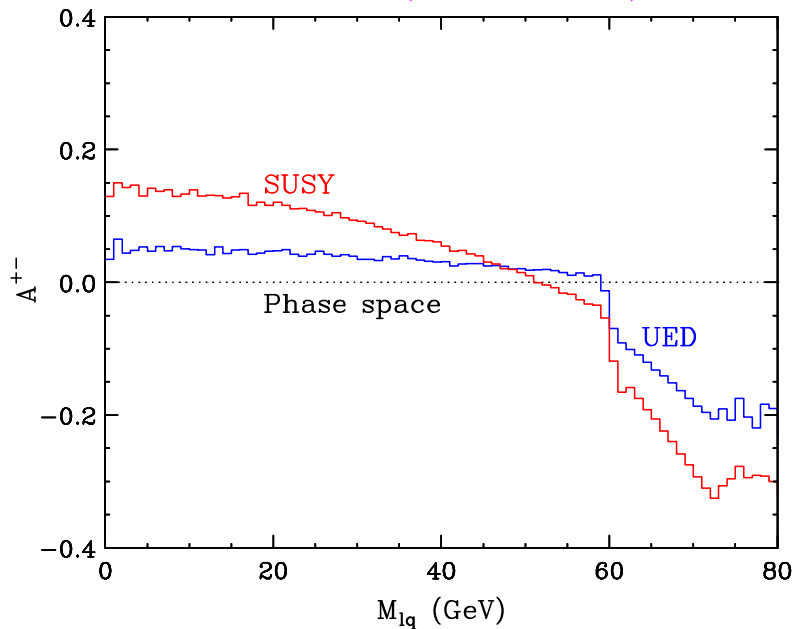
Spin measurements at LHC: SUSY vs UED



- Charge asymmetry in the differential cross-section Barr (2004)

$$A^{+-} = \frac{\sigma(l^+) - \sigma(l^-)}{\sigma(l^+) + \sigma(l^-)}$$

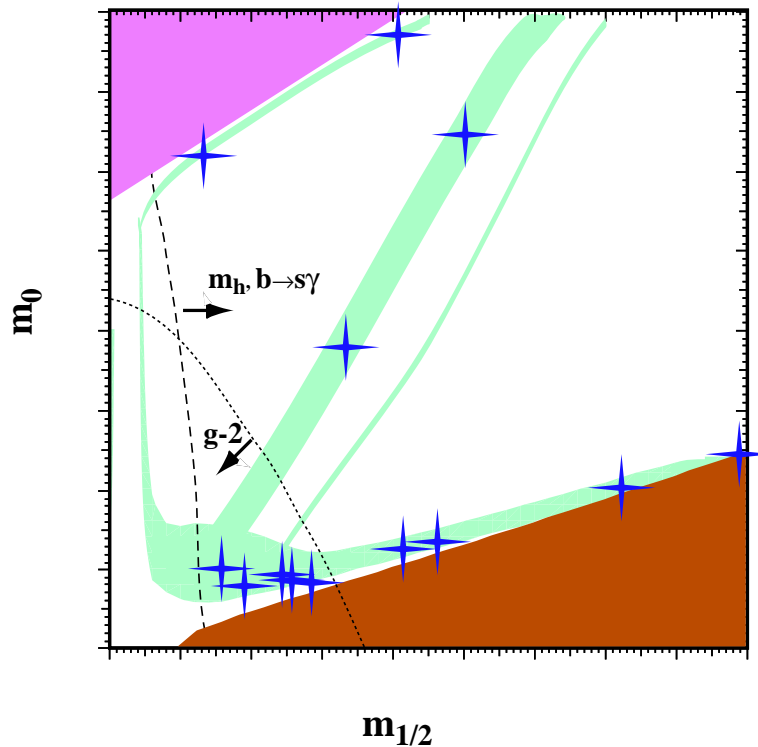
Kong, KM (preliminary)



SUSY vs UED: astroparticle probes

- How do we find the dark matter experimentally?
 - We can make it at high energy colliders
 - Direct detection: underground.
 - Indirect detection:
 - underground/underwater/underice: ν_μ
 - in space: e^+ , \bar{p} , γ ...
- SUSY benchmark points as examples

