



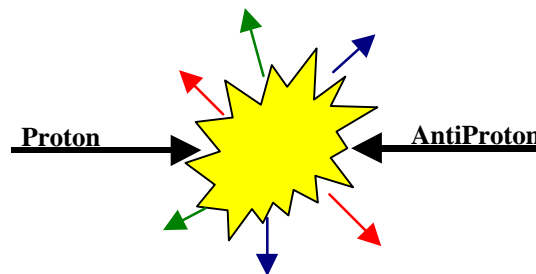
## Min-Bias Jets: The Evolution of Jets from 0.5 to 100 GeV

Rick Field & Dave Stuart

plus

Bologna Group (N. Moggi, F. Rimondi, S. Zucchelli)

*Talk by Rick Field Presented at the QCD Meeting March 25, 1999*



- Study the **CDF “Min-Bias” Data** with the goal of finding a **Monte-Carlo Generator** that will fit the data. Would like to describe (**approximately**) all the features of **the entire inelastic (“hard core”) cross section (low PT and high PT)!**
- Look at the data (**plot many observables**) and compare to **Herwig** and **Isajet** and **Pythia**.
- For now consider only charged particles in the region,  **$PT > 0.5 \text{ GeV}$   $|\eta| < 1$** , where efficiency is good.
- In this talk I will concentrate on Jets (“**Jet**” = **circular region**).
- **Plot distributions:**  $PT(\text{jet}\#1)$  (**connect with Jet20 data**).
- **Look at  $PT(\text{jet}\#1)$  dependence (plot averages versus  $PT(\text{jet}\#1)$ ):**  $\langle PT_{\text{max}} \rangle$ ,  $\langle N_{\text{jet}} \rangle$ ,  $\langle N_{\text{chgJet}\#1} \rangle$ ,  $\langle PT_{\text{jet}\#2} \rangle$ ,  $\langle PT_{\text{jet}\#3} \rangle$ ,  $\langle \text{JetSize} \rangle$ , etc..
- **Look at Jet Development as function of  $PT(\text{jet}\#1)$ :**  $N_{\text{chg}}(\text{Jet}\#1)$ , Jet Size, N-flow and PT-flow relative to Jet#1 direction, “Fragmentation Functions”.
- **Many** more transparencies than I can show in this talk! All **30** transparencies are on the **WEB**.

[http://www.phys.ufl.edu/~rfield/cdf/QCD\\_Talk2.html](http://www.phys.ufl.edu/~rfield/cdf/QCD_Talk2.html)

## Min-Bias Data – Inelastic Cross-Section

Inelastic “Hard Core” Cross Section:

$$\sigma_{\text{tot}} = \sigma_{\text{elastic}} + \sigma_{\text{inelastic}}$$

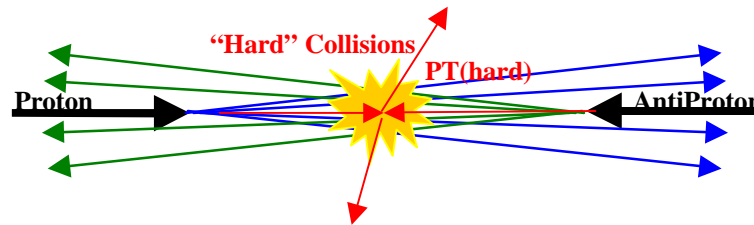
$$\sigma_{\text{inelastic}} = \sigma_{\text{HC}} + \sigma_{\text{SD}} + \sigma_{\text{DD}}$$

Hard Core
Single Diffraction
Double Diffraction

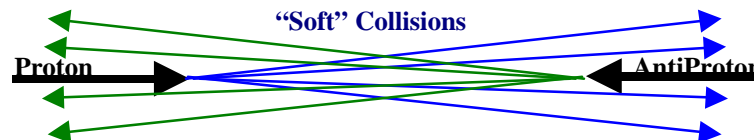
Inelastic “Hard Core” Cross Section at 1.8 TeV:

$$\sigma_{\text{HC}} = \sigma_{\text{inelastic}} - \sigma_{\text{SD}} - \sigma_{\text{DD}} = 60 \text{ mb} - 9 \text{ mb} - 1 \text{ mb} = 50 \text{ mb}$$

Want to describe (approximately) the entire “hard core” part of the inelastic cross section,  $\sigma_{\text{HC}}$ , which has a QCD “hard scattering” component that becomes infinite as  $P_T(\text{hard})$  becomes small,



and may also have a “soft collision” component (not calculable from perturbation theory).



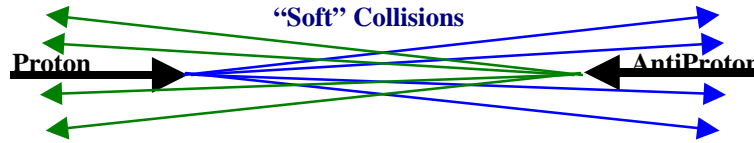
Two possible approaches:

- **Two Component Model:**  
 $\sigma(\text{inelastic HC}) =$   
 $\sigma(\text{“hard perturbative”, } P_T > P_{T\text{min}}) + \sigma(\text{“soft”, everything else})$
- **One Component Model:**  
 $\sigma(\text{inelastic HC}) =$   
 $\sigma(\text{“hard perturbative”, all } P_T \text{ but remove the divergences})$

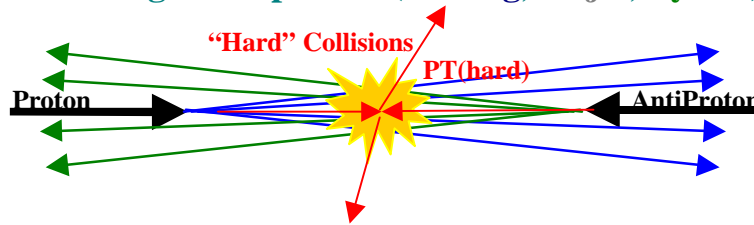
# QCD MC – Herwig, Isajet, Pythia

## “Soft Collision” Component (Herwig, Isajet):

Herwig and Isajet provide a “Soft Collision” generator for simulating Min-Bias events. They produce roughly 4 charged particles per unit  $\eta$  and have no correlations (except resonances).



## QCD “Hard Scattering” Component (Herwig, Isajet, Pythia):

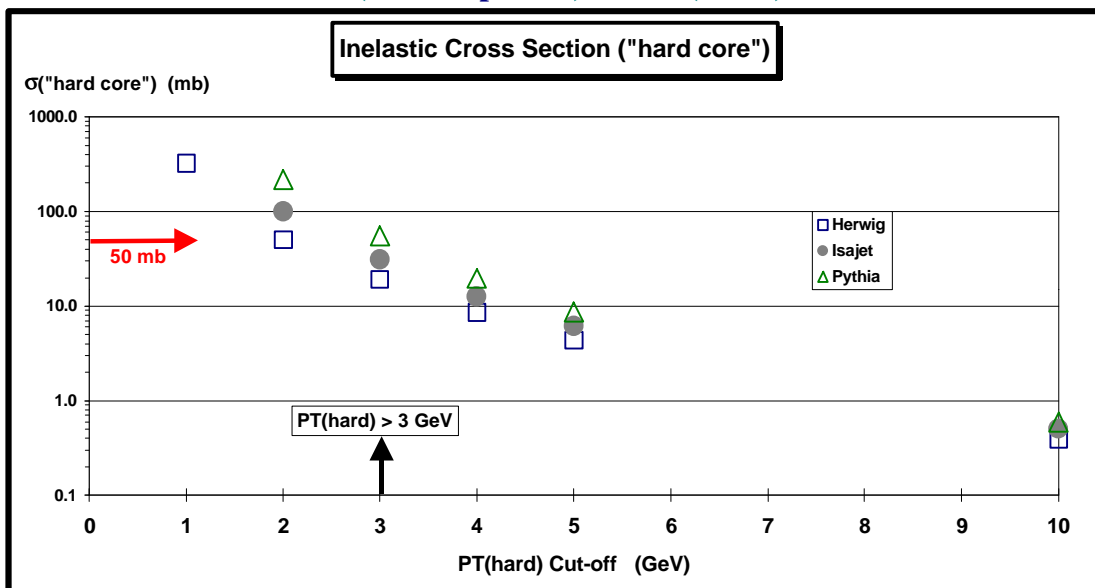


**Herwig QCDJET3:** Herwig QCD 2-2 parton-parton “hard” scattering with  $P_T(\text{hard}) > 3 \text{ GeV}$  ( $\sigma = 19.3 \text{ mb}$ ).

**Isajet QCDJET3:** Isajet QCD 2-2 parton-parton “hard” scattering with  $P_T(\text{hard}) > 3 \text{ GeV}$  ( $\sigma = 31.1 \text{ mb}$ ).

**Pythia QCDJET3:** Pythia QCD 2-2 parton-parton “hard” scattering with  $P_T(\text{hard}) > 3 \text{ GeV}$  ( $\sigma = 55.1 \text{ mb}$ ).

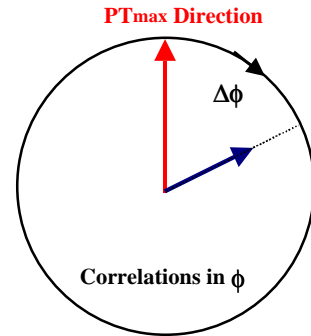
## Inelastic Cross-Section (HC component) vs $P_T(\text{hard})$ Cut-off:



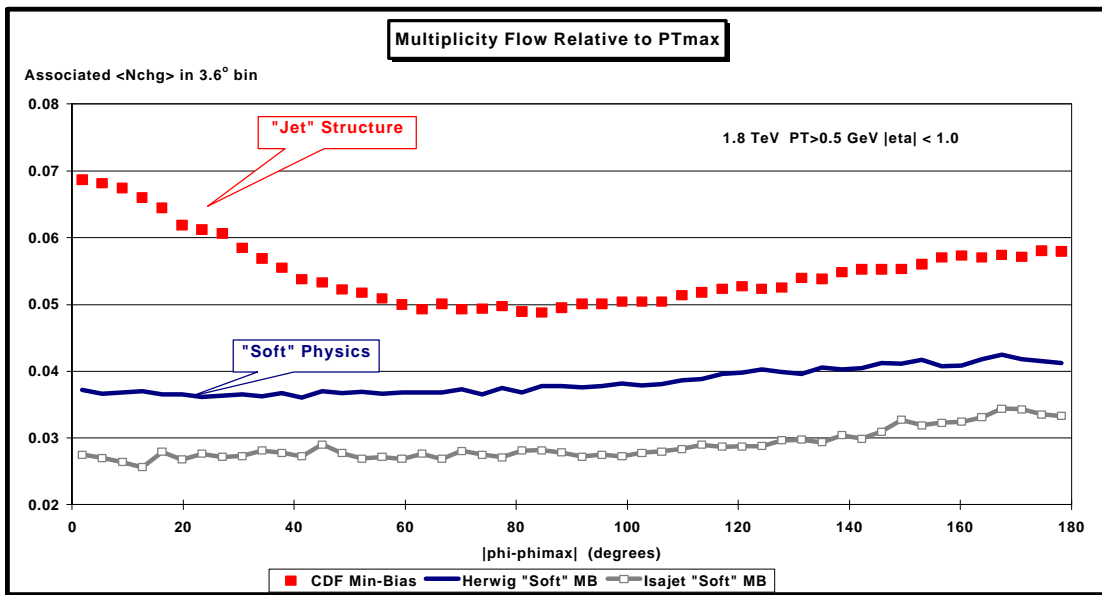
QCD perturbative cross section becomes infinite as  $P_T(\text{hard})$  cut-off goes to zero.

# MB Jets – N-Flow & PT-Flow Relative to PTmax

Define PTmax to be the highest PT charged particle in the event ( $PT > 0.5 \text{ GeV}$ ,  $|\eta| < 1$ ) and look at correlations in azimuthal angle  $\phi$ .

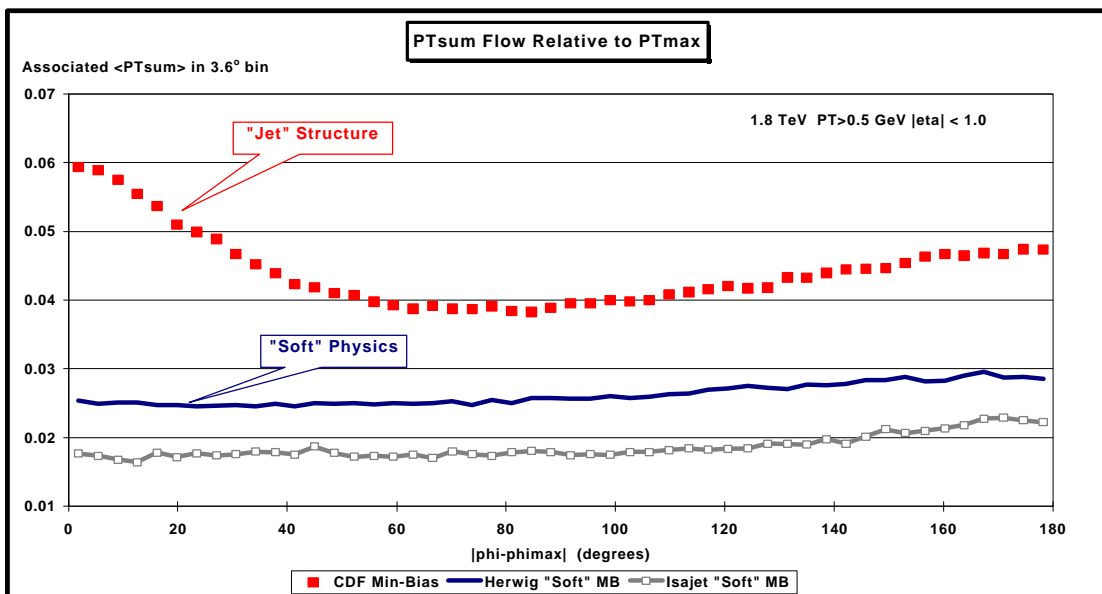


$\langle N_{ch} \rangle$  Produced in Association with PTmax versus  $|\phi - \phi_{max}|$ :



Does not include PTmax ( $N_{ch} \geq 2$ )

$\langle PT_{sum} \rangle$  Produced in Association with PTmax versus  $|\phi - \phi_{max}|$ :



Does not include PTmax ( $N_{ch} \geq 2$ )

## MB Jets – Jet Algorithm

Examine “Circular Regions” in  $\eta$ - $\phi$  space with “distance” defined by

$$d = \sqrt{\Delta h^2 + \Delta f^2}$$

Use a Simple Jet Algorithm (“Jet” = circular region):

- Order Charged Particles ( $P_T > 0.5$  GeV  $|\eta| < 1$ )
- Start with highest  $P_T$  particle and include in the “Jet” all particles ( $P_T > 0.5$  GeV  $|\eta| < 1$ ) within radius  $R = 0.7$
- Go to the next highest  $P_T$  particle (not already included in a previous jet) and include in the “Jet” all particles ( $P_T > 0.5$  GeV  $|\eta| < 1$ ) within radius  $R = 0.7$  (not already included in a previous jet)
- Continue until all particles are in a jet

Example (6 particles, 5 jets):

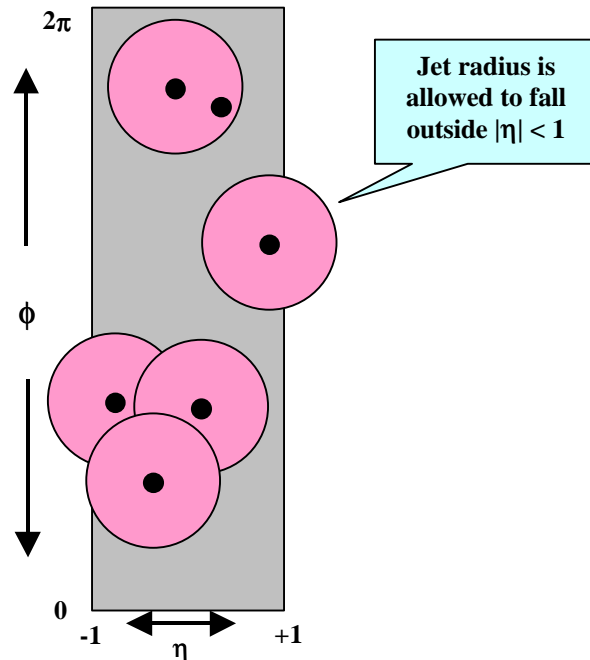
The maximum number of jets is

$$\sim 2(2)(2\pi)/(\pi(0.7)^2) \sim 16$$

Jets have a momentum given by

$$\vec{P}_{jet} = \sum_{i=1}^{N_j} \vec{p}_i,$$

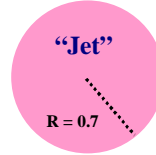
where  $N_j = N_{chgJet}$  is the number of charged particles in the jet and



