

Announcements

- Homework 10 is due next Wednesday, April 19.
- Homework 11 is due next **Monday, April 24**.

Last time

- Band theory of solids

Today's class

- Semiconductors

in-class quiz (5 min)

For a semiconductor, let's say the bandgap E_g is 1 eV. Let's assume Fermi energy is near the middle of the gap. At room temperature, what is the fraction of electrons near the bottom of the conduction band?

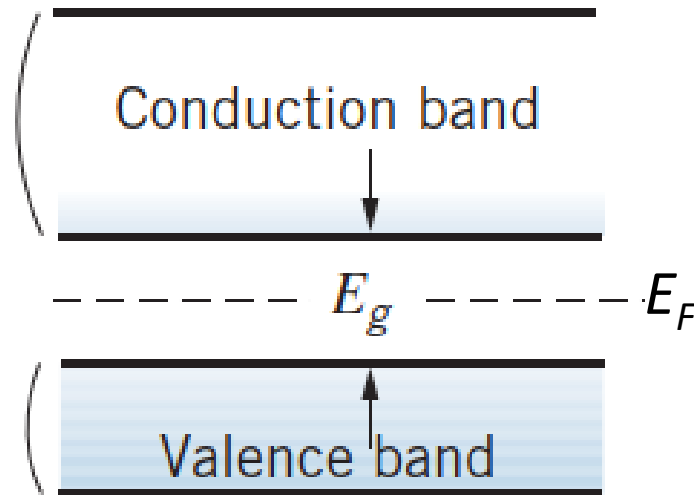
A. 0

B. 10^{-20}

C. 10^{-9}

D. 0.5

E. 1



in-class quiz (5 min)

$$E - E_f = \frac{1}{2} E_g = 0.5 \text{ eV}$$

$$kT = 0.025 \text{ eV}$$

$$f(E) = \frac{1}{e^{(E-E_f)/kT} + 1} = \frac{1}{e^{20} + 1} = e^{-20} = 10^{-9}$$

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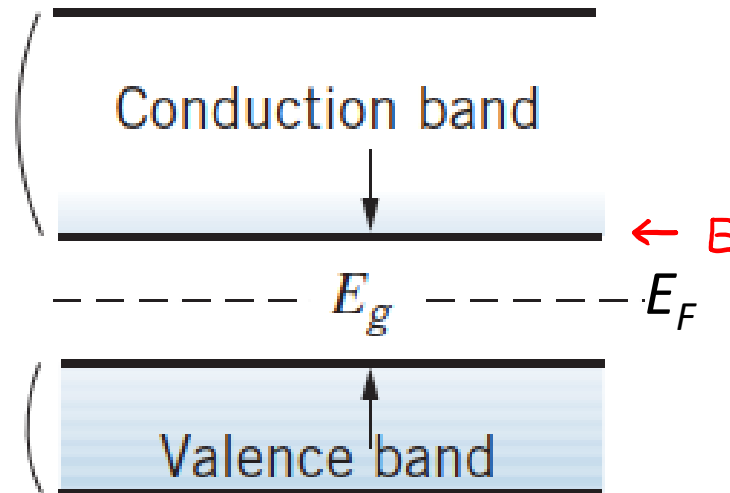
A. 0

B. 10^{-20}

C. 10^{-9}

D. 0.5

E. 1



Electrons and holes

Conduction band:

charge carrier: electrons

move easily – lots of empty states to move into

Valence band:

