

# Announcements

- Homework 10 is due next Wednesday, April 19.
- Homework 11 is due next **Monday, April 24**.

# Last time

- Crystal structures
- Heat capacity

# Today's class

- Band theory of solids

# in-class quiz (5 min)

For a specific metal, plotting  $C/T$  against  $T^2$  yields a straight line with a slope of  $1.66 \times 10^{-4} \text{ J/mole}\cdot\text{K}^4$ . What is this metal?

- A. K
- B. Na
- C. Au
- D. Ag
- E. Cu

Metal	Debye Temperature
K	91 K
Na	157 K
Au	162 K
Ag	227 K
Cu	347 K

# in-class quiz (5 min)

$$C = \frac{12\pi^4}{5} R \left(\frac{T}{T_D}\right)^3 \Rightarrow \frac{C}{T} = \underbrace{\frac{12\pi^4}{5} R \frac{1}{T_D^3}}_{\text{slope}} T^2$$

$$R = 8.31 \text{ J} \cdot \text{mol}^{-1} \cdot \text{K}^{-1}$$

$$T_D = 227 \text{ K}$$

For a specific metal, plotting  $C/T$  against  $T^2$  yields a straight line with a slope of  $1.66 \times 10^{-4} \text{ J/mole} \cdot \text{K}^4$ . What is this metal?

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# Fermi function $f(E)$

- Read textbook section 10.5
- Definition: fraction of occupied states as a function of energy.

$$f(E) = \frac{1}{e^{(E - E_F)/kT} + 1}$$

$E$  is the variable.

$f(E)$  is  $T$  dependent.

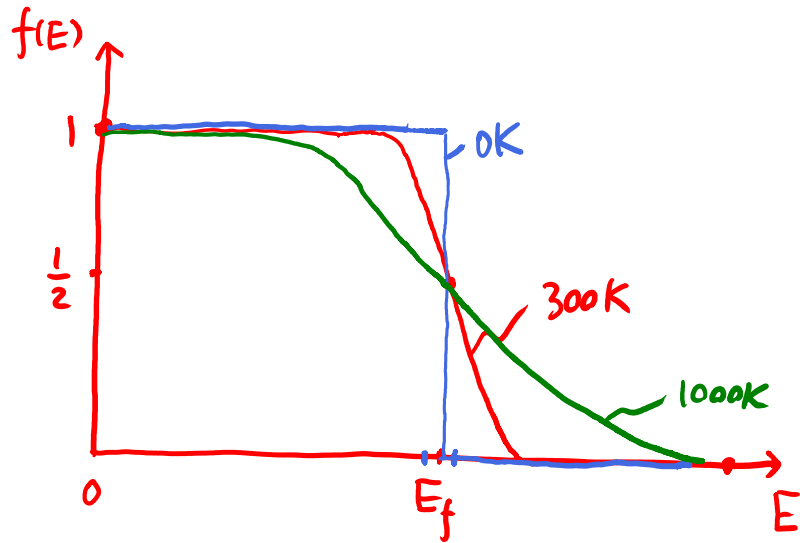
$E_F$  is Fermi energy, a constant for a given material.

$E_F$  has a negligible change with temperature.

Element	Fermi Energy eV
Li	4.74
Na	3.24
K	2.12
Rb	1.85
Cs	1.59
Cu	7.00
Ag	5.49
Au	5.53
Be	14.3
Mg	7.08
Ca	4.69

# Fermi function: shape, temperature dependence

$$f(E) = \frac{1}{e^{(E-E_f)/kT} + 1}$$



$$T = 300\text{K} \Rightarrow kT = 0.025\text{eV}, \quad E_f = 1\text{eV}$$

$$E = 0, \quad f(E) = \frac{1}{e^{-E_f/kT} + 1} = \frac{1}{e^{-40} + 1} = 1$$

$$E = E_f, \quad f(E) = \frac{1}{e^0 + 1} = \frac{1}{2}$$

$$E \gg E_f, \quad f(E) = \frac{1}{e^{E/kT} + 1} \approx 0$$

$$T = 0\text{K}, \text{ say } T = 10^{-15}\text{K}, \quad kT \text{ is extremely small}$$

$$E = 0, \quad f(E) = \frac{1}{e^{-E_f/kT} + 1} = \frac{1}{e^{-\infty} + 1} = 1$$