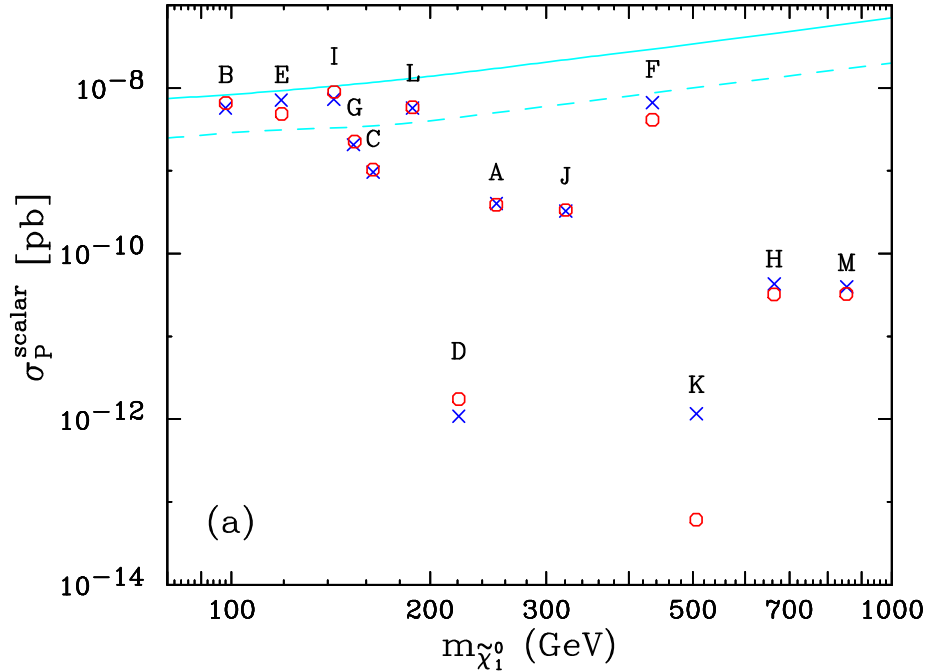
Battaglia et al., hep-ph/0106204



SUSY DM: direct detection

- Spin-independent cross-sections for the 13 benchmark points of Battaglia et al. hep-ph/0106204.

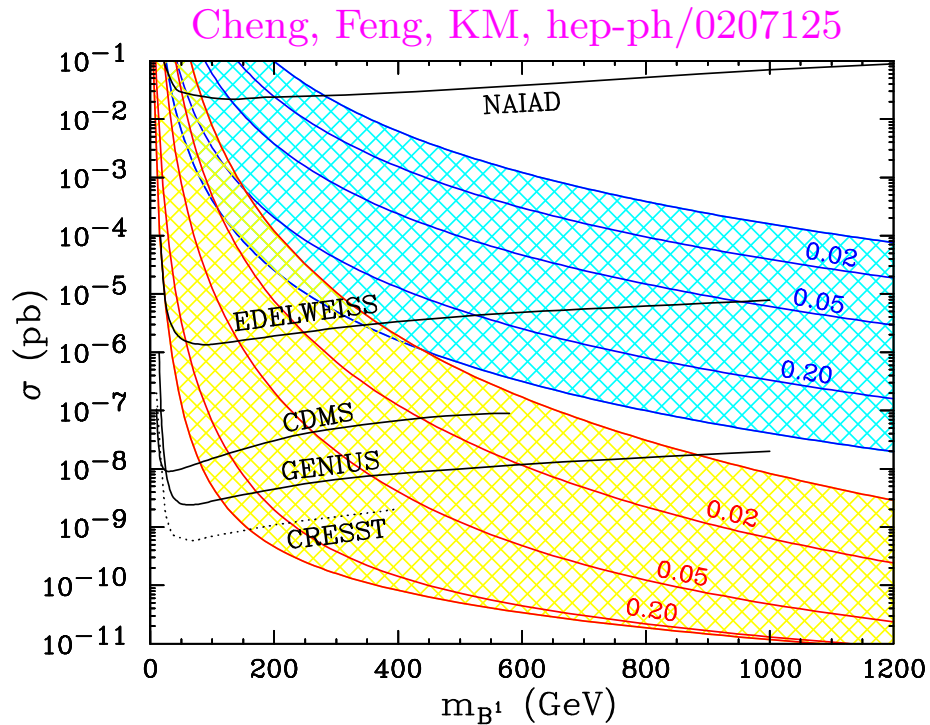
Ellis, Feng, Ferstl, KM, Olive hep-ph/0110225



- No lower limit: cancellations are possible.

KK DM: direct detection

- As usual, spin-dependent and spin-independent cross-sections.



- The signals are enhanced near the s -channel resonance:
 $\sigma \sim (m_{q^1} - m_{B^1})^{-2}$. Unnatural in SUSY, guaranteed here.