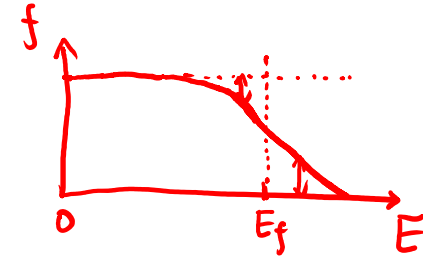
charge carrier: electrons

harder to move – most states are occupied

apparent motion of “vacancies” or “holes” in the opposite direction

effectively charge carrier: positively-charged holes

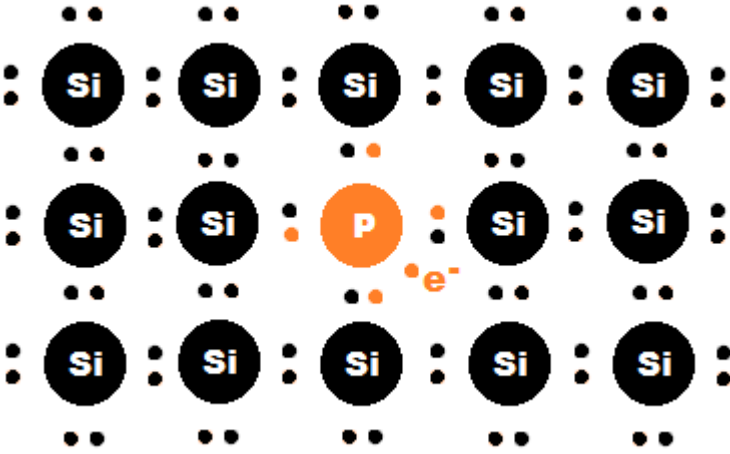
Intrinsic semiconductors



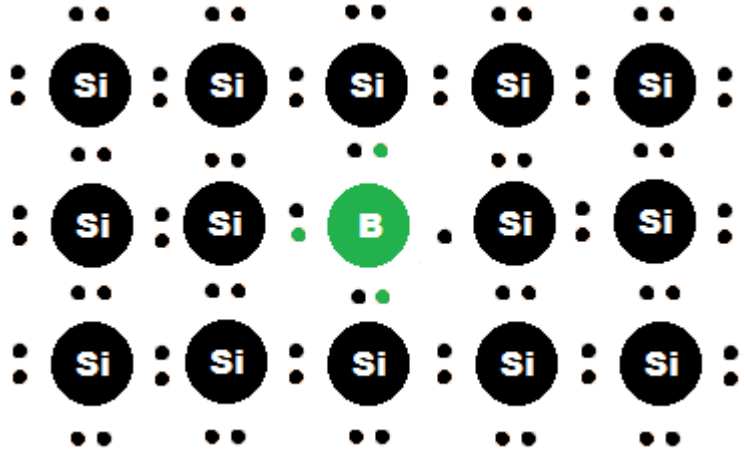
- # of electrons in the conduction band vs. # of holes in the valence band? *equal*
- Where is Fermi energy with respect to the band gap? *middle*
- Which one contributes more to conduction – electrons or holes? *electrons*
- Fraction of electrons (or holes) contributes to conduction? *10^{-9}*