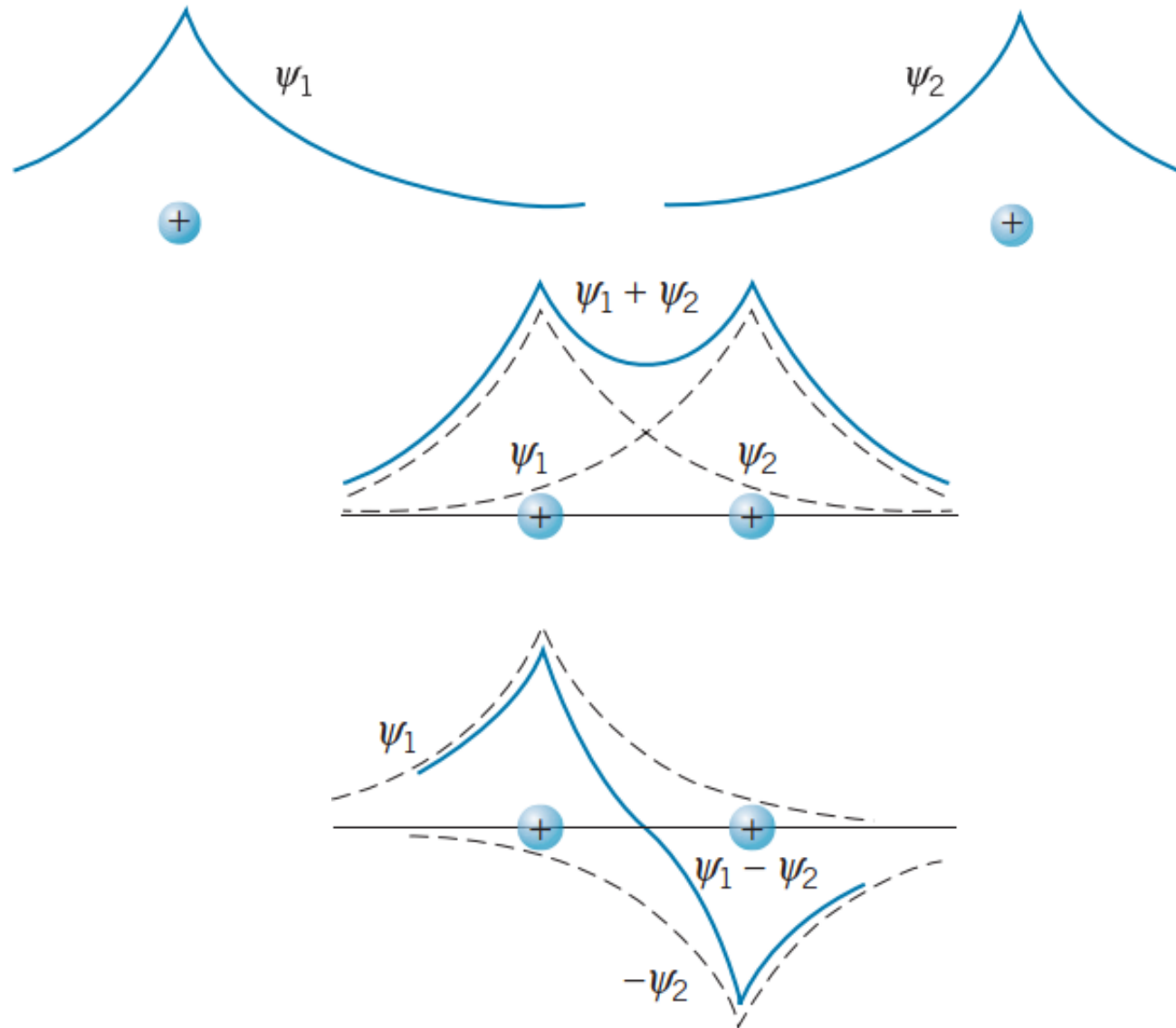
$$E = E_f, \quad f(E) = \frac{1}{e^0 + 1} = \frac{1}{2}$$