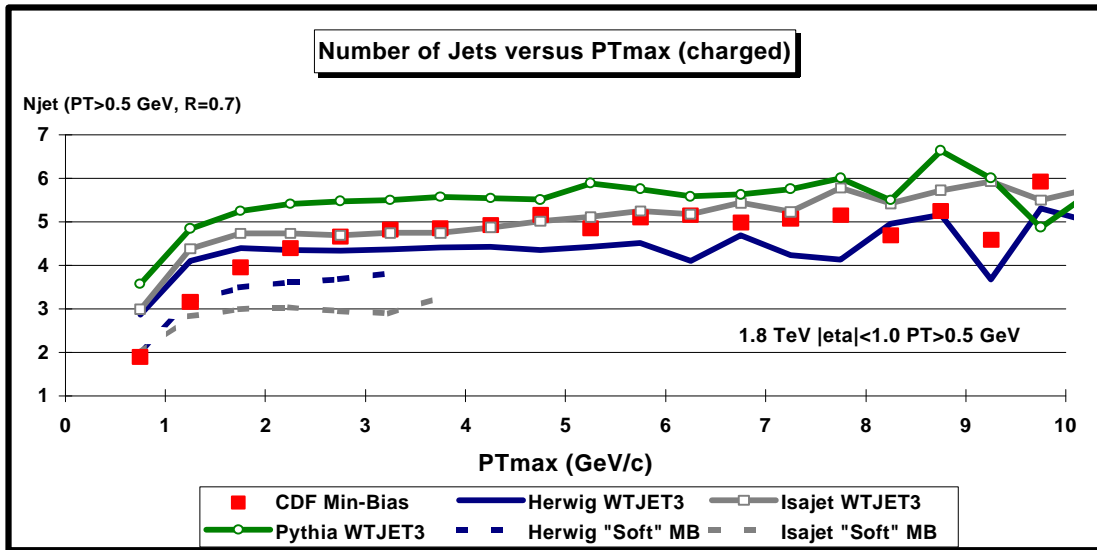
$$P_T(jet) = \sqrt{P_x(jet)^2 + P_y(jet)^2}$$

# Min-Bias Data – Dependence on PTmax

“Jet” = Circular Region →

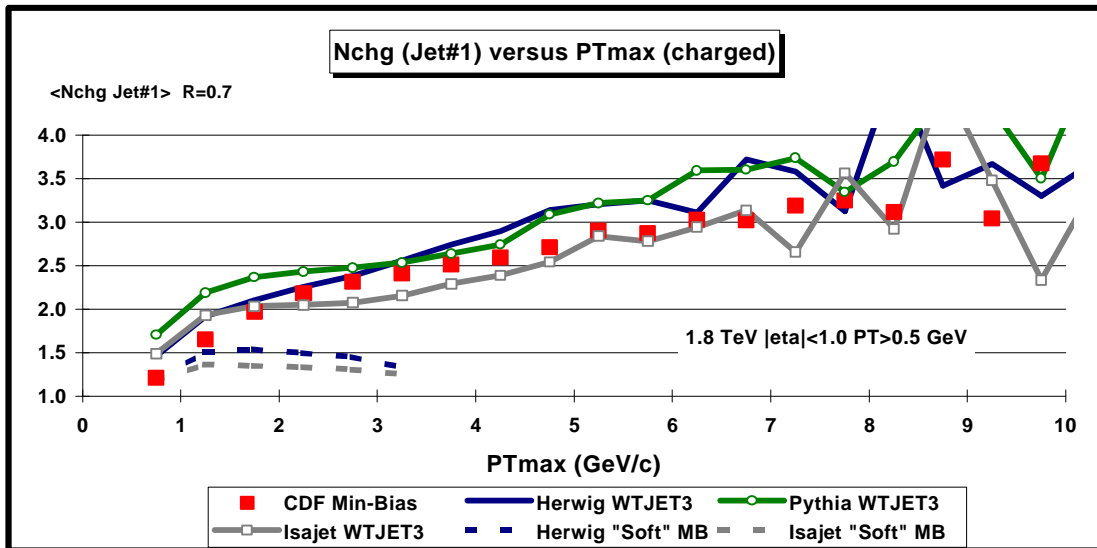


$\langle N_{jet} \rangle$  ( $PT_{jet} > 0.5$  GeV,  $R = 0.7$ ) versus  $PT_{max}$ :



CDF Data plus QCD Monte-Carlo Predictions.

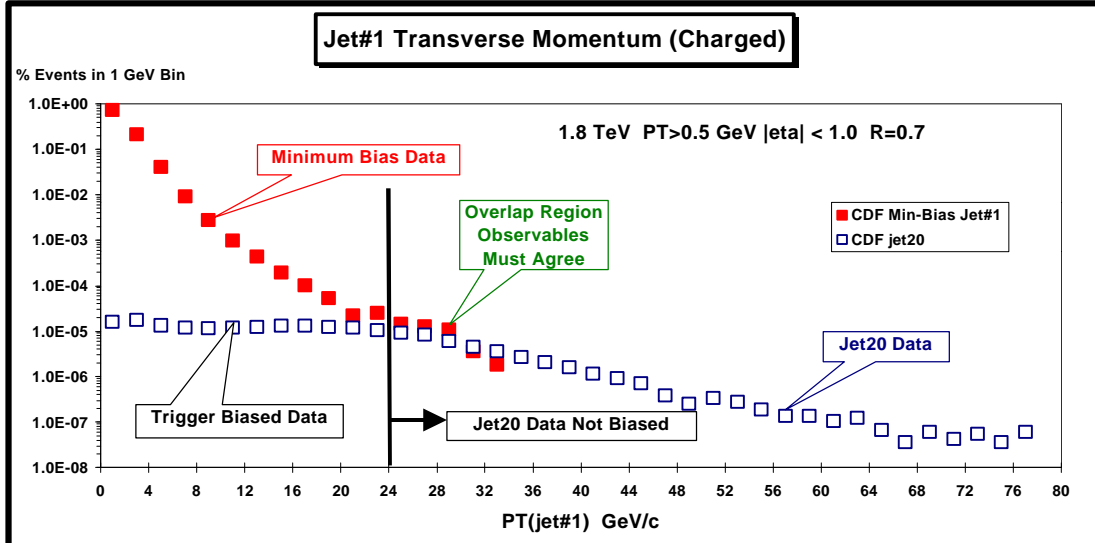
$\langle N_{chg}(\text{Jet}\#1) \rangle$  ( $PT_{jet} > 0.5$  GeV,  $R = 0.7$ ) versus  $PT_{max}$ :



CDF Data plus QCD Monte-Carlo Predictions.

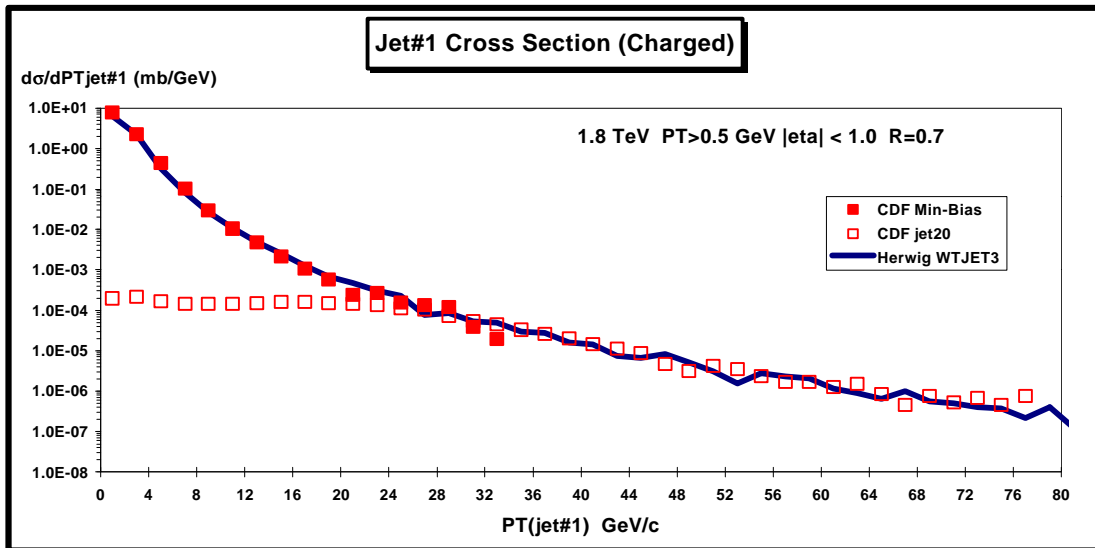
# MB Jets – Jet#1 Cross-Section

## Jet#1 Transverse Momentum Distribution (R = 0.7):



CDF Min-Bias Data normalized to 1. Use this plot to determine the relative normalization between the Min-Bias data and the Jet20 data.

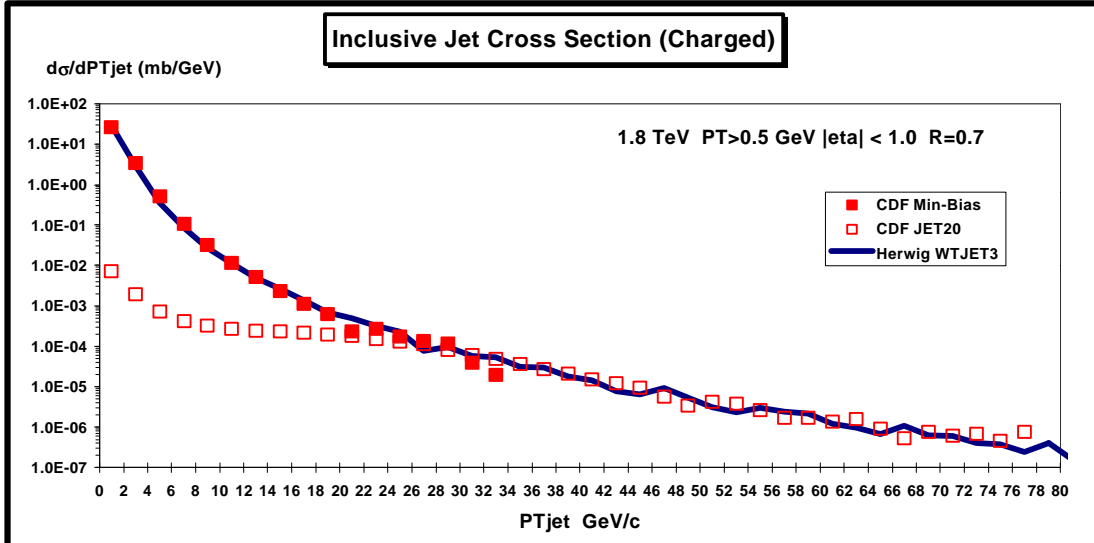
## Jet#1 Differential Cross-Section (mb/GeV, R = 0.7):



Normalize CDF data to the Herwig QCDJET3 Jet#1 differential cross section which corresponds to  $\sigma_{inel} = 19.2$  mb.

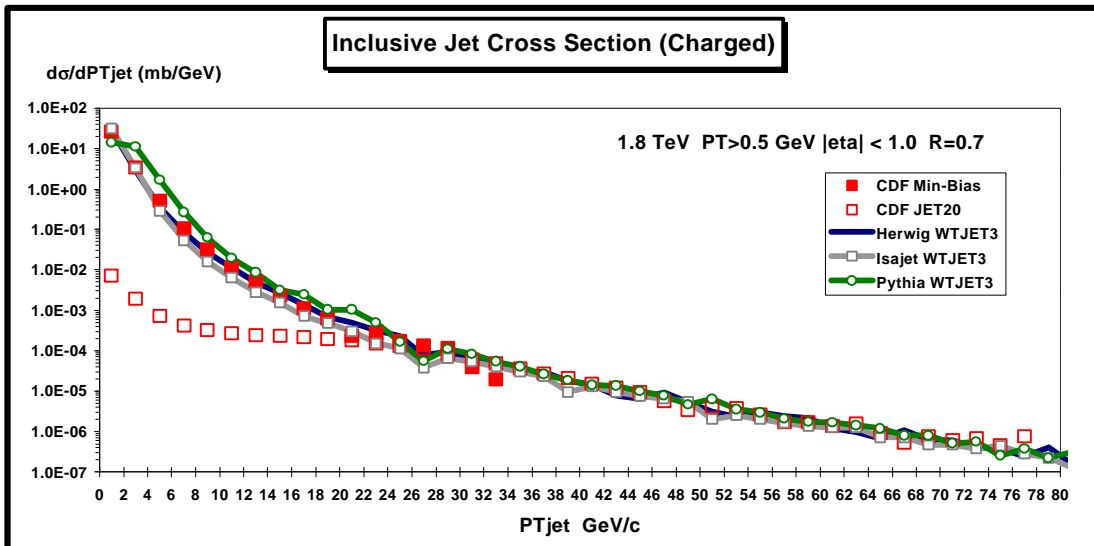
# MB Jets – Inclusive Jet Cross-Section

**Inclusive Charged Jet Cross-Section (mb/GeV, R = 0.7):**



**CDF Min-Bias Data and Jet 20 Data normalization fixed from Jet#1 differential cross-section.**

**Inclusive Charged Jet Cross-Section (mb/GeV, R = 0.7):**

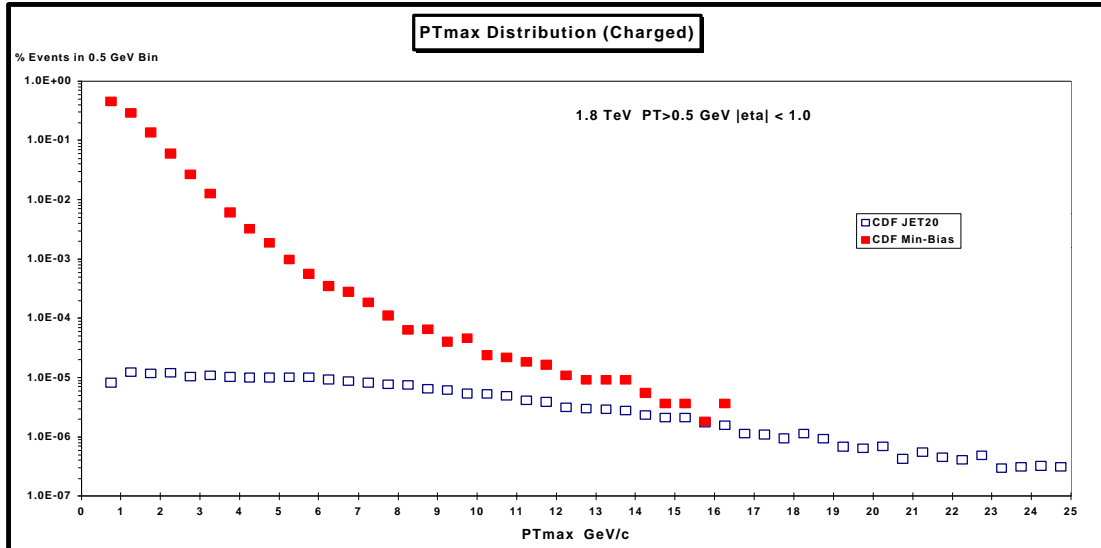


**Herwig, Isajet, Pythia.**



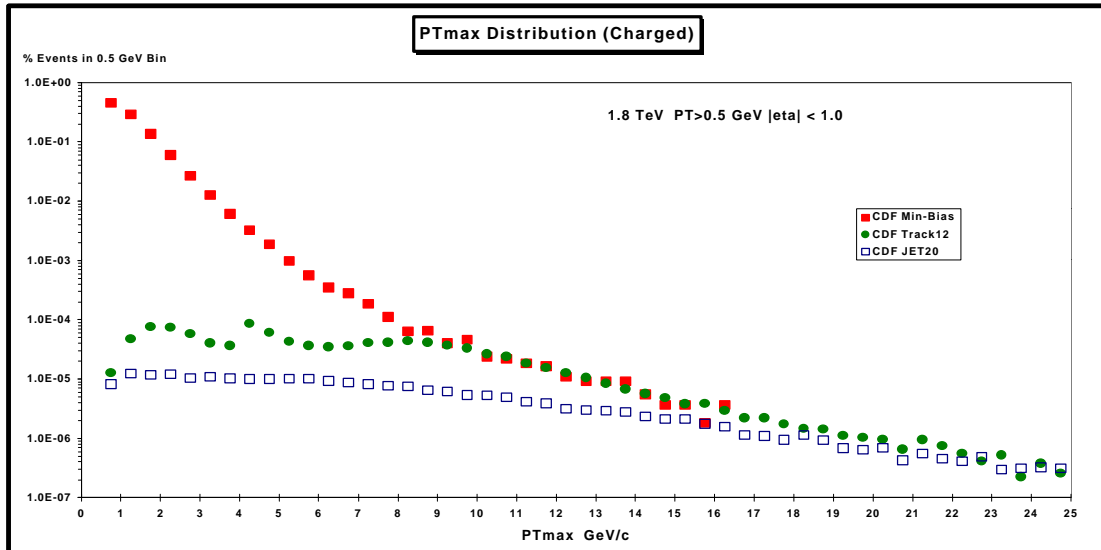
# Min-Bias Data – PTmax Cross Section

## Distribution of PTmax (highest PT charged particle):



CDF Min-Bias Data normalized to 1. Relative normalization between the **Min-Bias** data and the **Jet20** data comes from the **Jet#1** momentum distribution plot.