Impurity semiconductors

Doping at 1 in 10^6 or 10^7 can dominate conduction \gg intrinsic 10^9

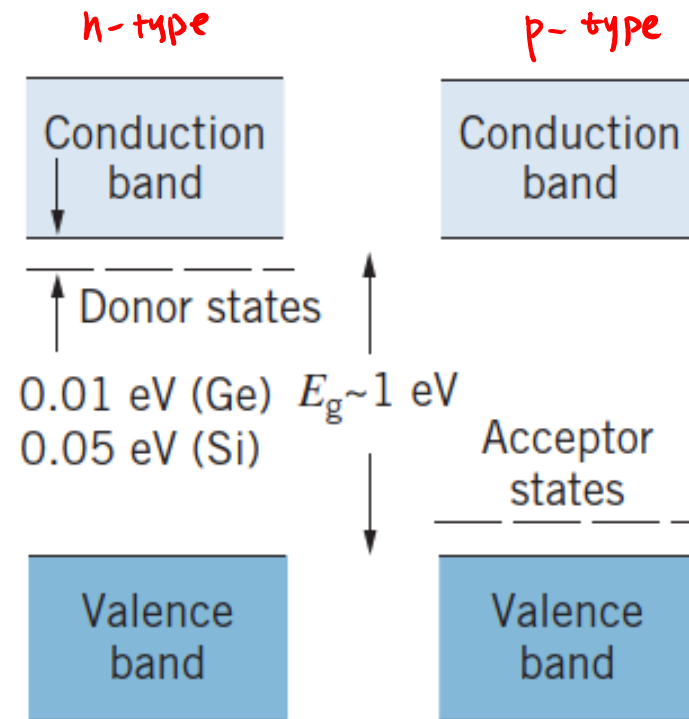


n-type
Doping with Group V elements
Donor impurities



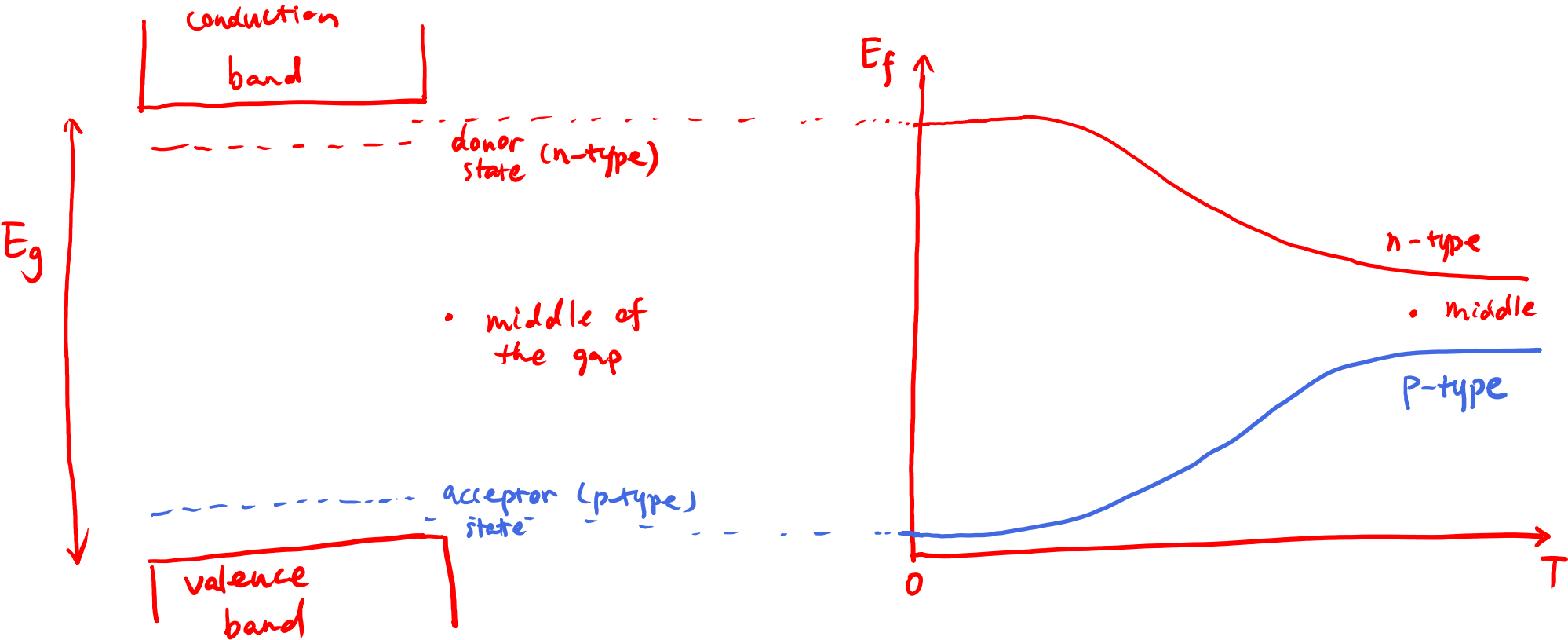
p-type
Doping with Group III elements
Acceptor impurities

Energy levels in semiconductors



Doping introduces a new energy level within the bandgap.
Electron donor impurities create states near the conduction band.
Electron acceptor impurities create states near the valence band.

