

Mathematics Prerequisite Evaluation for Quantum Mechanics I

correct

Consider the following two matrices:

$$A = \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}; B = \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$$

What is $A + B$?

$$(29) \quad A + B = \begin{pmatrix} 1 & 1 \\ 1 & -1 \end{pmatrix}$$

What is AB (multiplication)?

$$(24) \quad A \cdot B = \begin{pmatrix} 0 & 1 \\ -1 & 0 \end{pmatrix}$$

What are the eigenvalues and eigenvectors of the matrix, $A + B$?

$$\begin{vmatrix} 1-\lambda & 1 \\ 1 & -1-\lambda \end{vmatrix} = 0 \rightarrow (1-\lambda)(-1-\lambda) - 1 = 0 \rightarrow -1 + \lambda^2 - 1 = 0 \\ \rightarrow \lambda^2 = 2 \rightarrow \lambda = \pm\sqrt{2}$$

$$(6) \quad \begin{pmatrix} 1-\sqrt{2} & 1 \\ 1 & -1-\sqrt{2} \end{pmatrix} \begin{pmatrix} -1 \\ 1-\sqrt{2} \end{pmatrix} = 0 \Rightarrow \text{eigenvec.} = \begin{pmatrix} -1 \\ 1-\sqrt{2} \end{pmatrix} \text{ for } \lambda = \sqrt{2}$$

$$(3) \quad \begin{pmatrix} 1+\sqrt{2} & 1 \\ 1 & -1-\sqrt{2} \end{pmatrix} \begin{pmatrix} -1 \\ 1+\sqrt{2} \end{pmatrix} = 0 \Rightarrow \text{eigenvec.} = \begin{pmatrix} -1 \\ 1+\sqrt{2} \end{pmatrix} \text{ for } \lambda = -\sqrt{2}$$

What is the general form of the solution to the differential equation $\frac{d^2 x}{dt^2} = -\omega^2 x$?

$$(21) \quad x(t) = A \cos(\omega t) + B \sin(\omega t)$$

What is the general form of the solution to the differential equation $\frac{d^2 x}{dt^2} = \omega^2 x$?

$$(18) \quad x(t) = A e^{\omega t} + B e^{-\omega t}$$