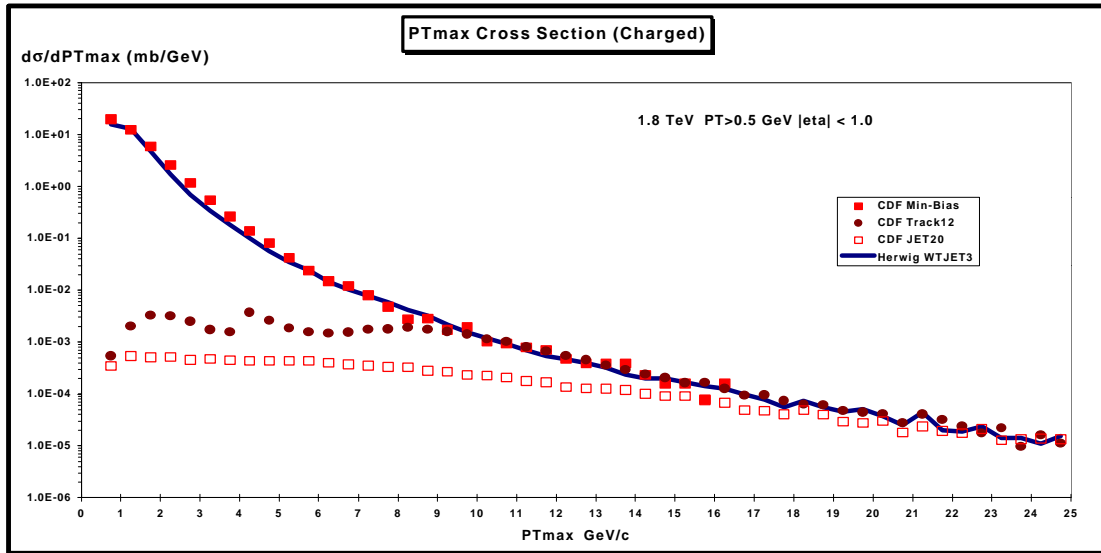
## Distribution of PTmax (highest PT charged particle):



CDF Min-Bias Data normalized to 1. The relative normalization between the **Min-Bias** data and the **Jet20** data comes from the **Jet#1** momentum distribution plot. The relative normalization between the **Min-Bias** data and the **Track 12** data comes from this plot.

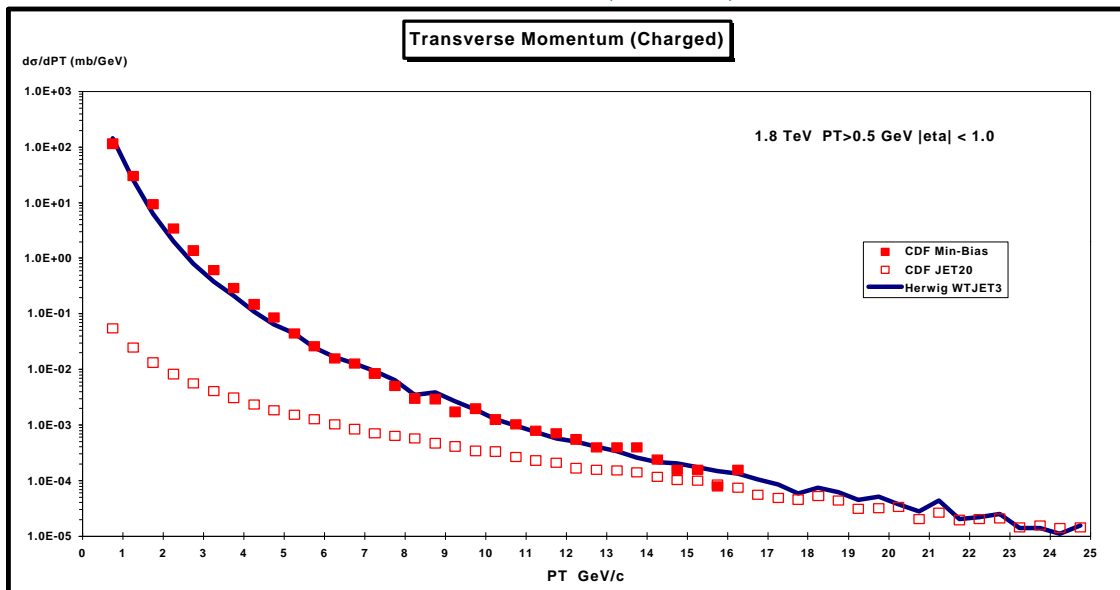
# Min-Bias Data – Differential Cross Sections

## PTmax (highest PT charged particle) Cross Section (mb/GeV):



CDF Min-Bias Data normalization fixed from Jet#1 PT distribution. Relative normalization between the Min-Bias data and the Jet20 data comes from the Jet#1 PT distribution plot and relative normalization between the Min-Bias data and the Track12 data comes from this plot.

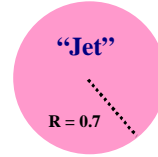
## Transverse Momentum Cross Section (mb/GeV):



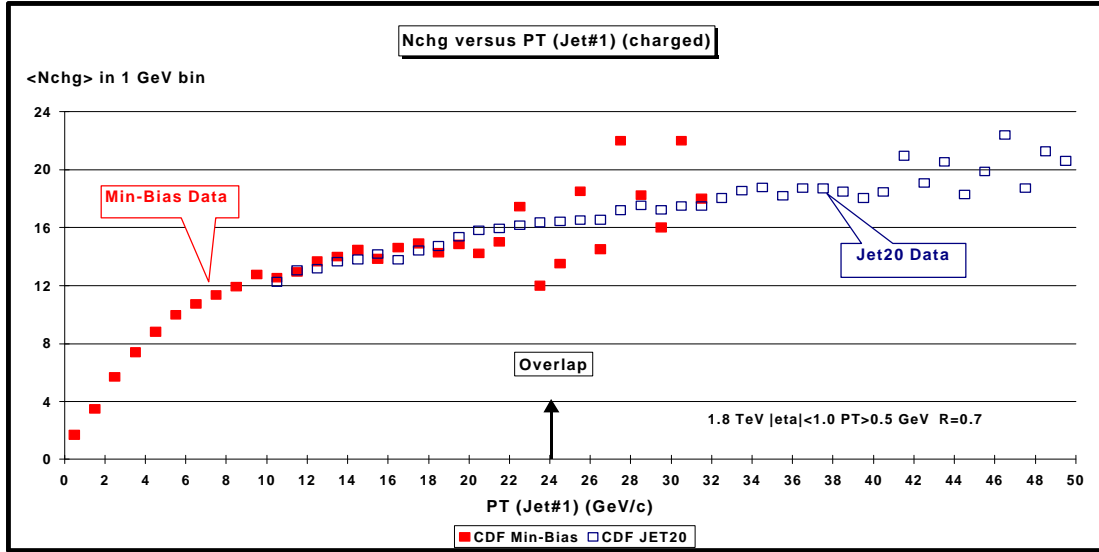
CDF Min-Bias Data normalization fixed from Jet#1 PT distribution. Relative normalization between the Min-Bias data and the Jet20 data comes from the Jet#1 PT distribution.

# CDF Data – $\langle N_{chg} \rangle$ vs $PT(jet\#1)$

“Jet” = Circular Region  $\rightarrow$

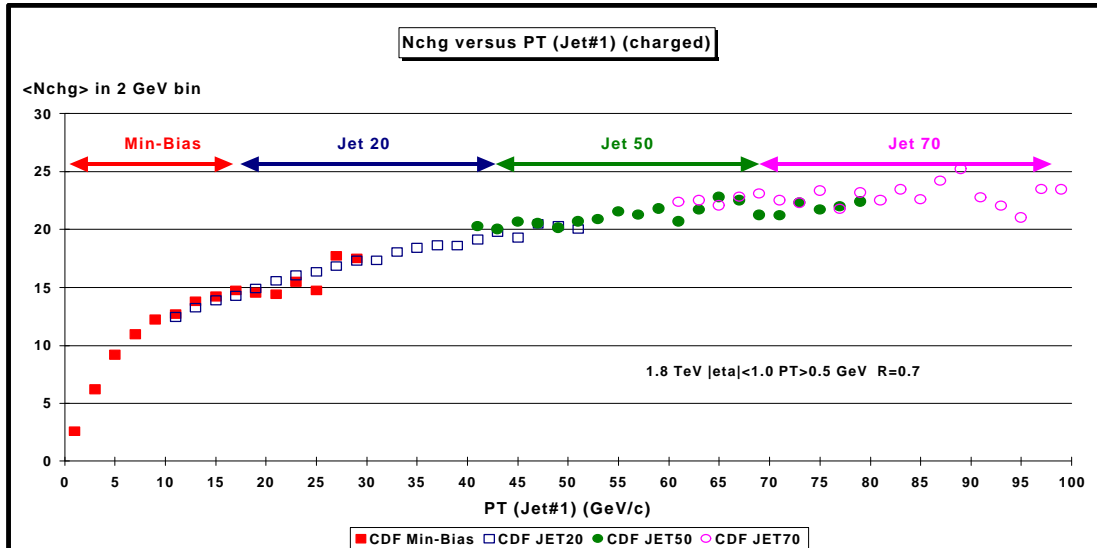


## Average Number of Charged Particles versus $PT(jet\#1)$ (highest PT jet):



CDF Data Only

## Average Number of Charged Particles versus $PT(jet\#1)$ (highest PT jet):

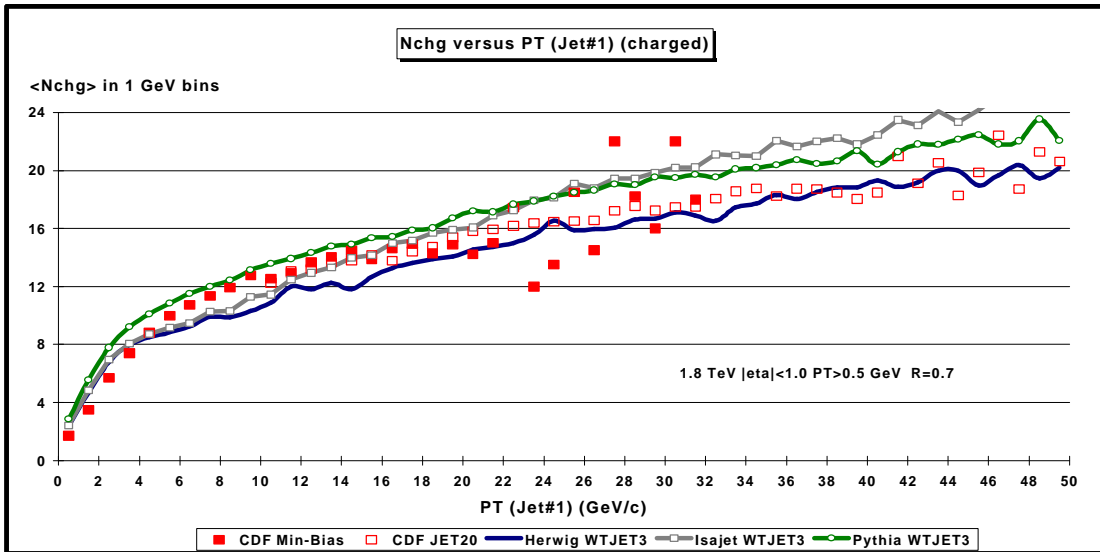


CDF Data Only

# QCD-MC Predictions – $\langle N_{chg} \rangle$ vs $PT(jet\#1)$

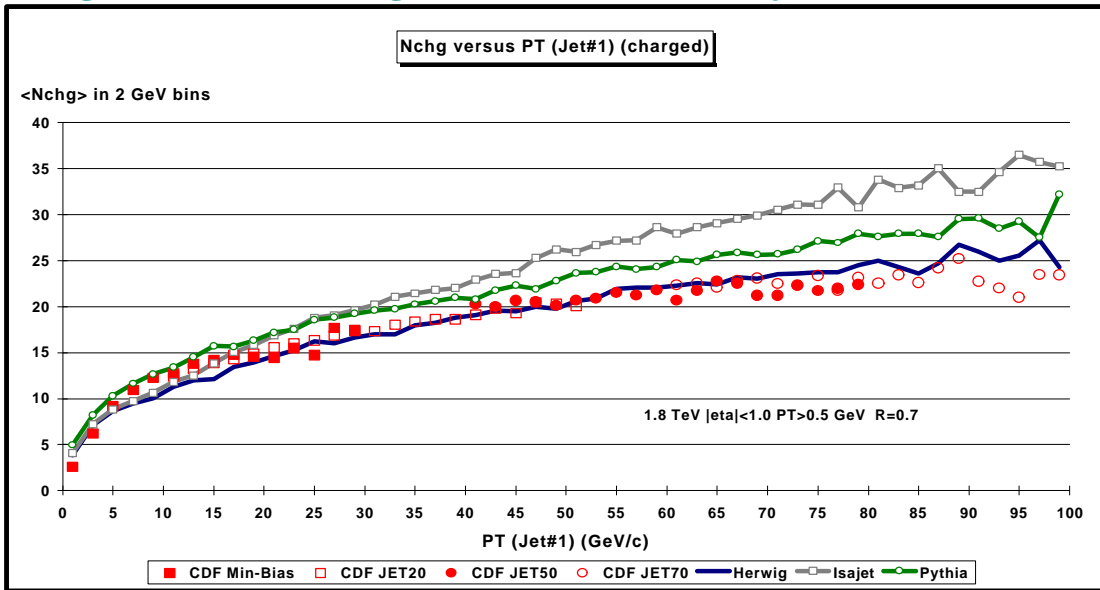


## Average Number of Charged Particles versus $PT(jet\#1)$ (highest PT jet):



CDF Data plus QCD Monte-Carlo Predictions

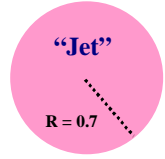
## Average Number of Charged Particles versus $PT(jet\#1)$ (highest PT jet):