$$E \gg E_f, \quad f(E) = \frac{1}{e^{E/kT} + 1} = \frac{1}{e^{\infty} + 1} = 0$$

$$E - E_f = 0.01\text{eV}, \quad f(E) = \frac{1}{e^{0.01/kT} + 1} = \frac{1}{e^{\infty} + 1} = 0$$

$$E - E_f = -0.01\text{eV}, \quad f(E) = \frac{1}{e^{-0.01/kT} + 1} = \frac{1}{e^{-\infty} + 1} = 1$$

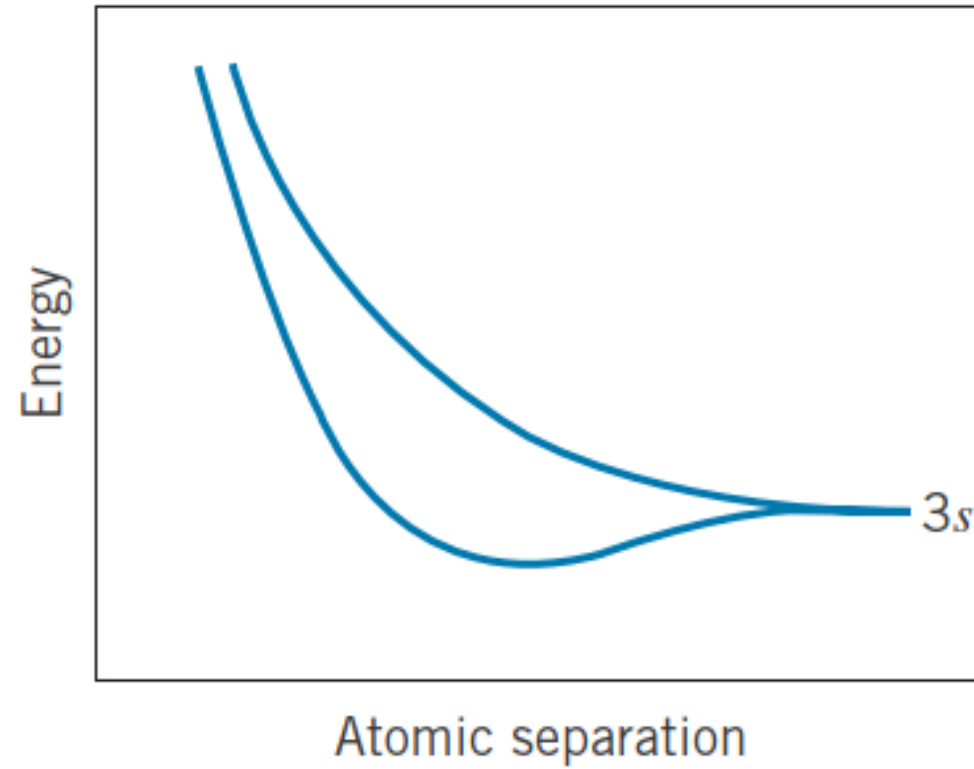
Wave functions begin to overlap as two identical atoms approach each other.



Split of energy levels

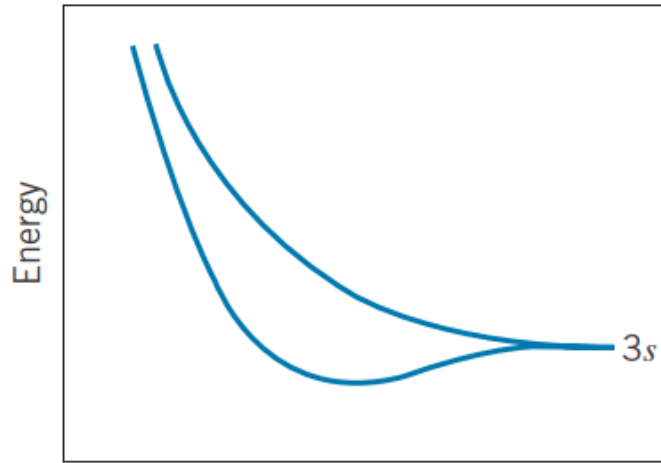


Energy level split when two identical atoms approach each other.