Cheng, Feng, KM, hep-ph/0207125

Servant, Tait, hep-ph/0209262

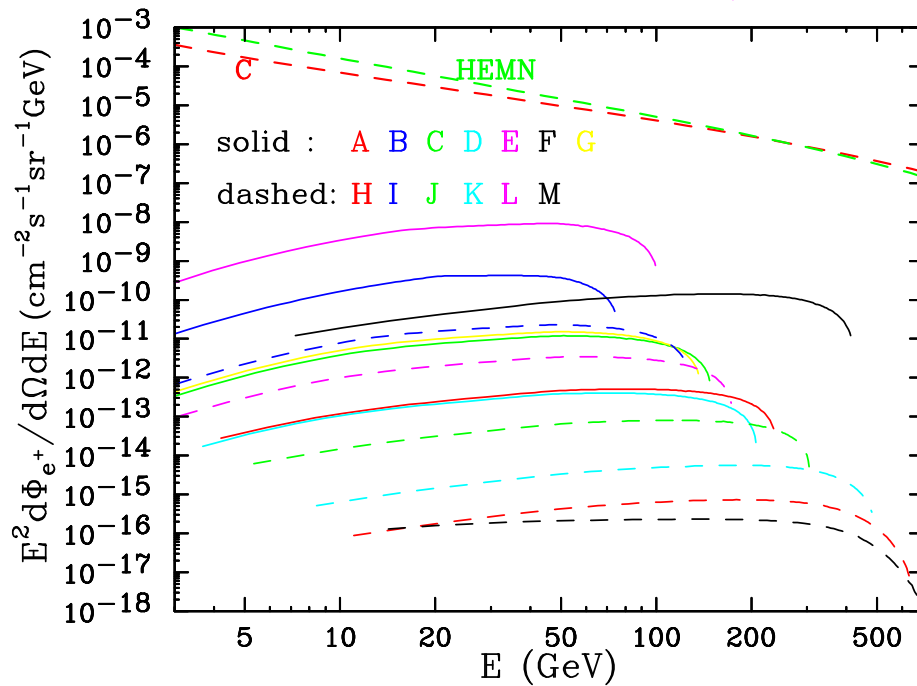
Majumdar, hep-ph/0209277

- Constructive interference: lower bound!

SUSY Dark Matter: Positron signal

- Cosmic ray positrons are an indirect signature of dark matter
- Direct annihilation $\tilde{\chi}_1^0 \tilde{\chi}_1^0 \rightarrow e^+ e^-$ helicity suppressed
- Hard e^+ 's only come from $\tilde{\chi}_1^0 \tilde{\chi}_1^0 \rightarrow WW$ and $\tilde{\chi}_1^0 \tilde{\chi}_1^0 \rightarrow ZZ$.

Ellis, Feng, Ferstl, KM, Olive hep-ph/0110225



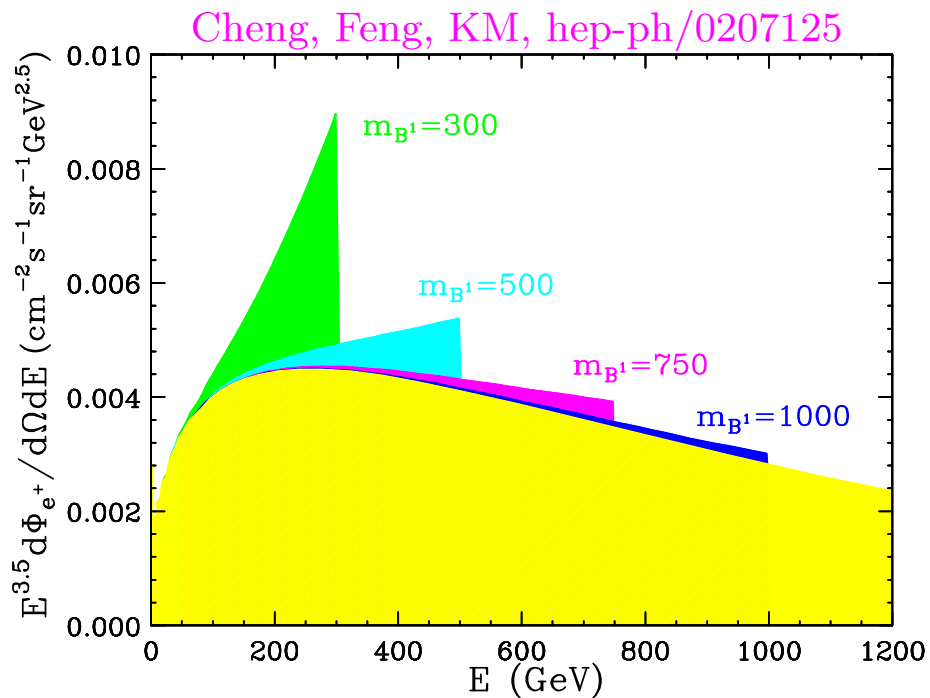
- Background shape and normalization are uncertain.
- The signal is typically a small fraction of the background, **and** the shape is not very characteristic.

KK DM Indirect Detection: Positrons

- Annihilation into fermion pairs is **not** helicity suppressed.