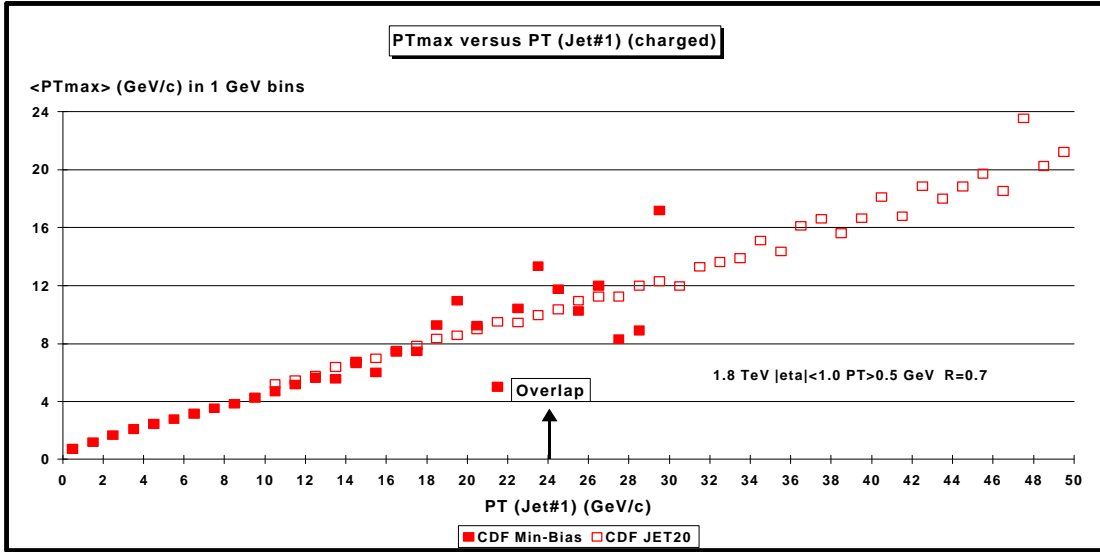
CDF Data plus QCD Monte-Carlo Predictions

# CDF Data – $\langle PT_{max} \rangle$ vs $PT(jet\#1)$

“Jet” = Circular Region  $\rightarrow$

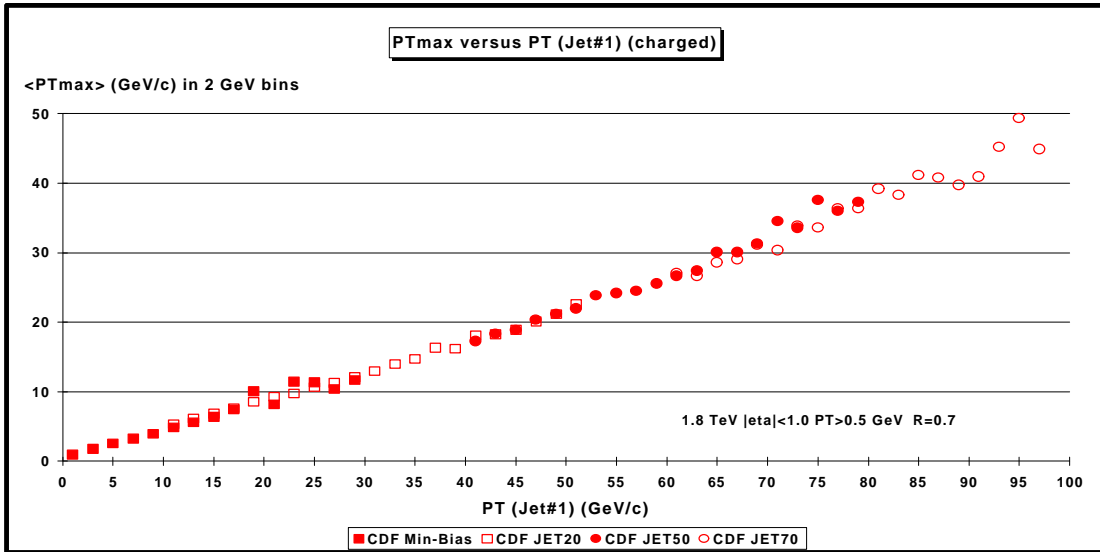


$\langle PT_{max} \rangle$  (highest charged particle PT) versus  $PT(jet\#1)$  (highest PT jet):



CDF Data only

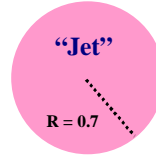
$\langle PT_{max} \rangle$  (highest charged particle PT) versus  $PT(jet\#1)$  (highest PT jet):



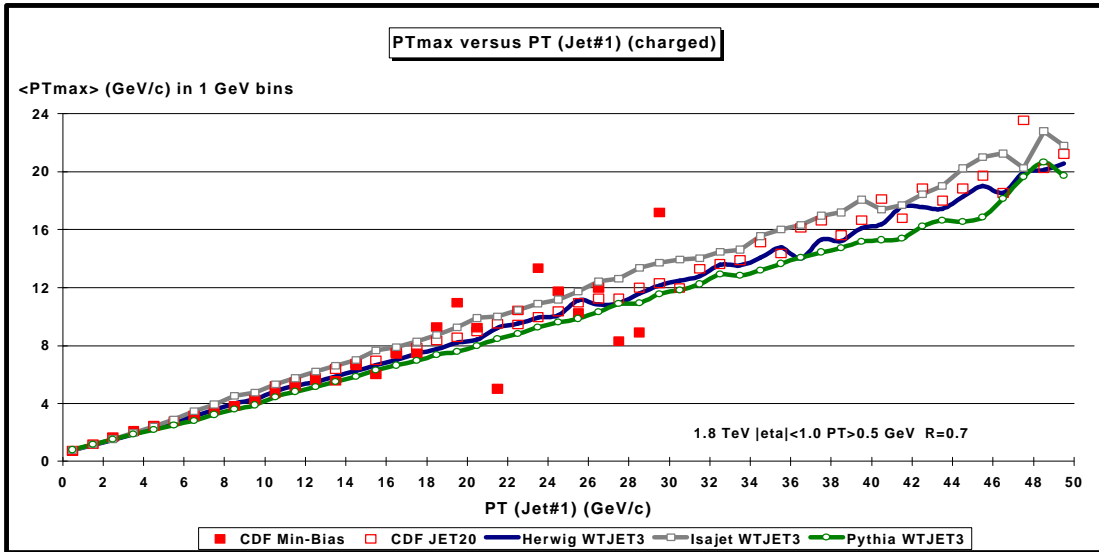
CDF Data only

# QCD-MC Predictions – $\langle PT_{max} \rangle$ vs $PT(jet\#1)$

“Jet” = Circular Region  $\rightarrow$

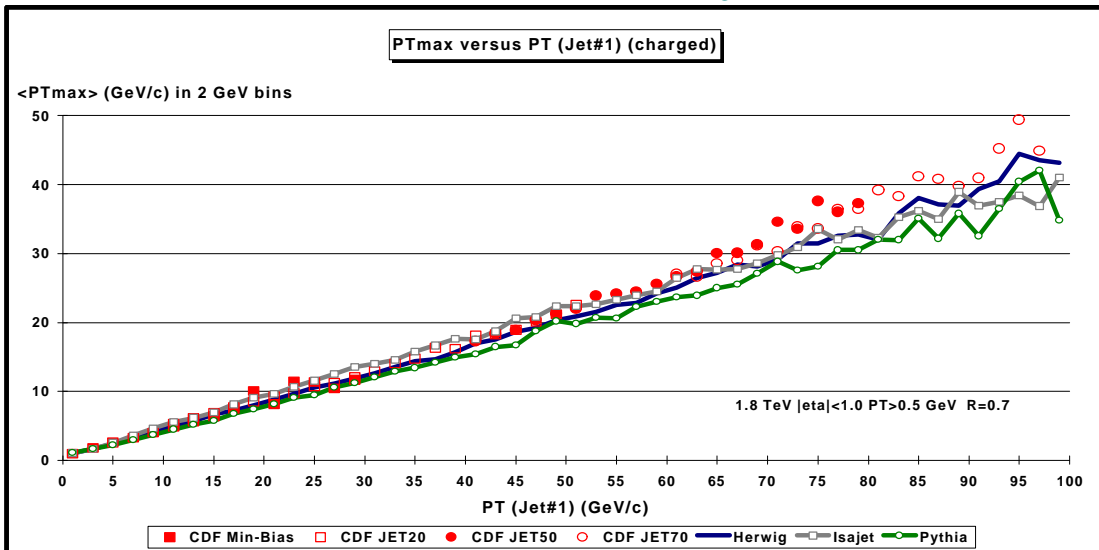


$\langle PT_{max} \rangle$  (highest charged particle PT) versus  $PT(jet\#1)$  (highest PT jet):



CDF Data plus QCD Monte-Carlo Predictions

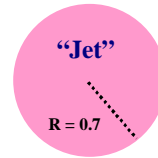
$\langle PT_{max} \rangle$  (highest charged particle PT) versus  $PT(jet\#1)$  (highest PT jet):



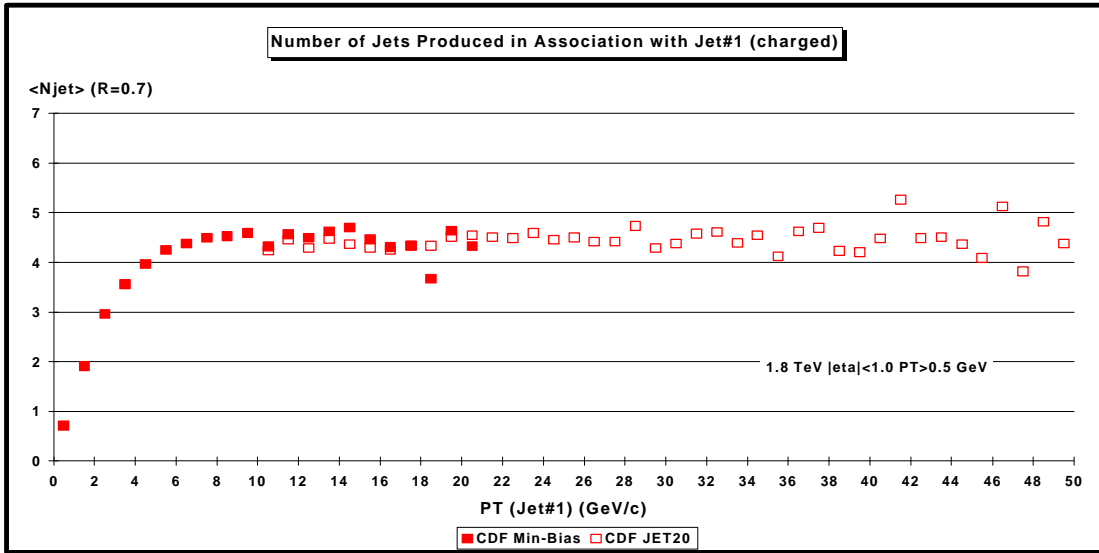
CDF Data plus QCD Monte-Carlo Predictions

# CDF Data - Number of Jets Produced in Association with Jet#1

“Jet” = Circular Region →

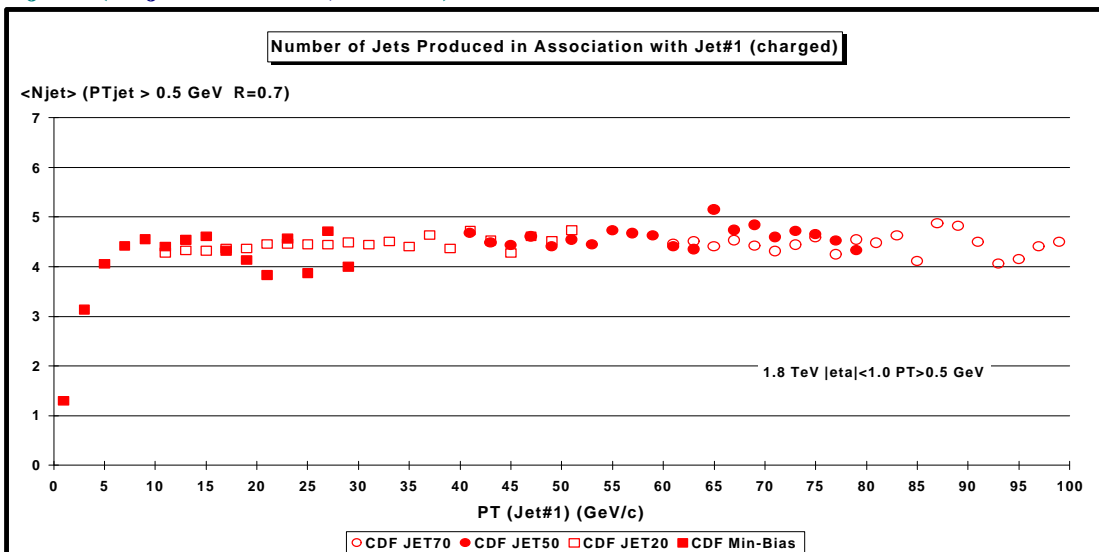


$\langle N_{jet} \rangle$  ( $PT_{jet} > 0.5$  GeV,  $R = 0.7$ ) Produced in Association with Jet#1:



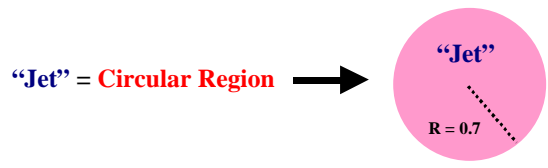
CDF Data (Jet#1 not included).

$\langle N_{jet} \rangle$  ( $PT_{jet} > 0.5$  GeV,  $R = 0.7$ ) Produced in Association with Jet#1:

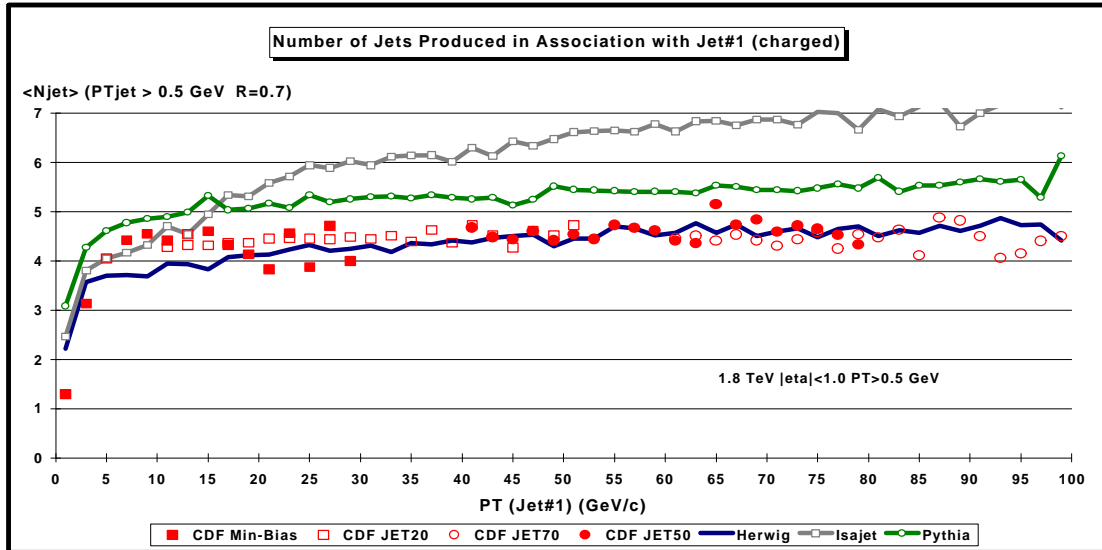


CDF Data (Jet#1 not included).