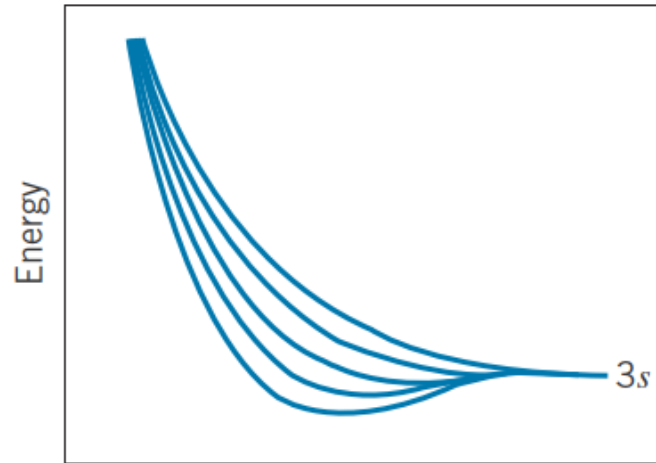
Energy band forms when many identical atoms approach each other.

1s band  $2N$   
 2s band  $2N$   
 2p band  $6N$   
 3p band  $6N$   
 nl band  $\frac{2(2l+1)N}{m_s m_l}$



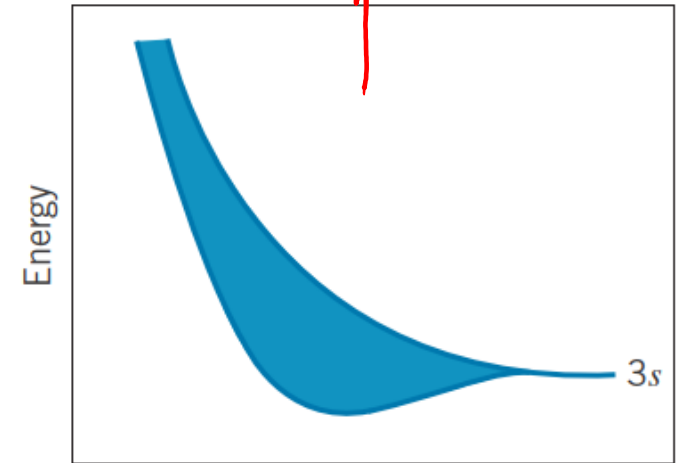
Atomic separation

2 atoms  
 2 levels



Atomic separation