$$B(B^1 B^1 \rightarrow e^+ e^-) = 20\%$$

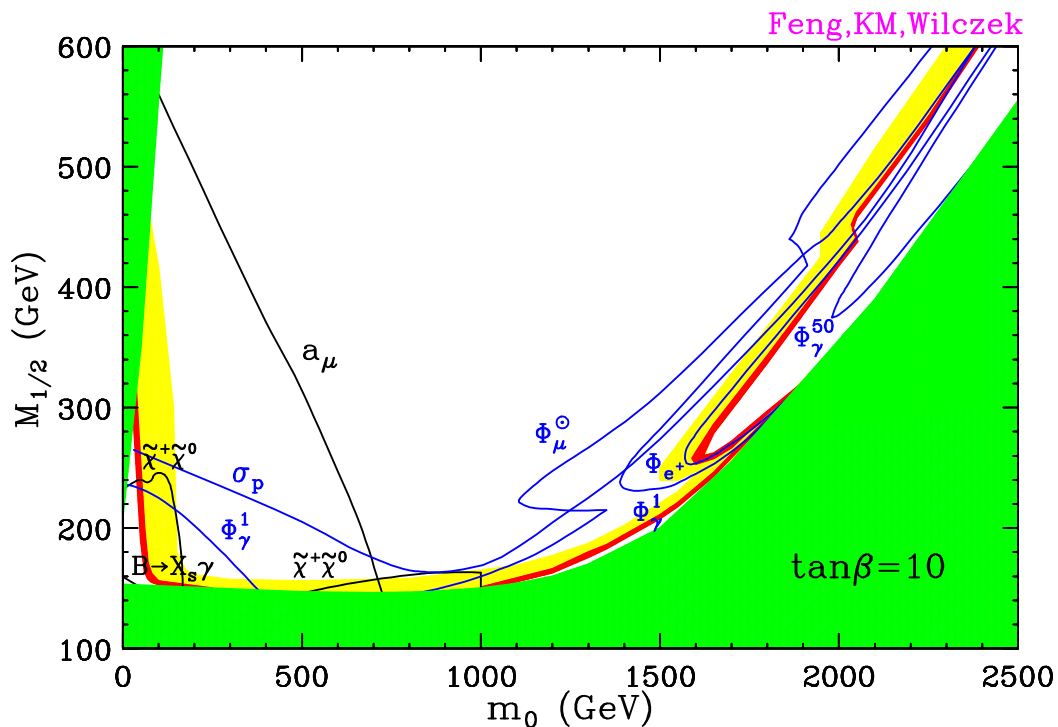
- There is a bump! The positrons are monoenergetic at birth. Some smearing from propagation through the galaxy.



- AMS-II will be able to measure high- p_T positrons!

SUSY WIMP detection

- Combination of “all” pre-LHC experiments
 - Direct SUSY searches: Tevatron
 - Indirect SUSY searches: E827, B-factories
 - Direct WIMP searches: CDMS, CRESST, GENIUS
 - Indirect WIMP searches: Amanda, AMS, GLAST



- Many possible DM signals before 2007-08.
- Particle physics and astrophysics probes are highly complementary.

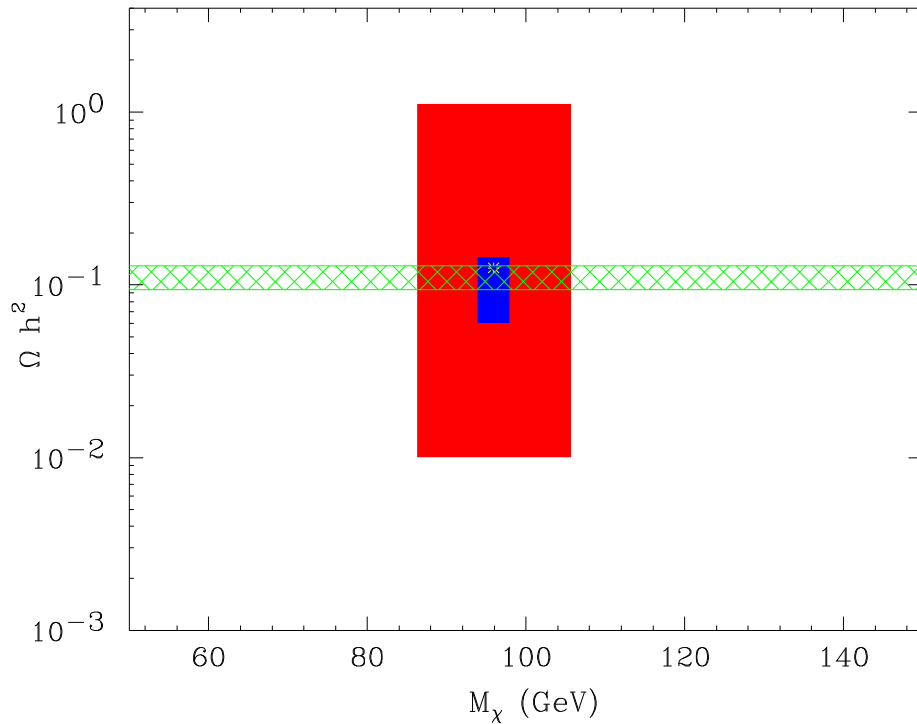
The particle physics/cosmology interface

- Who gets the Nobel prize for the discovery of dark matter?
- The strengths and limitations of different experiments
- Cosmology and astroparticle physics
 - direct probe of dark matter
 - unknown identity, undetermined properties, quantum numbers...
 - direct detection signal roughly bounds the mass and interaction strength
 - indirect detection signal plagued by astrophysical uncertainties; cannot fully discriminate between models
- Collider experiments
 - cannot discover **the** dark matter
 - missing energy signal may be due to quasistable particles
[Feng, Rajaraman, Takayama, hep-ph/0302215](#)
- The full picture will only emerge from the synergy between astrophysics and particle physics probes

LHC vs. ILC vs. WMAP

- LCWG: Connections to Astrophysics and Cosmology (2003)
Eds.: Battaglia, Feng, Graf, Peskin, Trodden
- Typical MSUGRA benchmark:
 - $m_0 = 57, M_{1/2} = 250, A_0 = 0, \tan \beta = 10, \mu > 0.$
 - Similar points discussed in the LHC literature
- LHC: $\tilde{\chi}_1^0, \tilde{\chi}_2^0, \tilde{\chi}_1^\pm, \tilde{q}_L$ to within 10%.