# QCD-MC Predictions - Number of Jets Produced in Association with Jet#1

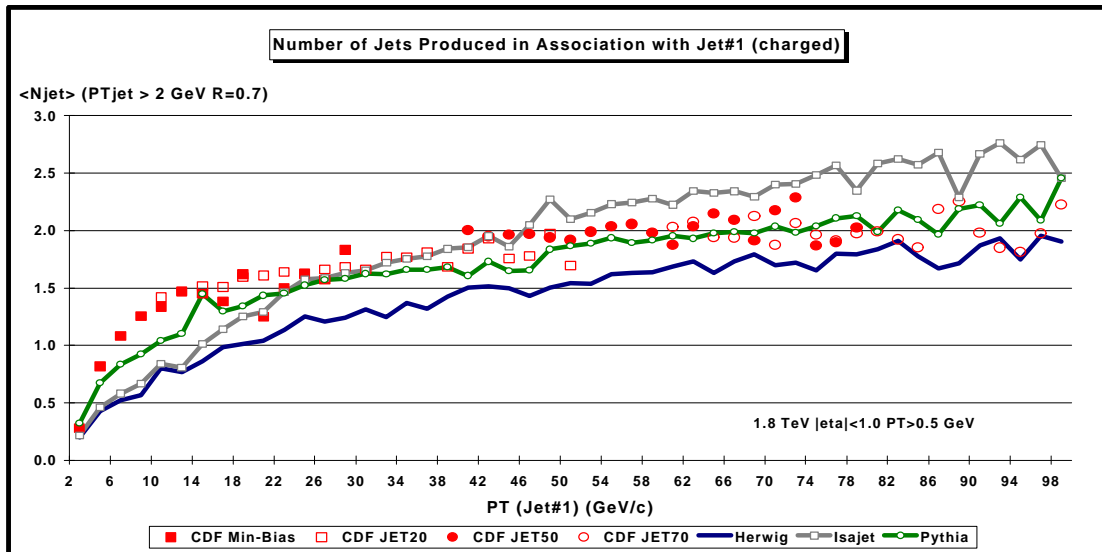


**<Njet> (PTjet > 0.5 GeV, R = 0.7) Produced in Association with Jet#1:**



CDF Data plus QCD Monte-Carlo Predictions (Jet#1 not included).

**<Njet> (PTjet > 2.0 GeV, R = 0.7) Produced in Association with Jet#1:**

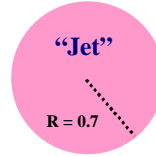


CDF Data plus QCD Monte-Carlo Predictions (Jet#1 not included).

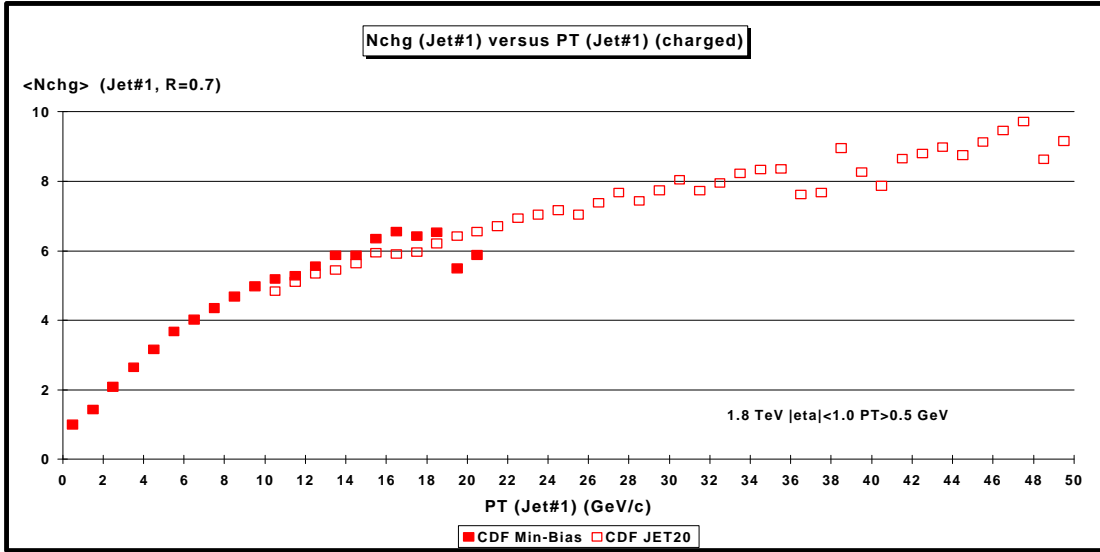


# CDF Data – $\langle N_{ch} \text{Jet\#1} \rangle$ vs $PT(\text{jet\#1})$

“Jet” = Circular Region  $\rightarrow$

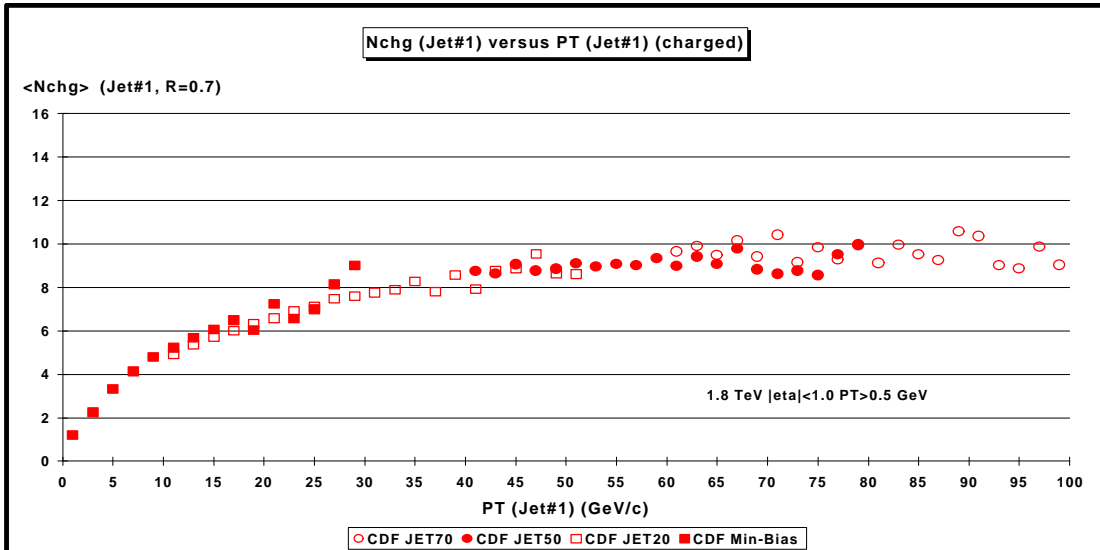


## Average Number of Charged Particles in Jet#1 versus $PT(\text{jet\#1})$ :



CDF Data Only

## Average Number of Charged Particles in Jet#1 versus $PT(\text{jet\#1})$ :

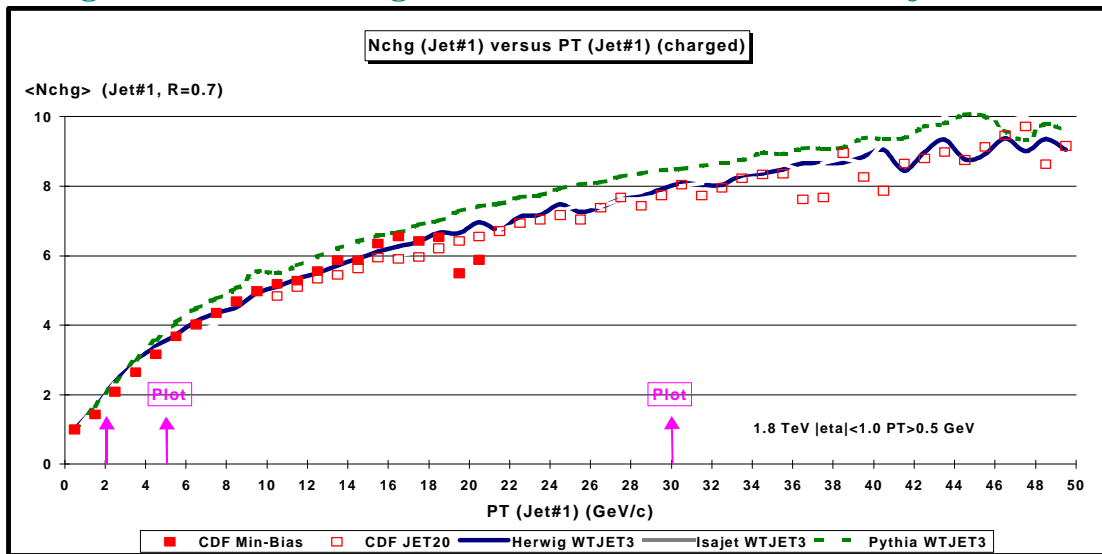


CDF Data Only

# QCD-MC Predictions – $\langle N_{chgJet\#1} \rangle$ vs $PT(jet\#1)$

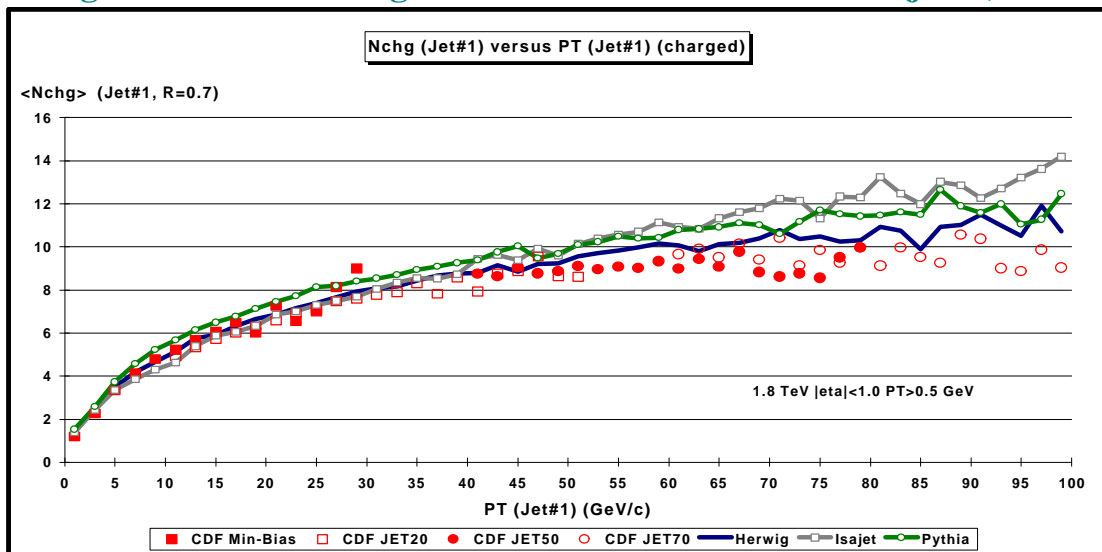


## Average Number of Charged Particles in Jet#1 versus $PT(jet\#1)$ :



CDF Data plus QCD Monte-Carlo Predictions

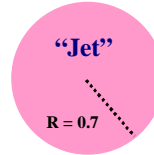
## Average Number of Charged Particles in Jet#1 versus $PT(jet\#1)$ :



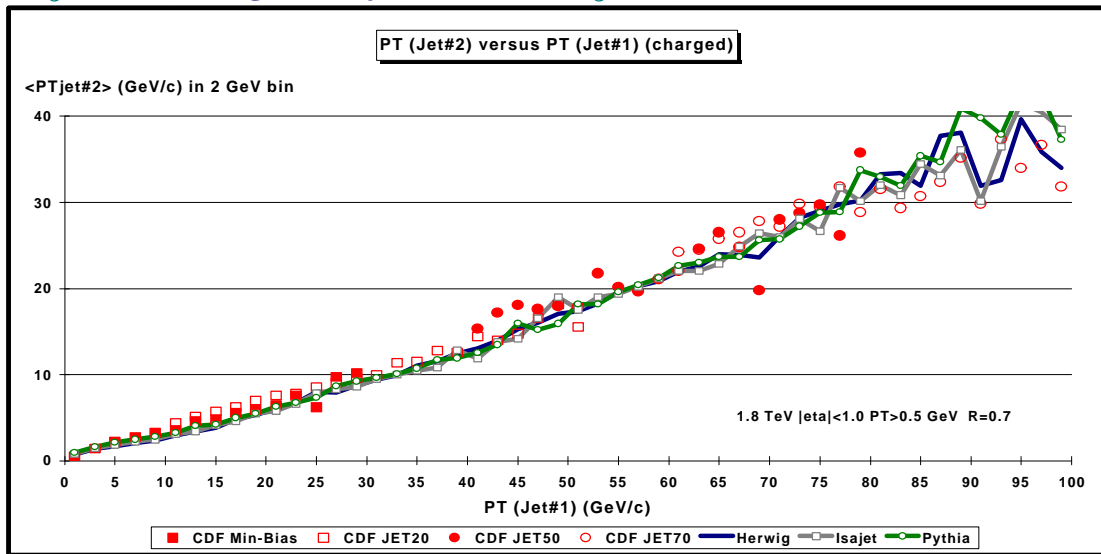
CDF Data plus QCD Monte-Carlo Predictions