5 atoms  
 5 levels



Atomic separation

N atoms  
 N levels  $\rightarrow$  band

each level  
# of electrons

2

2

2

total electrons

4

10

$2N$

total capacity

# Energy bands in Na metal

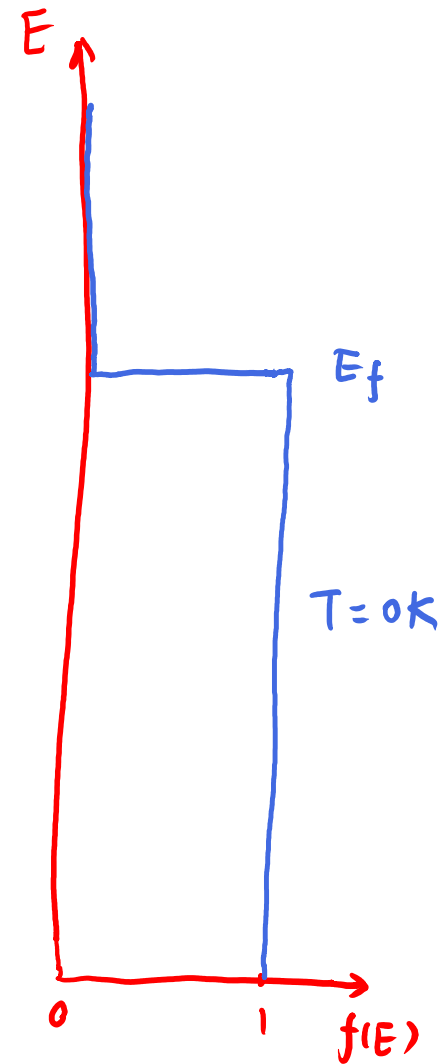
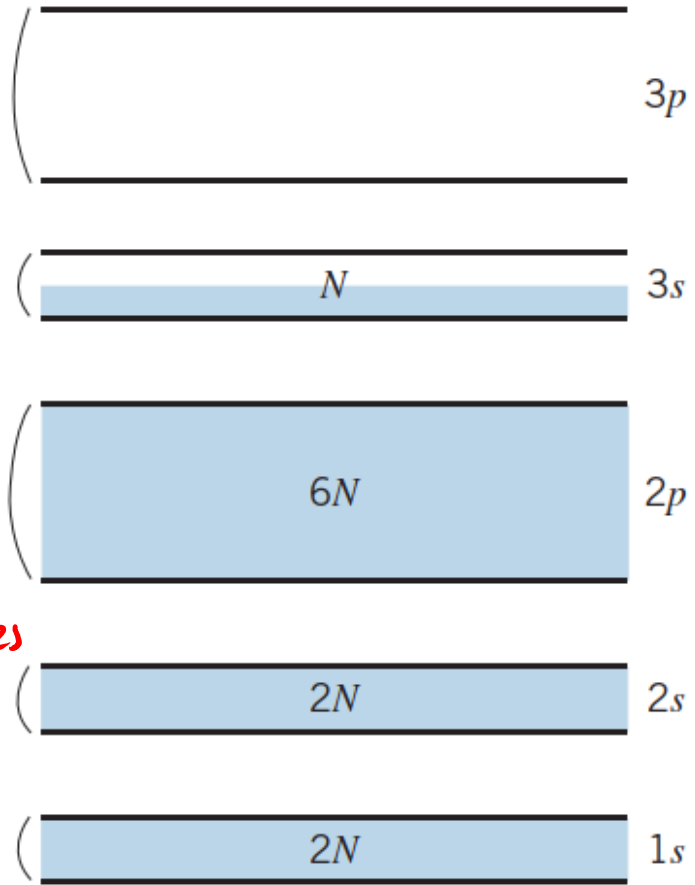
electron configuration  
atomic theory