Birkedal, KM “Quantum Universe”



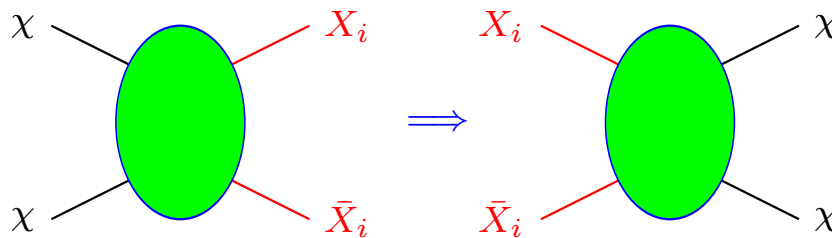
- ILC: $\tilde{\chi}_1^0, \tilde{\chi}_2^0, \tilde{\chi}_1^\pm, \tilde{\ell}_L, \tilde{\ell}_R$ to within 2%. The rest above 250 GeV.

Dark matter production at colliders

- Can we predict dark matter signals at colliders?
- Expect missing energy signatures. Can we quantify?
- The DM relic abundance is governed by the annihilation cross-sections for the reactions

$$\chi + \chi \rightarrow X_i + \bar{X}_i, \quad X_i = \{q, \ell, g, W, Z, \gamma, h\}.$$

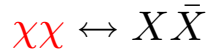
- The inverse reaction takes place at colliders:



- $X_i = \{\mu, \tau, \nu, h, t, b\}$ channels are challenging, the rest accessible at least in principle at LHC and ILC.

Relic density calculation

- At early times, the DM particles χ are in thermal equilibrium with the SM stuff:



- The process of freeze-out of thermal relics is described by the Boltzmann equation

$$\frac{dn_\chi}{dt} = -3Hn_\chi - \langle\sigma_{Av}\rangle (n_\chi^2 - n_{eq}^2)$$

- $-3Hn_\chi$ accounts for dilution due to the Hubble expansion
- $-\langle\sigma_{Av}\rangle n_\chi^2$ describes depletion due to $\chi\chi \rightarrow X\bar{X}$
- $+\langle\sigma_{Av}\rangle n_{eq}^2$ describes resupply due to $X\bar{X} \rightarrow \chi\chi$
- σ_A is the total DM annihilation cross-section:

$$\sigma_{Av} \equiv \sum_X \sigma(\chi\chi \rightarrow X\bar{X})v \equiv a + bv^2 + \mathcal{O}(v^4)$$

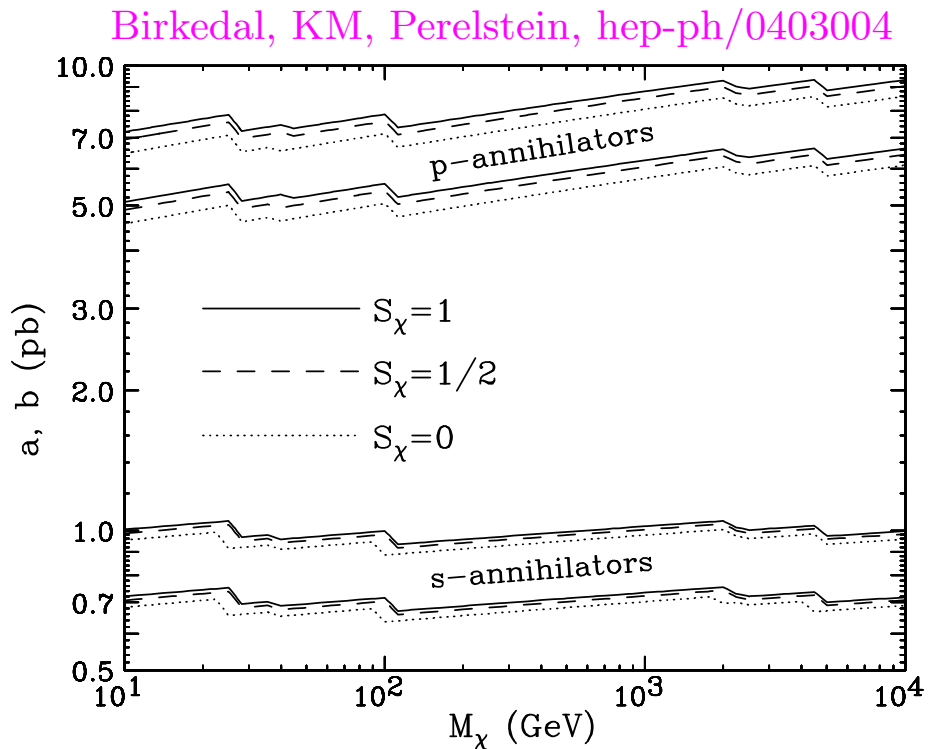
- An approximate analytical solution

$$\Omega h^2 = 0.08 \frac{1 \text{ pb}}{a + (3b - 0.75a)x_F}$$

where $x_F = T_F/M_\chi \sim 0.04$, with T_F the freeze-out temperature.