# QCD-MC Predictions – $\langle PT_{jet\#2} \rangle$ & $\langle PT_{jet\#3} \rangle$ versus $PT_{jet\#1}$

“Jet” = Circular Region  $\rightarrow$

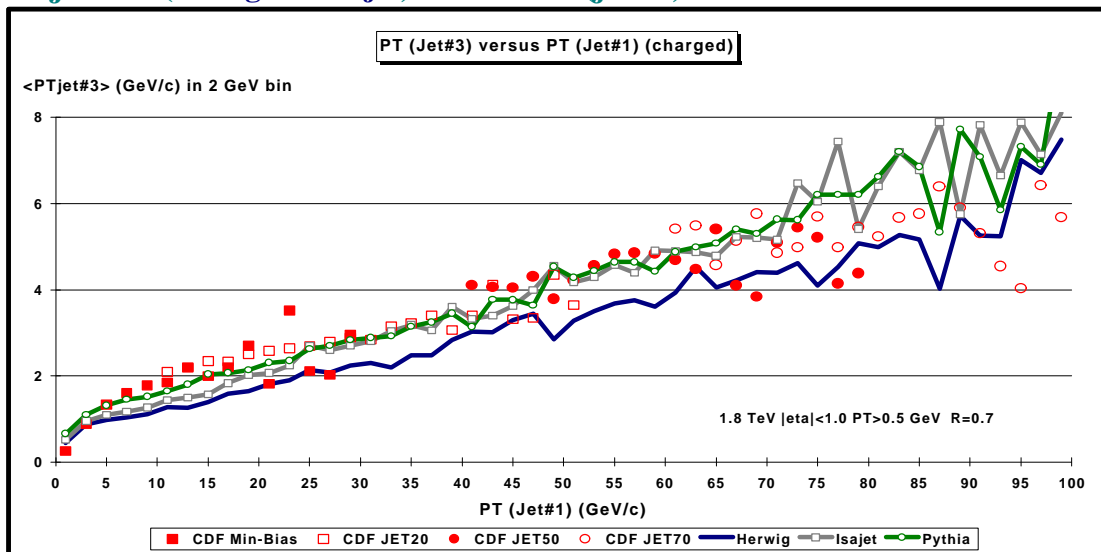


## $\langle PT_{jet\#2} \rangle$ (2<sup>nd</sup> highest $PT_{jet}$ ) versus $PT_{jet\#1}$ :



CDF Data plus QCD Monte-Carlo Predictions

## $\langle PT_{jet\#3} \rangle$ (3<sup>rd</sup> highest $PT_{jet}$ ) versus $PT_{jet\#1}$ :

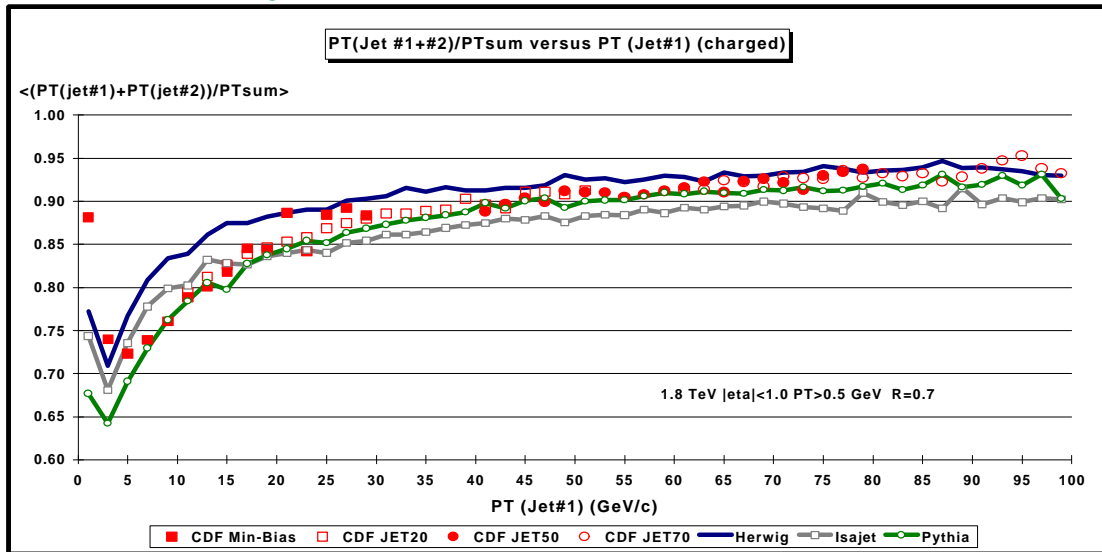


CDF Data plus QCD Monte-Carlo Predictions

# QCD-MC Predictions – $\langle R12 \rangle$ & $\langle RJ21 \rangle$ versus $PT(\text{jet}\#1)$

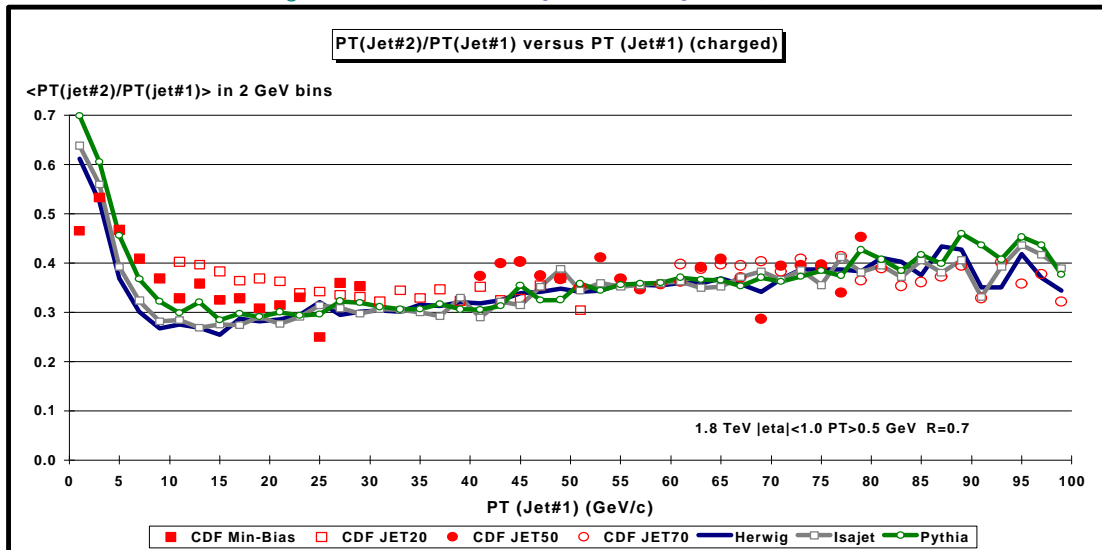


$\langle R12 \rangle$  versus  $PT(\text{jet}\#1)$  ( $R12=(PT(\text{jet}\#1)+PT(\text{jet}\#2))/PT_{\text{sum}}$ ):



CDF Data plus QCD Monte-Carlo Predictions

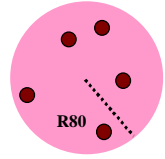
$\langle RJ21 \rangle$  versus  $PT(\text{jet}\#1)$  ( $RJ21=PT(\text{jet}\#2)/PT(\text{jet}\#1)$ ):



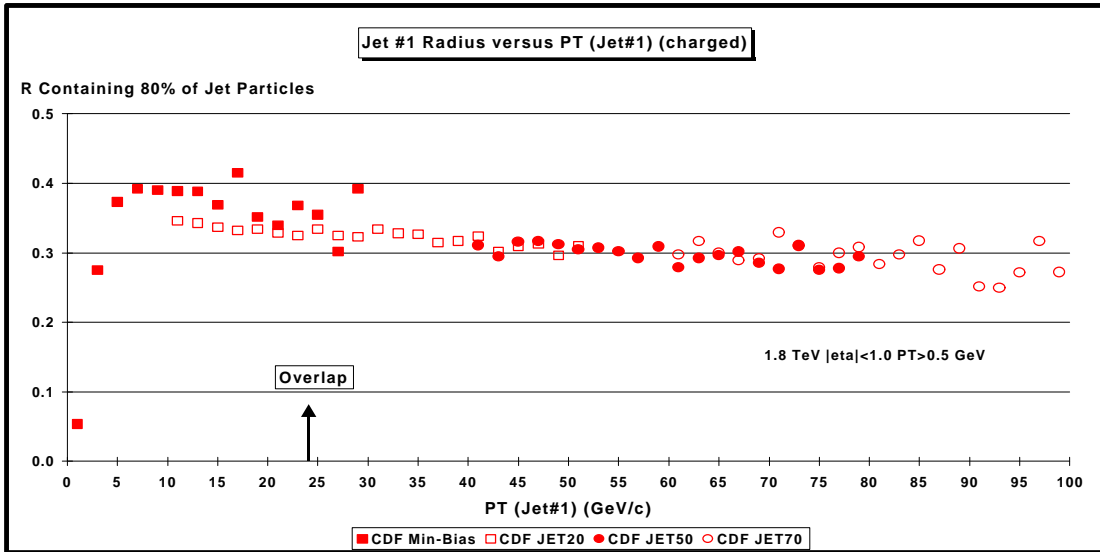
CDF Data plus QCD Monte-Carlo Predictions

# MB Jets – “Jet Size” versus PT(jet#1)

Radius containing 80% of Jet Particles

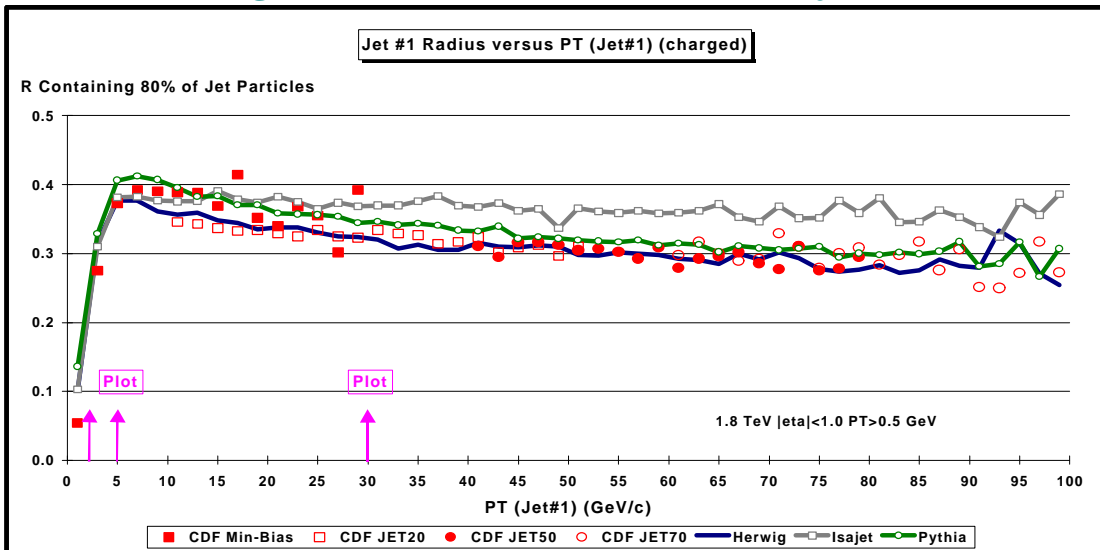


## Radius containing 80% of Jet#1 Particles versus PT(jet#1):



CDF Data only.

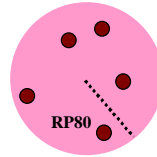
## Radius containing 80% of Jet#1 Particles versus PT(jet#1):



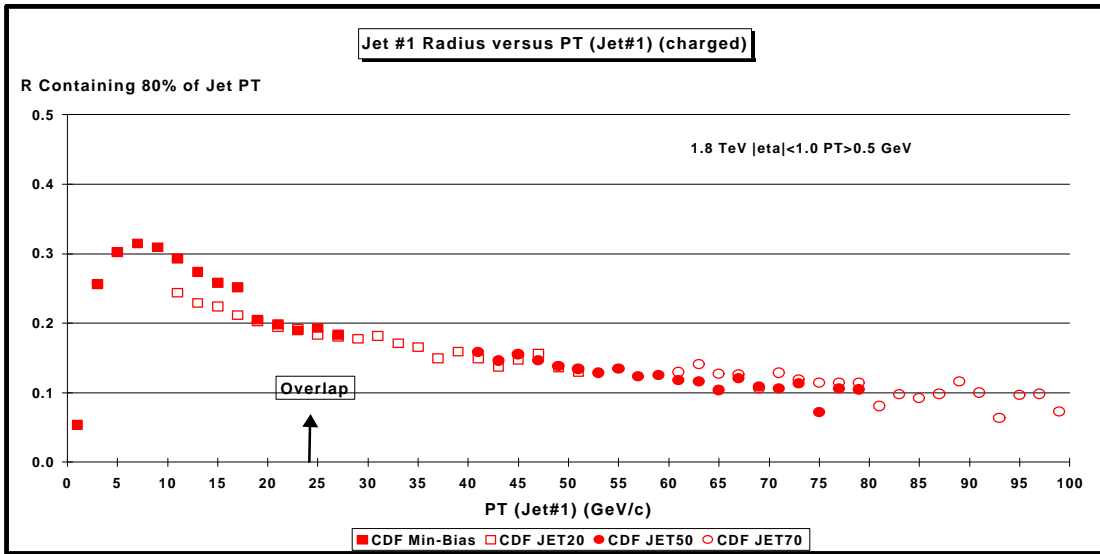
CDF Data plus QCD Monte-Carlo Predictions.

# MB Jets – “Jet Size” versus PT(jet#1)

Radius containing 80% of Jet PT

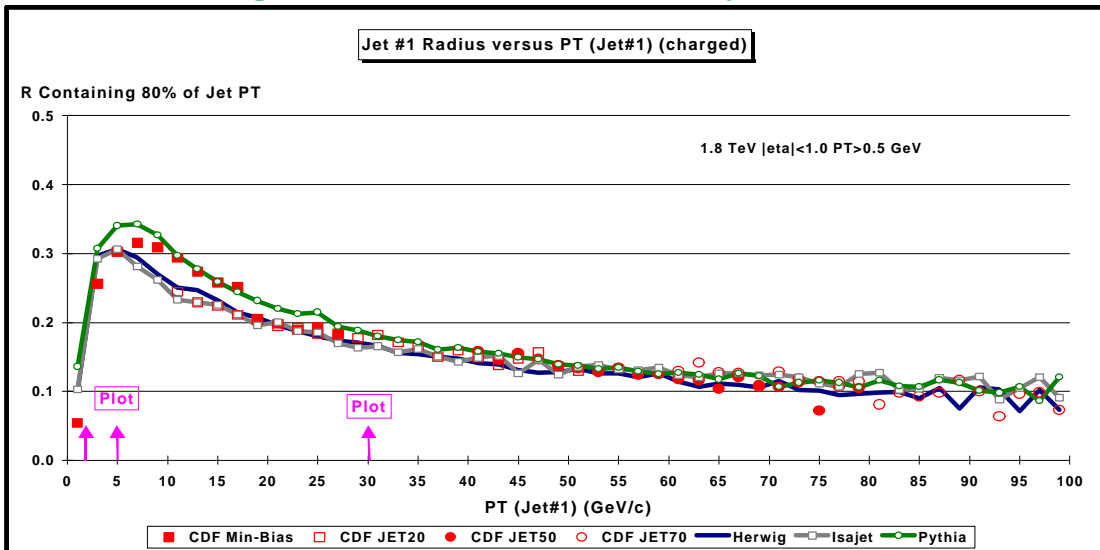


## Radius containing 80% of Jet#1 PT versus PT(jet#1):



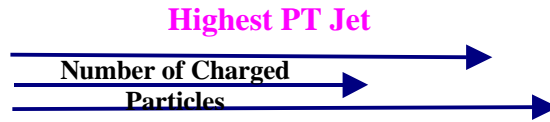
CDF Data only.

## Radius containing 80% of Jet#1 PT versus PT(jet#1):

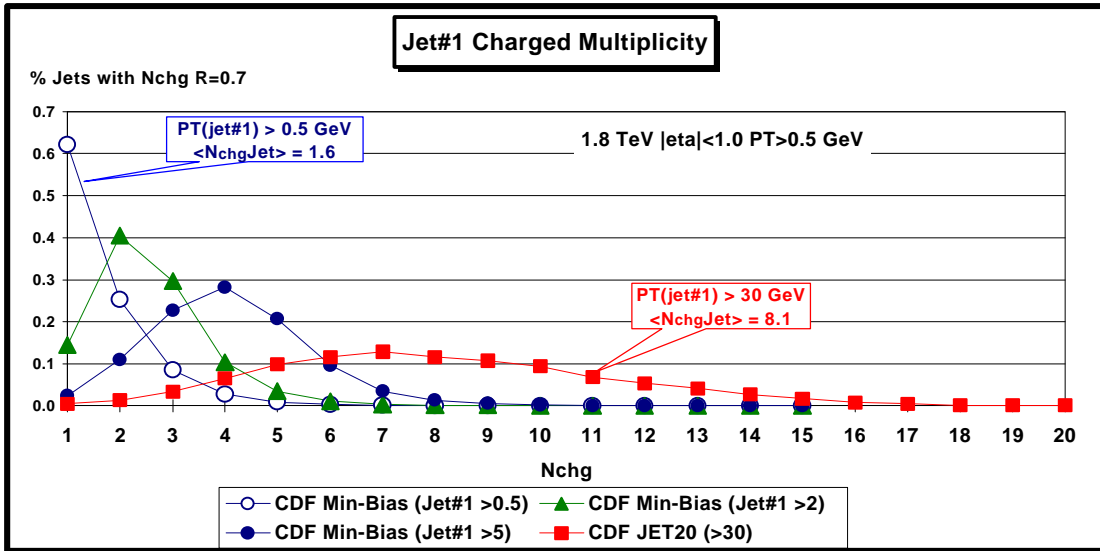


CDF Data plus QCD Monte-Carlo Predictions.