$1s^2 2s^2 2p^6 3s^1$        $11e^-$

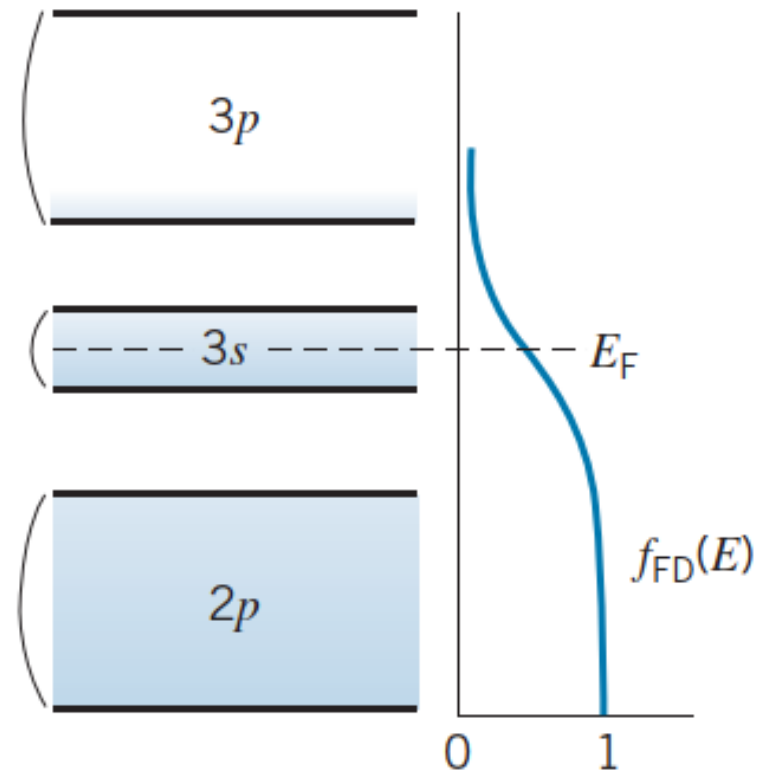
$N$  atoms       $11Ne^-$

Na is a good conductor.

$N$  relatively free  $3s$   $e^-$ s  
can move to  $N$  unoccupied  $3s$  states



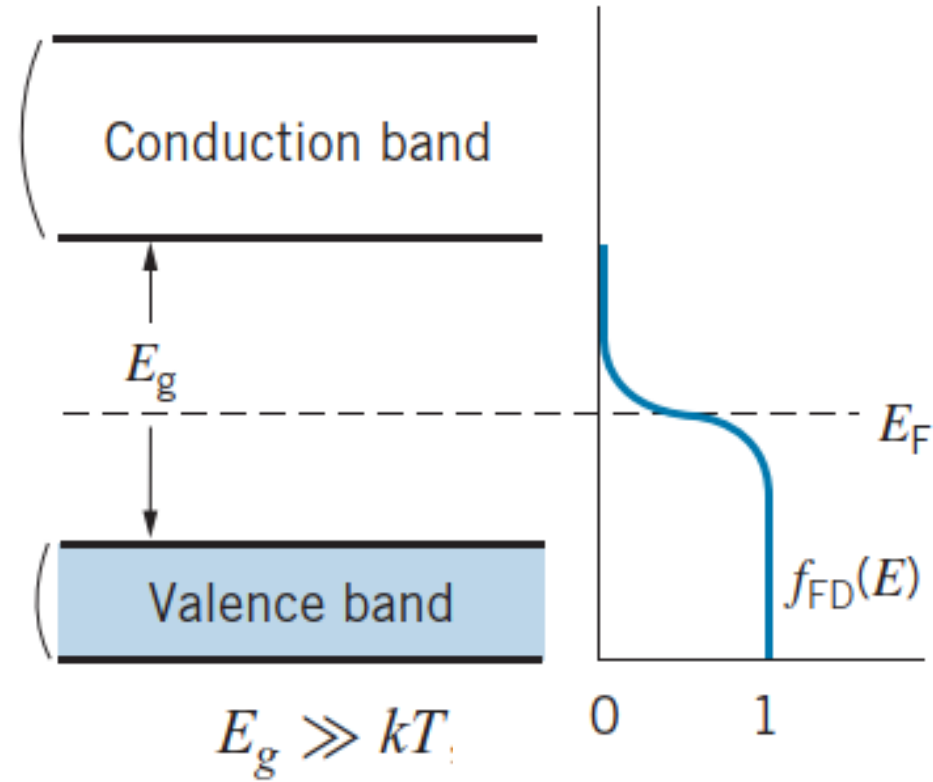
# Fermi function spreads with thermal excitation