What does WMAP tell us?

- Two classes of DM candidates:
 - $a \sim b$: “s-annihilators”
 - $a < bx_F \ll b$: “p-annihilators”
- The present amount of dark matter $\Omega_{DM}h^2 = 0.112 \pm 0.009$ tells us exactly the WIMP annihilation cross-section:

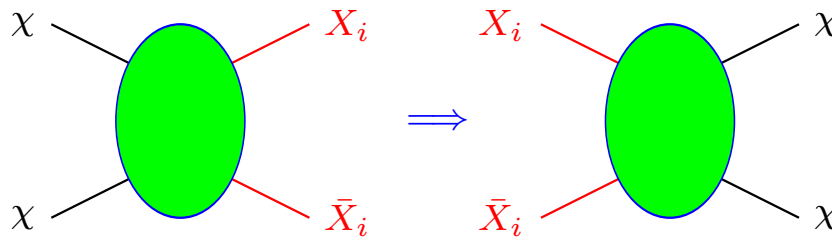


- The dependence on M_χ is only logarithmic and is offset by the change in effective number of dof in the SM at different T_F .

The WIMP production cross-section

- WIMP annihilation and WIMP production at colliders are related by detailed balancing:

$$\frac{\sigma(\chi + \chi \rightarrow X_i + \bar{X}_i)}{\sigma(X_i + \bar{X}_i \rightarrow \chi + \chi)} = 2 \frac{v_X^2 (2S_X + 1)^2}{v_\chi^2 (2S_\chi + 1)^2}$$



- Annihilation fractions:

$$\kappa_i = \frac{\sigma_i^{(J_0)}}{\sigma_{\text{tot}}}, \quad \sum_i \kappa_i = 1.$$

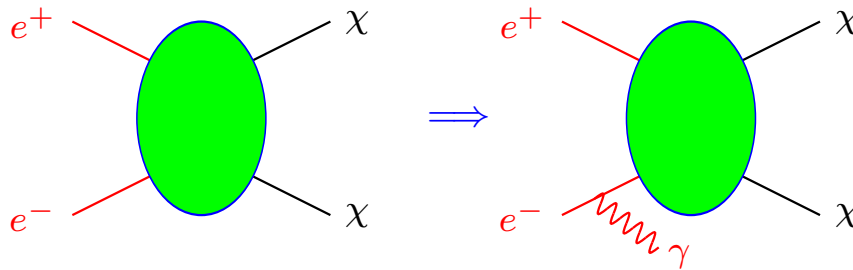
- Model-independent prediction of the WIMP production rate

$$\sigma(X_i \bar{X}_i \rightarrow 2\chi) = 2^{2(J_0-1)} \kappa_i \sigma_{\text{tot}} \frac{(2S_X + 1)^2}{(2S_\chi + 1)^2} \left(1 - \frac{4M_\chi^2}{s}\right)^{1/2+J_0}$$

- Known parameters: $\{\sigma_{an}, S_X, s\}$
- Unknown parameters: $\{\kappa_i, M_\chi, S_\chi, J_0\}$
- Applicable only close to 2χ threshold ($v_\chi \ll 1$).
- But... no trigerrable signature!

Soft photon factorization

- What to do?
 - Give up model-independence, consider production of heavier particles (superpartners, KK-modes etc.)
 - Tag the known initial state with a soft photon/gluon



- Soft/collinear photon factorization:

$$\frac{d\sigma(e^+e^- \rightarrow 2\chi + \gamma)}{dx d\cos\theta} = \frac{\alpha}{\pi} \frac{1 + (1-x)^2}{x} \frac{1}{\sin^2\theta} \hat{\sigma}(e^+e^- \rightarrow 2\chi)$$

where $x \equiv 2E_\gamma/\sqrt{s}$, $\hat{\sigma}$ is evaluated at $\hat{s} = (1-x)s$.

- Applicable for $E_\gamma \ll \sqrt{s} - M_\chi$.
- In specific models, we expect $\kappa_e \sim 20\% \implies \text{LC!}$
- Analogously, WIMP production at hadron colliders:

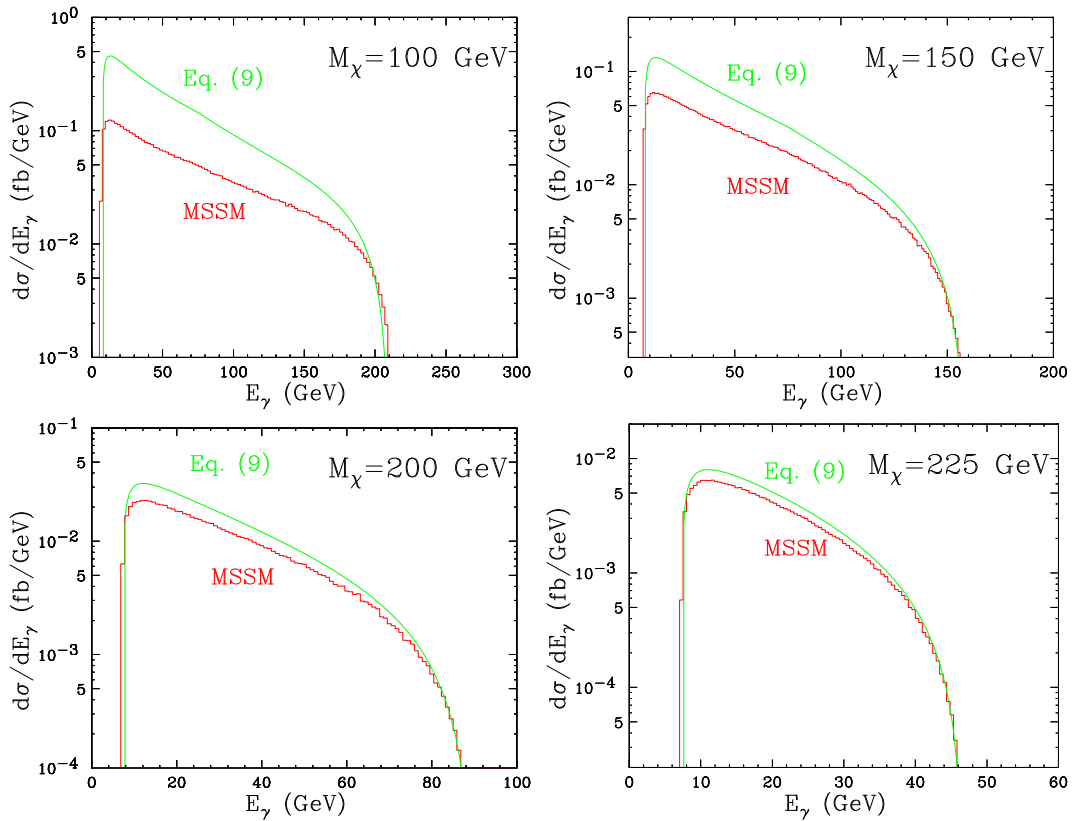
$$\sigma(q\bar{q} \rightarrow 2\chi + g) \sim \alpha_s \kappa_q \sigma_{an}, \quad \sigma(gg \rightarrow 2\chi + g) \sim \alpha_s \kappa_g \sigma_{an}$$

Very challenging experimentally...

How well did we do?

- Compare the analytic formula to the exact result in explicit models

Birkedal, KM, Perelstein, hep-ph/0403004



- At low v_χ , soft factorization breaks down.
- At high v_χ , higher-order terms in the velocity expansion become relevant.

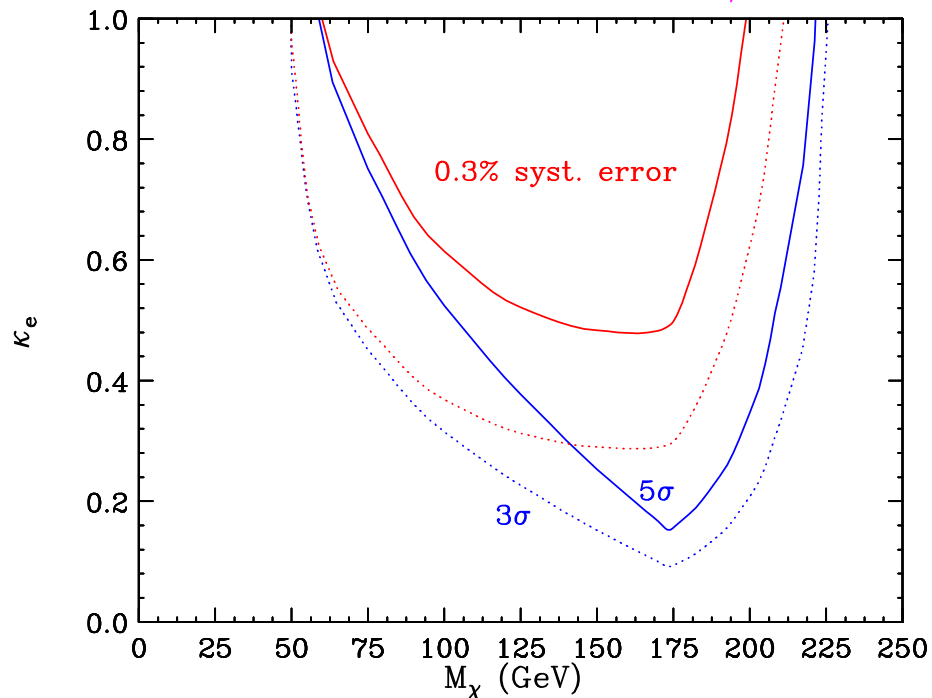
WIMP signal at a 500 GeV LC

- Discovery reach of LC500. Cuts:
 - $\sin \theta_\gamma > 0.1$, $p_{T,\gamma} > 7.5$ GeV (suppress Bhabha).
 - χ 's must be non-relativistic and E_γ below threshold:

$$\frac{\sqrt{s}}{2} \left(1 - \frac{8M_\chi^2}{s} \right) \leq E_\gamma \leq \frac{\sqrt{s}}{2} \left(1 - \frac{4M_\chi^2}{s} \right).$$

- No polarization. $L = 500 \text{ fb}^{-1}$.