# Jet Evolution – Jet#1 Charged Multiplicity

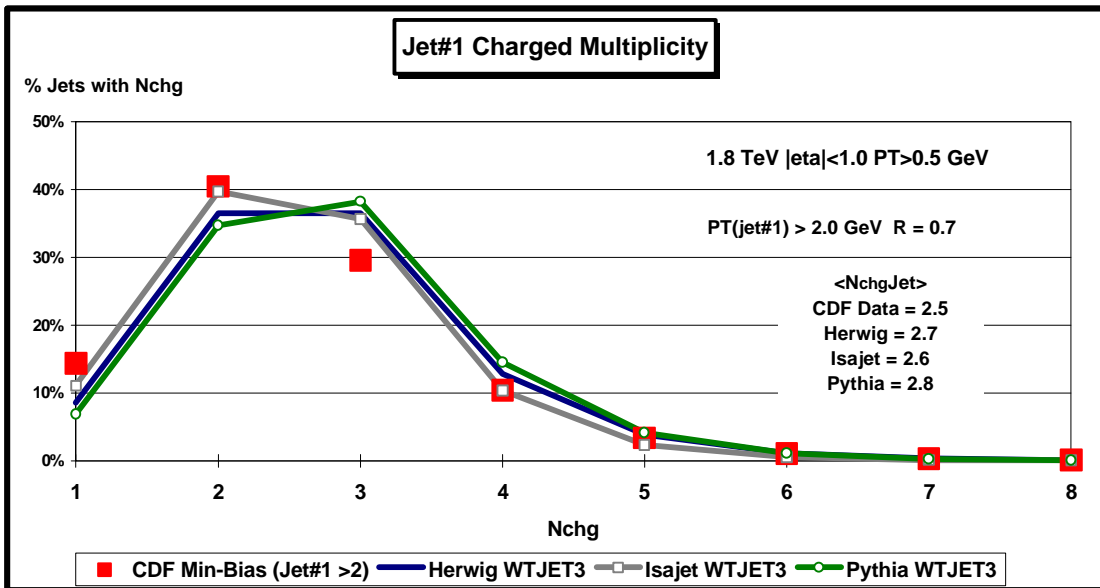


## Number of Charged Particles within Jet#1 (R = 0.7):

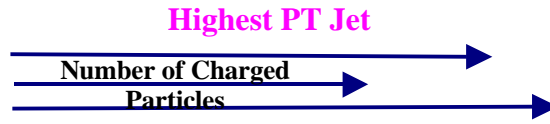


CDF Data

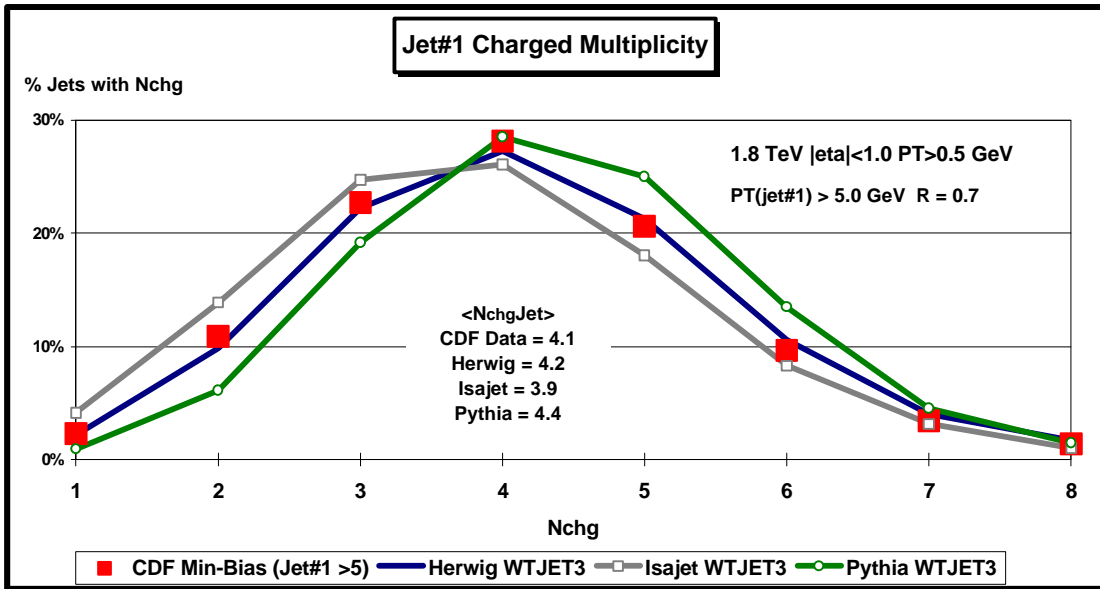
## Number of Charged Particles within Jet#1 (PT(jet#1) > 2 GeV, R = 0.7):



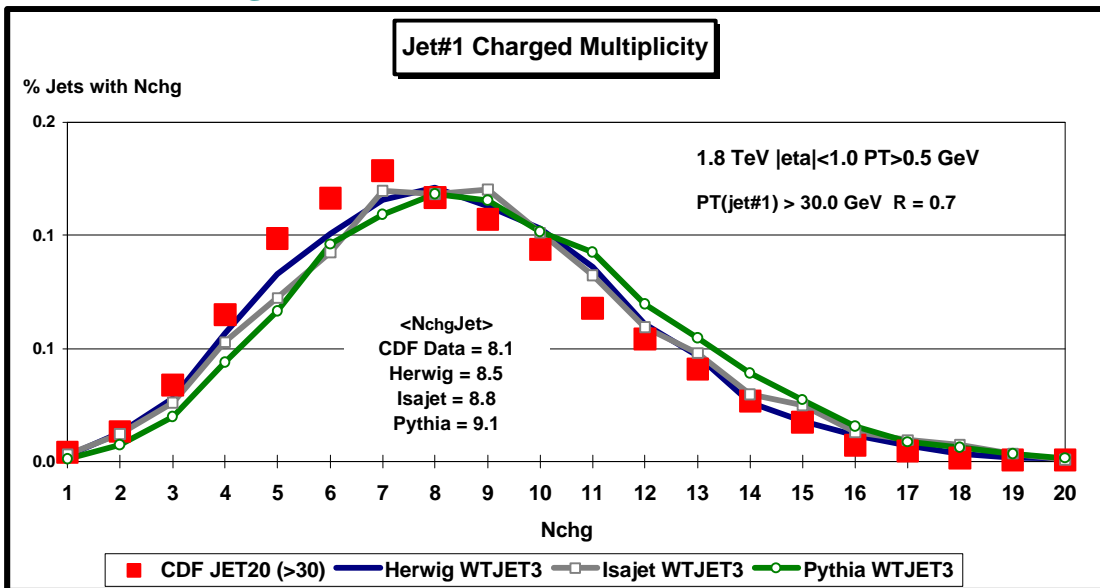
# Jet Evolution – Jet#1 Charged Multiplicity



Number of Charged Particles within Jet#1 ( $PT(jet\#1) > 5 \text{ GeV}$ ,  $R = 0.7$ ):



Number of Charged Particles within Jet#1 ( $PT(jet\#1) > 30 \text{ GeV}$ ,  $R = 0.7$ ):

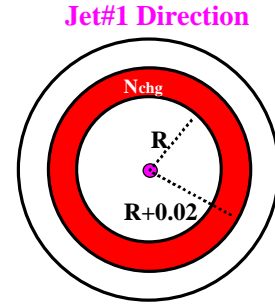




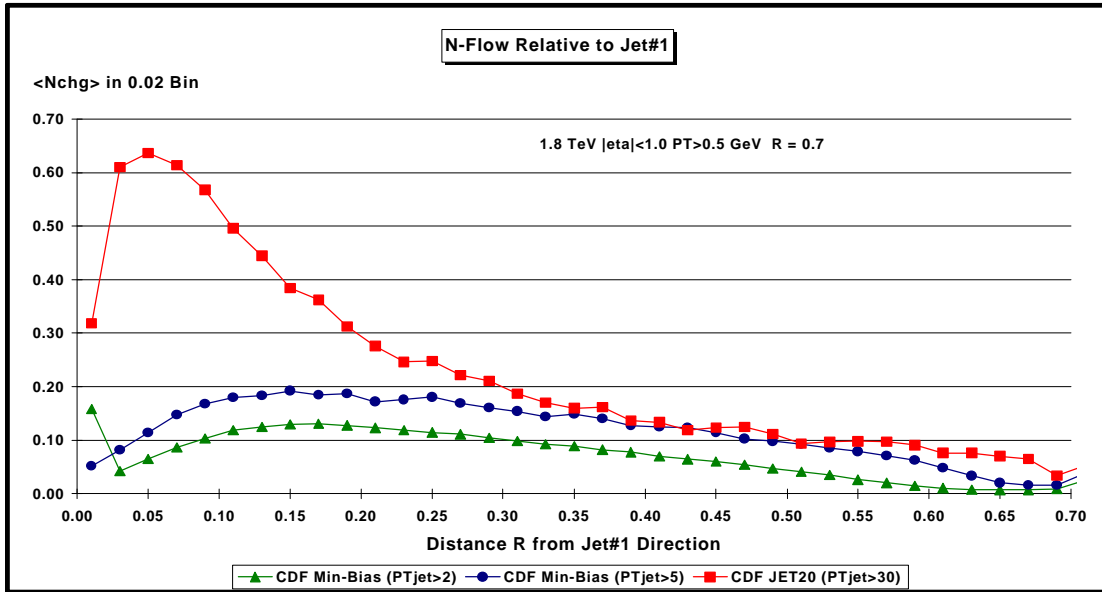
# Jet Evolution – Jet#1 Radial N-Flow

Look at the distribution of charged particles around the direction of Jet#1 where

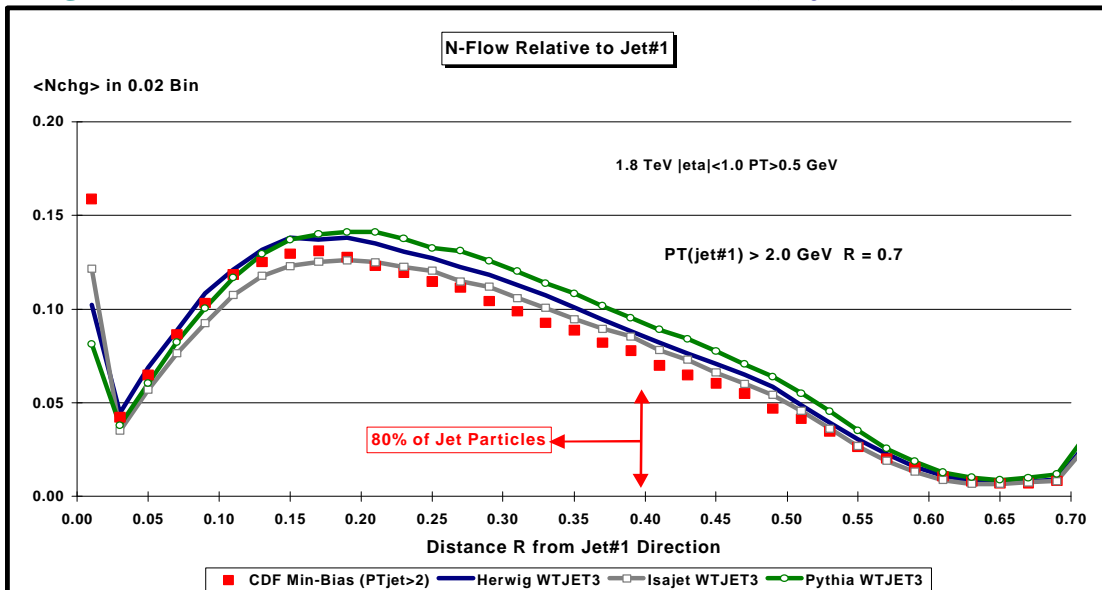
$$R_i = \sqrt{(h_i - h_{jet})^2 + (f_i - f_{jet})^2}$$



$\langle N_{chg} \rangle$  in  $\Delta R = 0.02$  bin around Jet#1 direction:



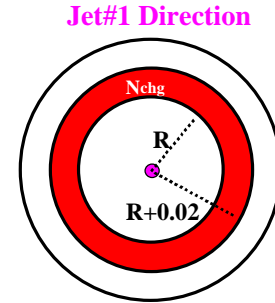
$\langle N_{chg} \rangle$  in  $\Delta R = 0.02$  bin around Jet#1 direction ( $PT(jet\#1) > 2$  GeV):



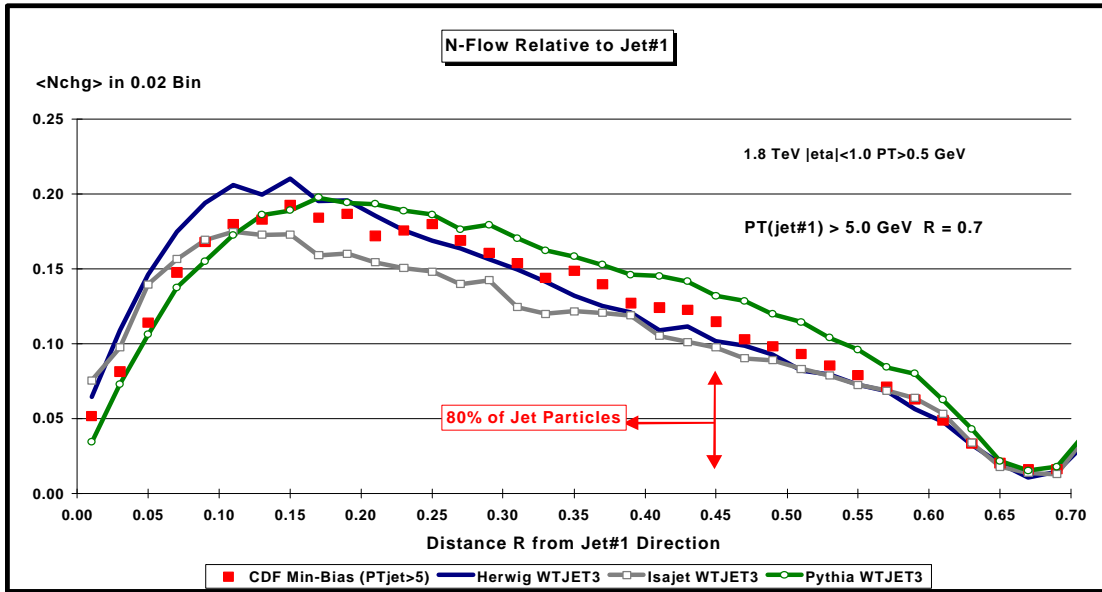
# Jet Evolution – Jet#1 Radial N-Flow

Look at the distribution of charged particles around the direction of Jet#1 where

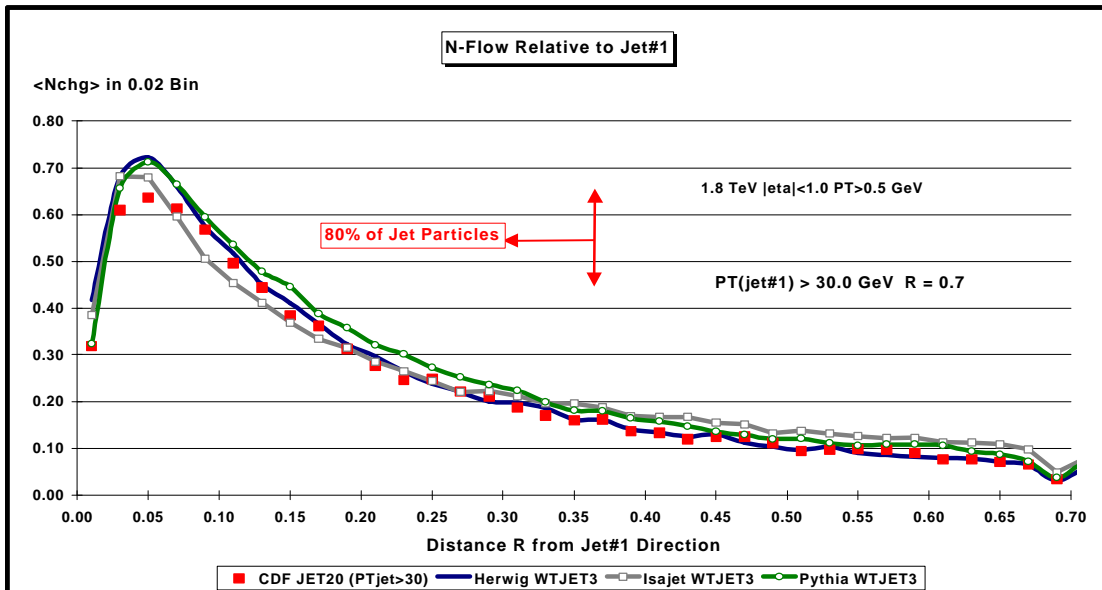
$$R_i = \sqrt{(h_i - h_{jet})^2 + (f_i - f_{jet})^2}$$



$\langle N_{chg} \rangle$  in  $\Delta R = 0.02$  bin around Jet#1 direction  
( $PT(jet\#1) > 5 \text{ GeV}$ ):



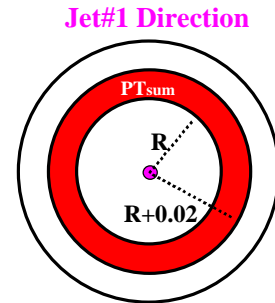
$\langle N_{chg} \rangle$  in  $\Delta R = 0.02$  bin around Jet#1 direction ( $PT(jet\#1) > 30 \text{ GeV}$ ):