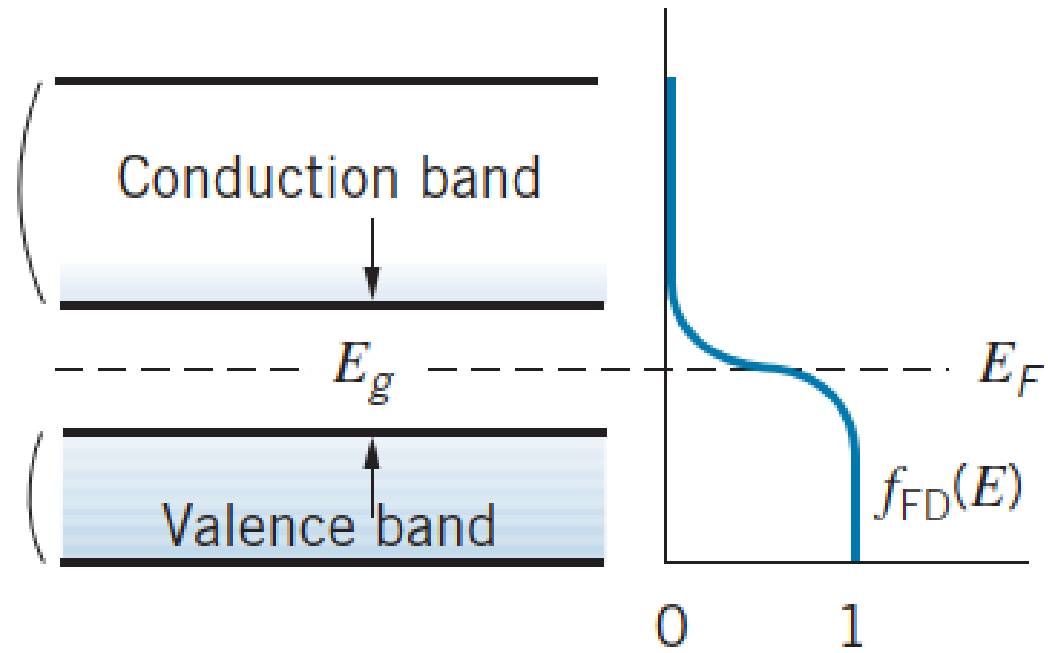
$T > 0$

3p has some electrons. 2p is not completely full.

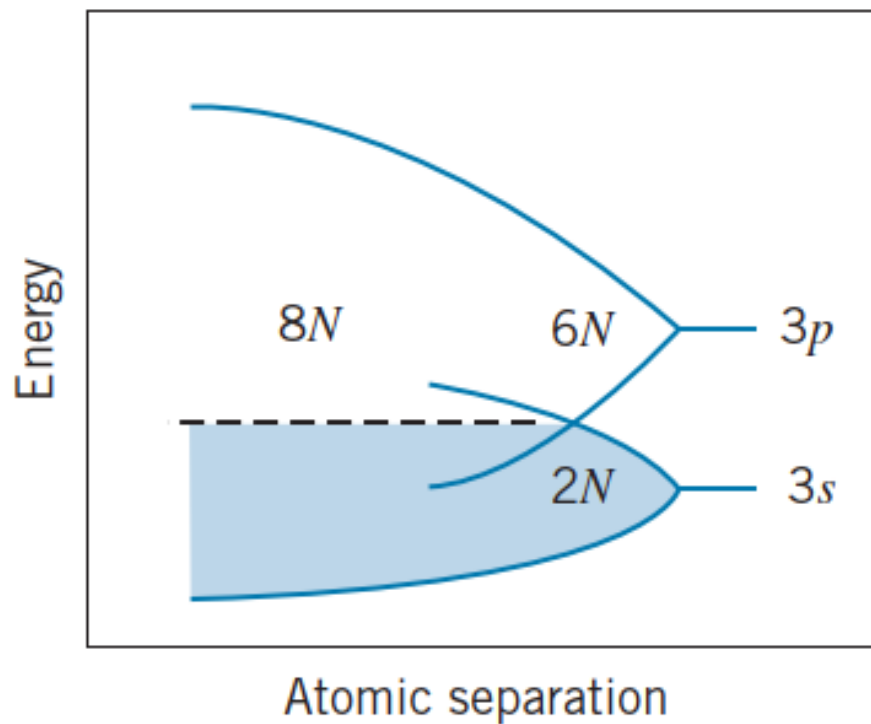
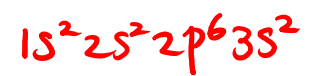
# Insulator



# Semiconductor



# Band structure in Mg metal



# Band structure in C, Si, Ge