Birkedal, KM, Perelstein, hep-ph/0403004

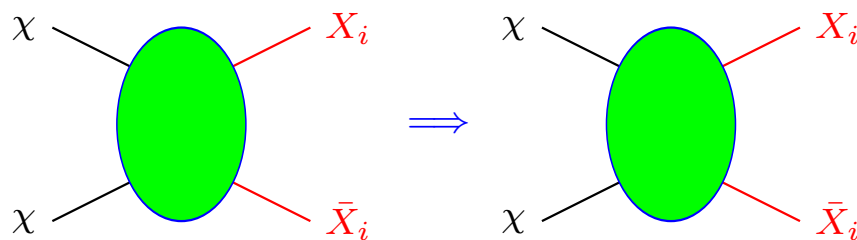


- In SUSY $\kappa_e \sim 25\%$. Polarization would help.

Indirect detection of dark matter: a model-independent approach

- The DM relic abundance is governed by the annihilation cross-sections for the reactions

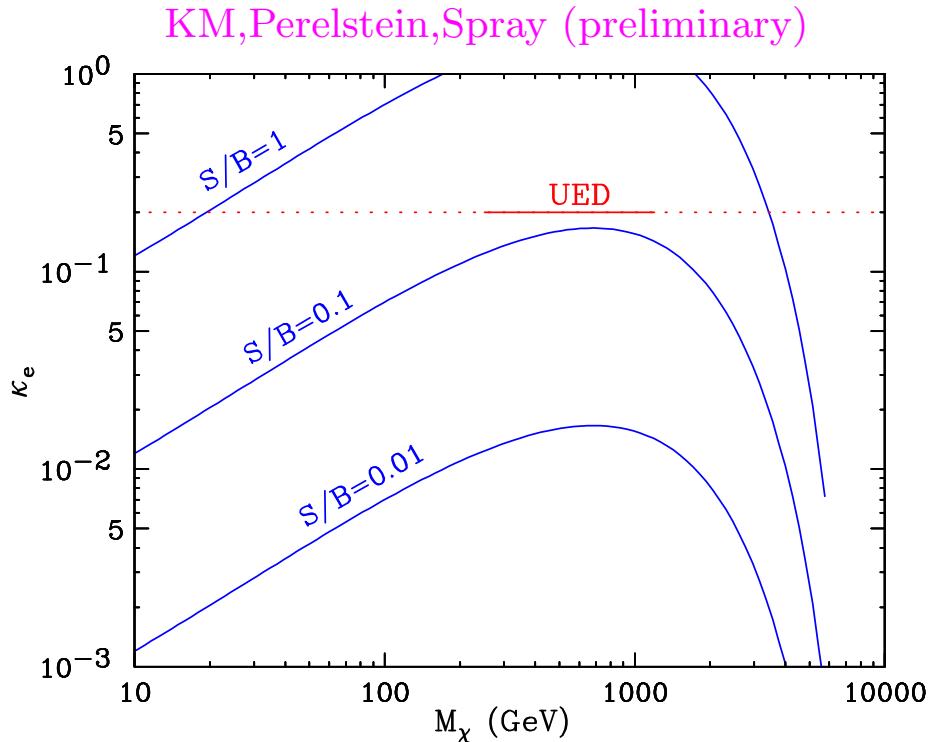
$$\chi + \chi \rightarrow X_i + \bar{X}_i, \quad X_i = \{q, \ell, g, W, Z, \gamma, h\}.$$



- The same annihilation reaction is happening right now:
 - neutrinos from the Sun/Earth
 - antimatter cosmic rays
 - high energy photons from the galactic center
- Model-independent indirect DM signals (KM, Perelstein, Spray)

Indirect WIMP signals: positrons

- A model-independent prediction for the positron peak rate due to DM annihilations $\chi\chi \rightarrow e^+e^-$ in the halo:



- In UED $\kappa_e \sim 25\%$. In SUSY much smaller.
- Similar predictions can be made for secondary positrons in
 - $\chi\chi \rightarrow \tau^+\tau^- \rightarrow e^+e^- \dots$
 - $\chi\chi \rightarrow W^+W^- \rightarrow e^+e^- \dots$
 - $\chi\chi \rightarrow ZZ \rightarrow e^+e^- \dots$

The Message

- Recent new ideas in particle physics lead to novel alternatives for dark matter candidates. SUSY DM? Not so fast...
- Extra dimensions **also** yield natural dark matter candidates, with **calculable** rates for detection.
- Little Higgs theories, with certain assumptions, also have a dark matter candidate.
- The usual question: how do we discover these models?
- How do we tell the difference?
- How do we uncover the identity of the dark matter?
- How will we know we have found the dark matter particle in a collider?
- Elucidating the nature of the dark matter will require both dark matter and collider experiments.
- Dark matter detection experiments should be prepared for surprises, avoid theory bias.
- WMAP implies model-independent, guaranteed and experimentally challenging rates for missing energy signals of DM at colliders.