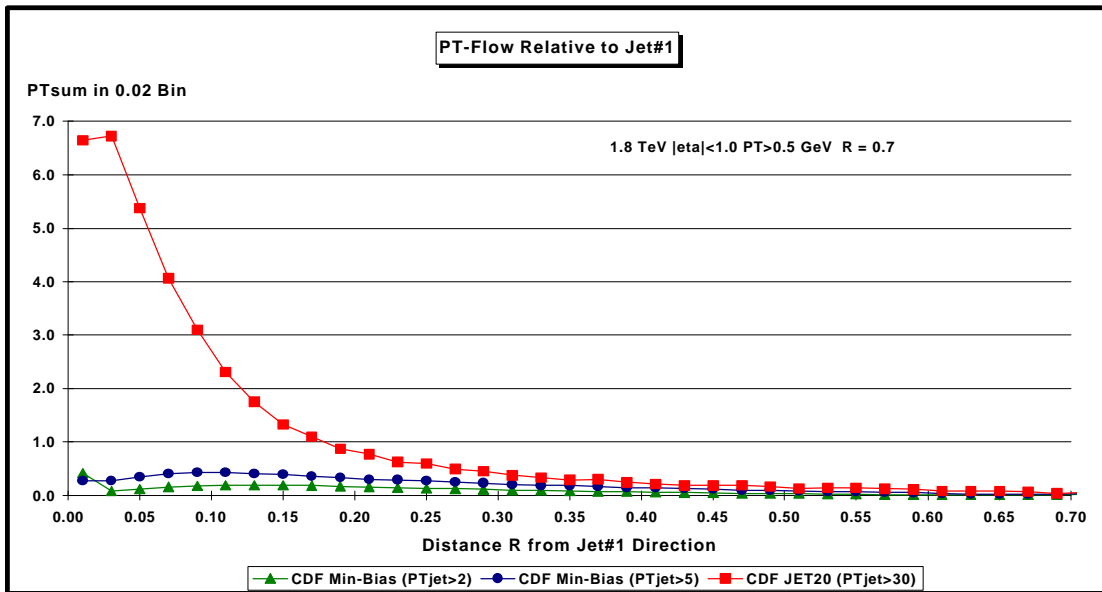
# Jet Evolution – Jet#1 Radial PT-Flow

Look at the distribution of charged particle **transverse momentum** around the direction of **Jet#1** where

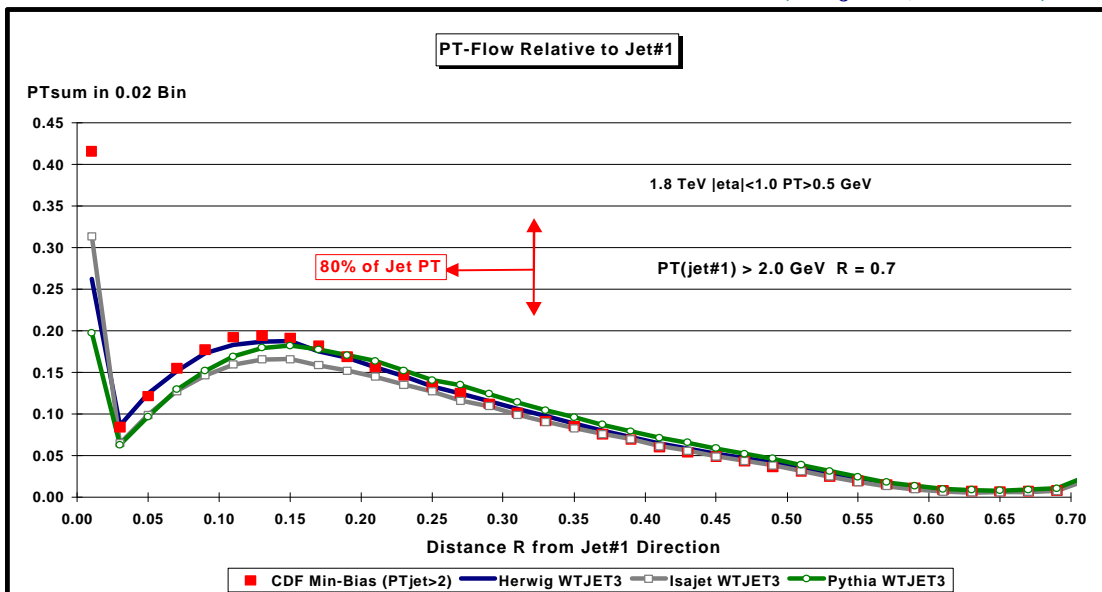
$$R_i = \sqrt{(h_i - h_{jet})^2 + (f_i - f_{jet})^2}$$



**<PTsum>** in  $\Delta R = 0.02$  bin around Jet#1 direction:



**<PTsum>** in  $\Delta R = 0.02$  bin around Jet#1 direction (**PT(jet#1) > 2 GeV**):

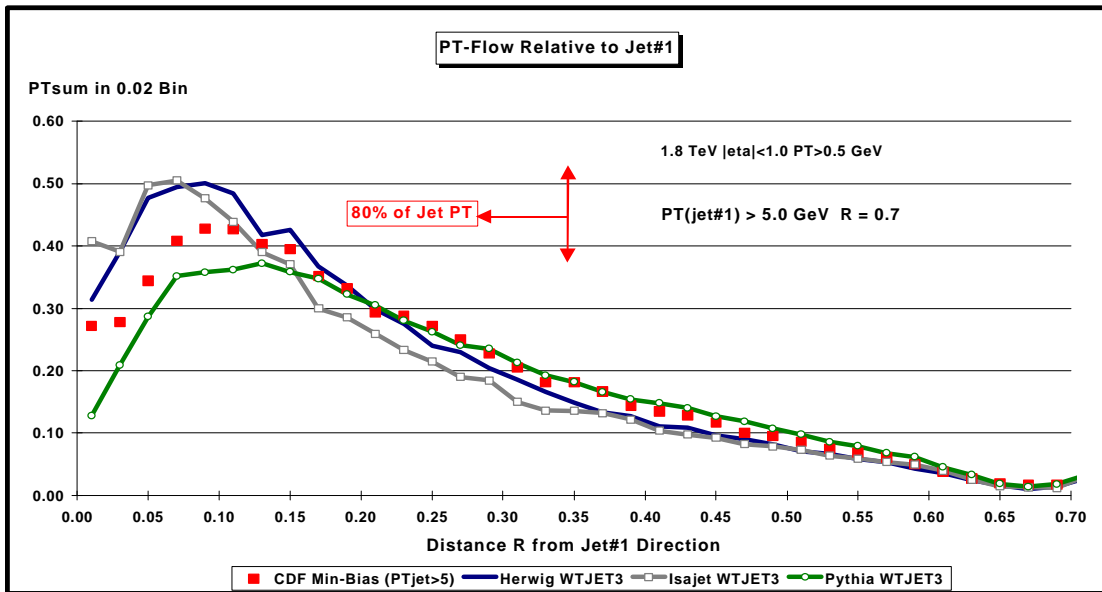
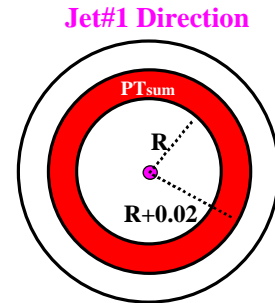


# Jet Evolution – Jet#1 Radial PT-Flow

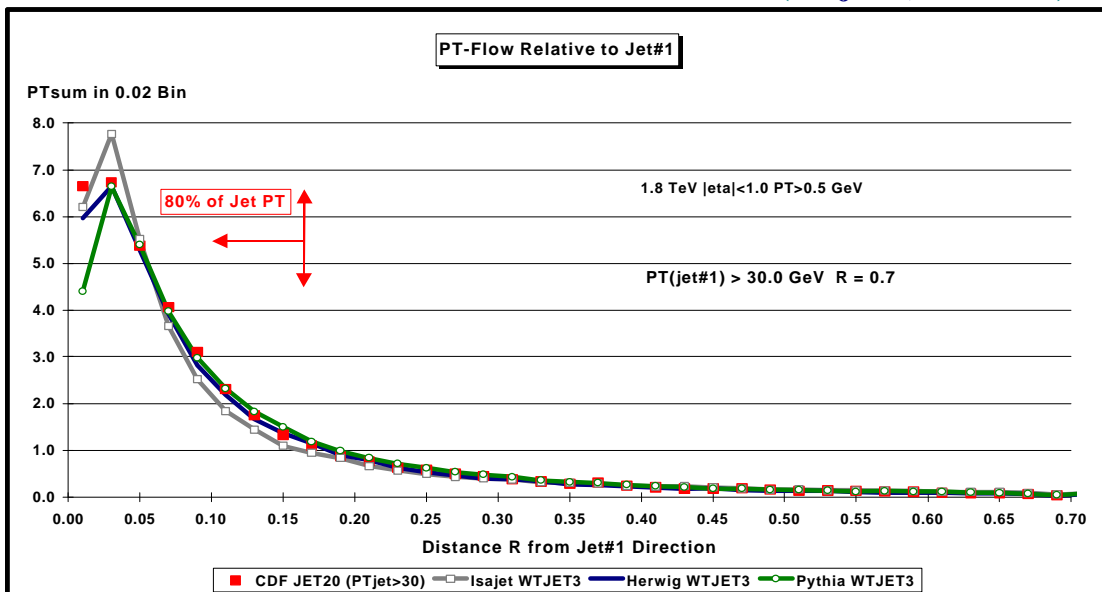
Look at the distribution of charged particle **transverse momentum** around the direction of **Jet#1** where

$$R_i = \sqrt{(h_i - h_{jet})^2 + (f_i - f_{jet})^2}$$

**<PTsum>** in  $\Delta R = 0.02$  bin around Jet#1 direction  
(PT(jet#1) > 5 GeV):



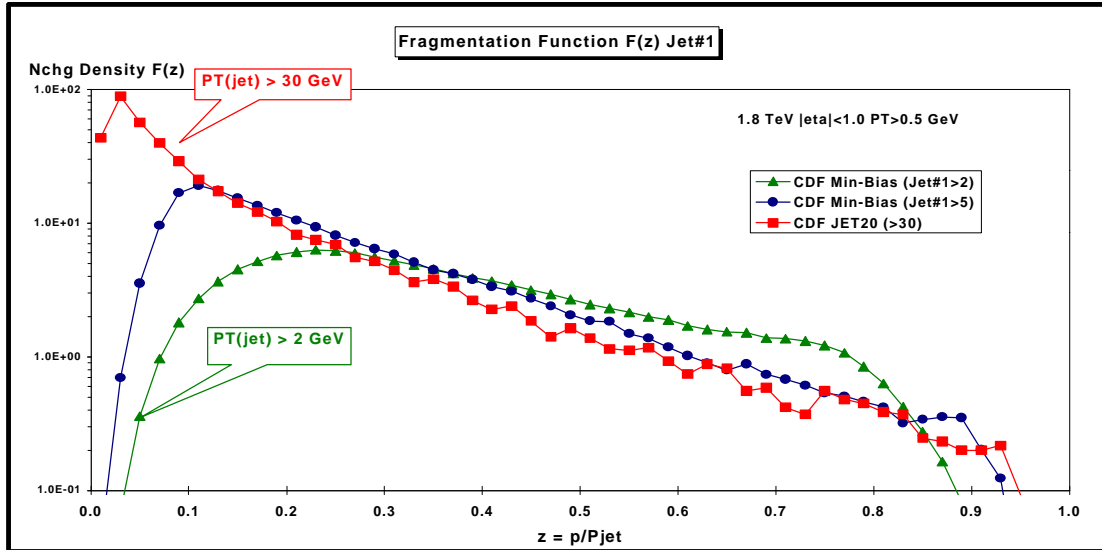
**<PTsum>** in  $\Delta R = 0.02$  bin around Jet#1 direction (PT(jet#1) > 30 GeV):



# Jet Evolution – Jet#1 Fragmentation Function

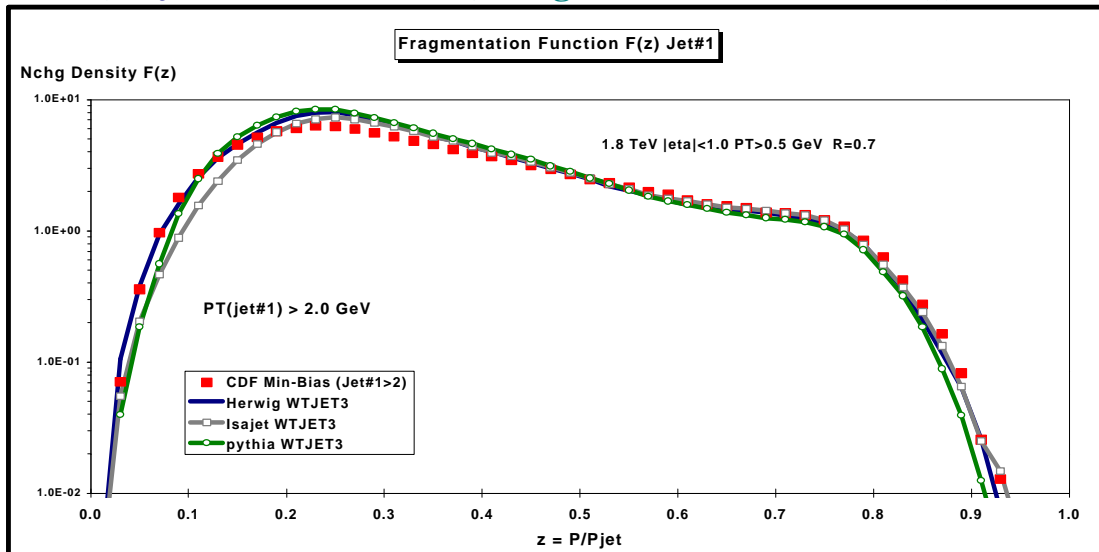


## Jet#1 (R = 0.7) Fragmentation Function F(z):



CDF Data

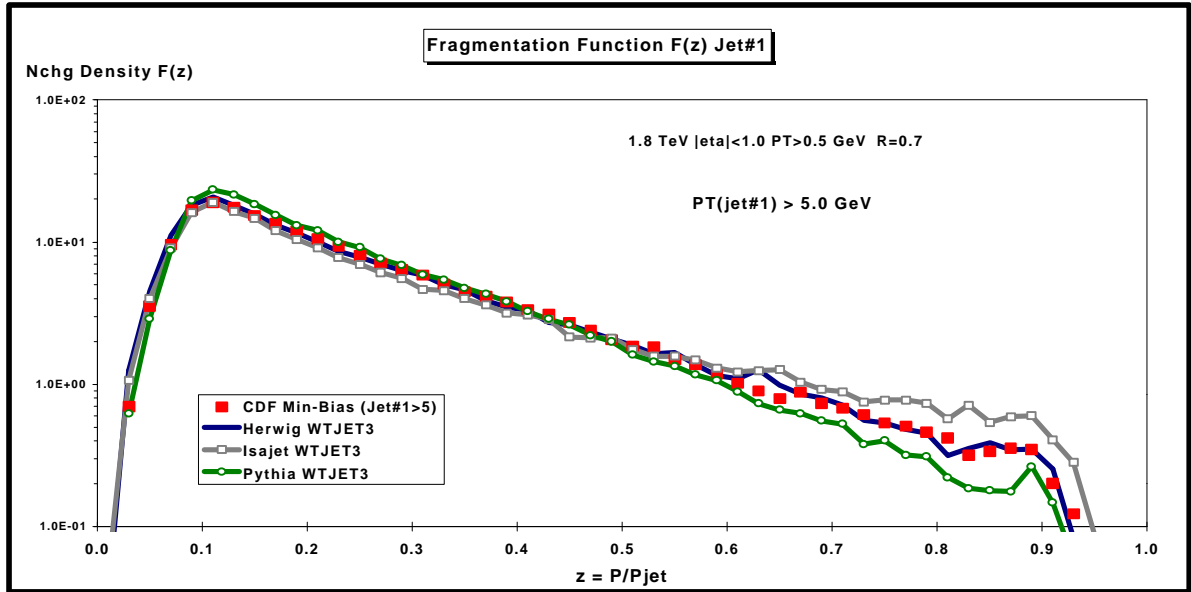
## Jet#1 (PT(jet#1) > 2 GeV, R = 0.7) Fragmentation Function F(z):



# Jet Evolution – Jet#1 Fragmentation Function



## Jet#1 (PT > 5 GeV, R = 0.7) Fragmentation Function F(z):



## Jet#1 (PT > 30 GeV, R = 0.7) Fragmentation Function F(z):