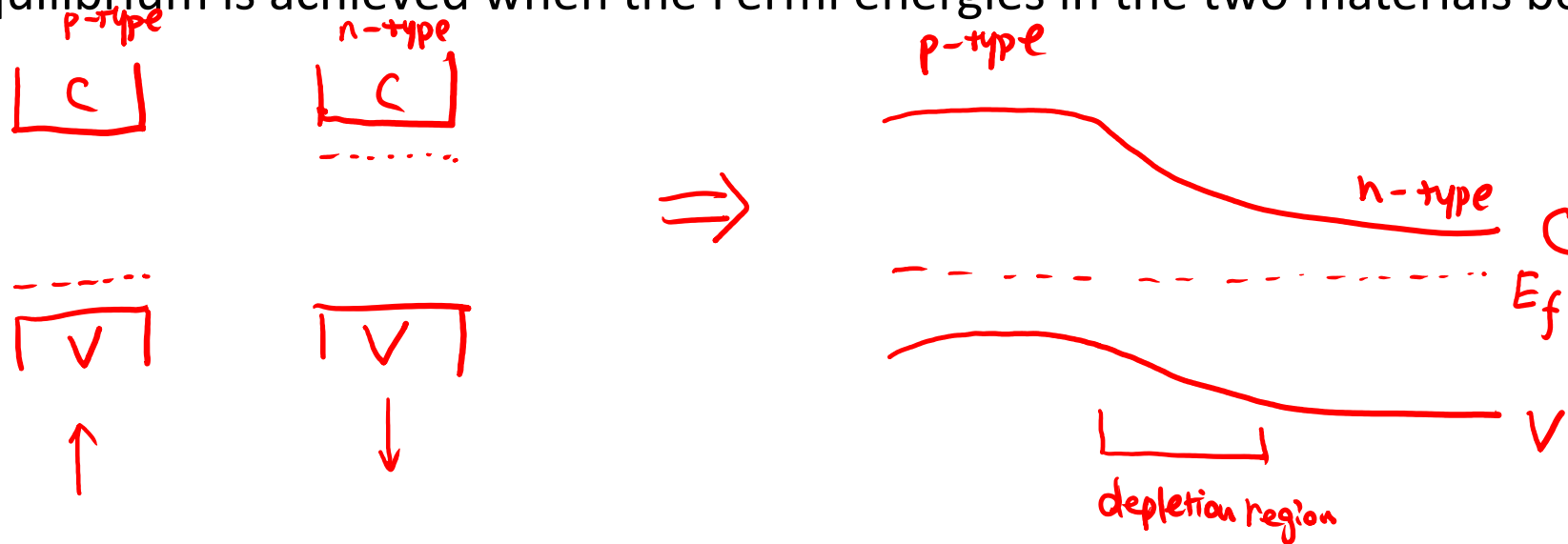
Fermi energy in semiconductors

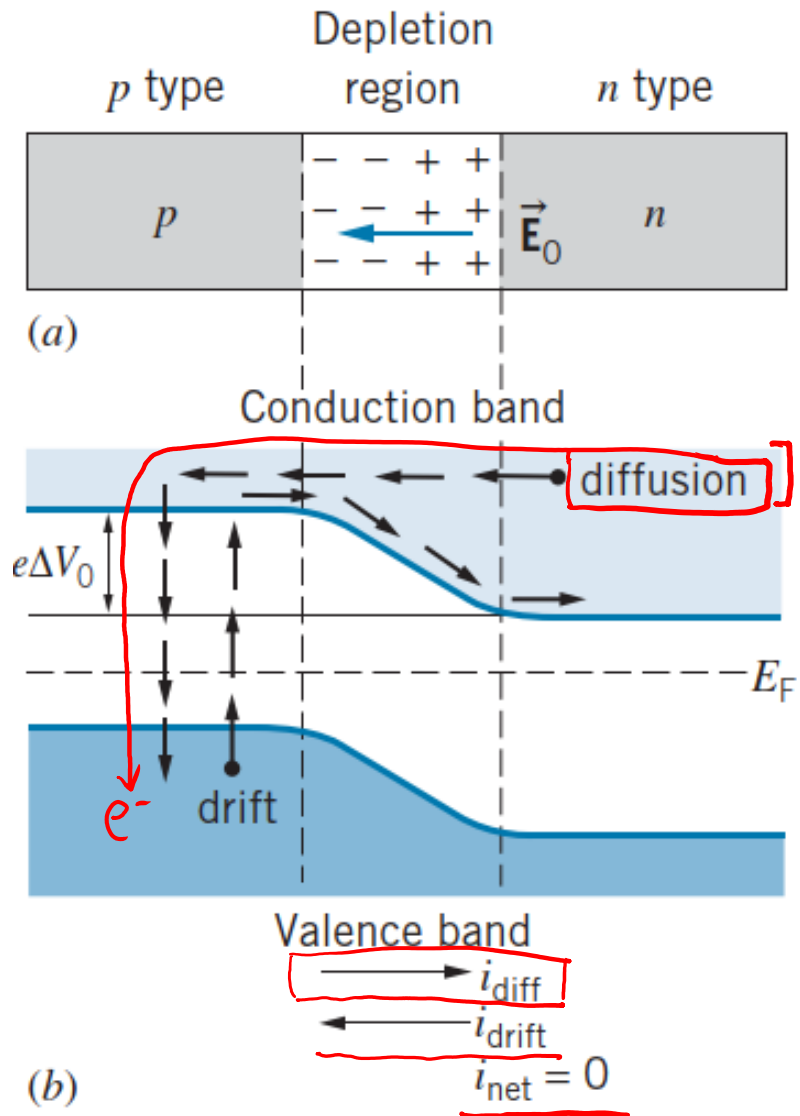


The p-n junction

Electrons flow from the n-type into the p-type material

Equilibrium is achieved when the Fermi energies in the two materials become identical





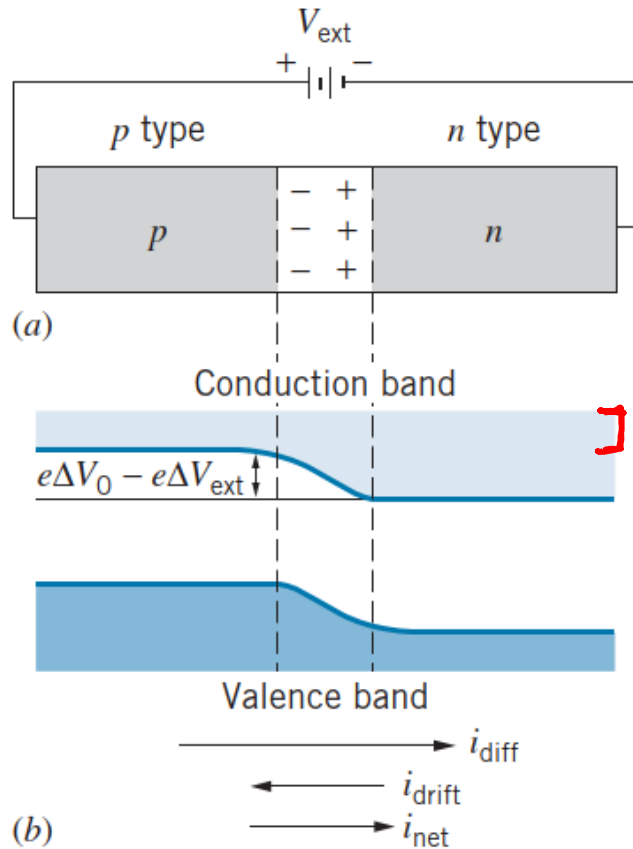
e^- s enter into p-type, building up \ominus charge
 $\Rightarrow E_0$, a net electric field in the depletion region.
 preventing further flow of e^- s.
 for e^- to go from n to p, it has to overcome
 the energy barrier imposed by \vec{E}_0 , eV_0

Diffusion current: highest-energy e^- s can
 go from n to p.

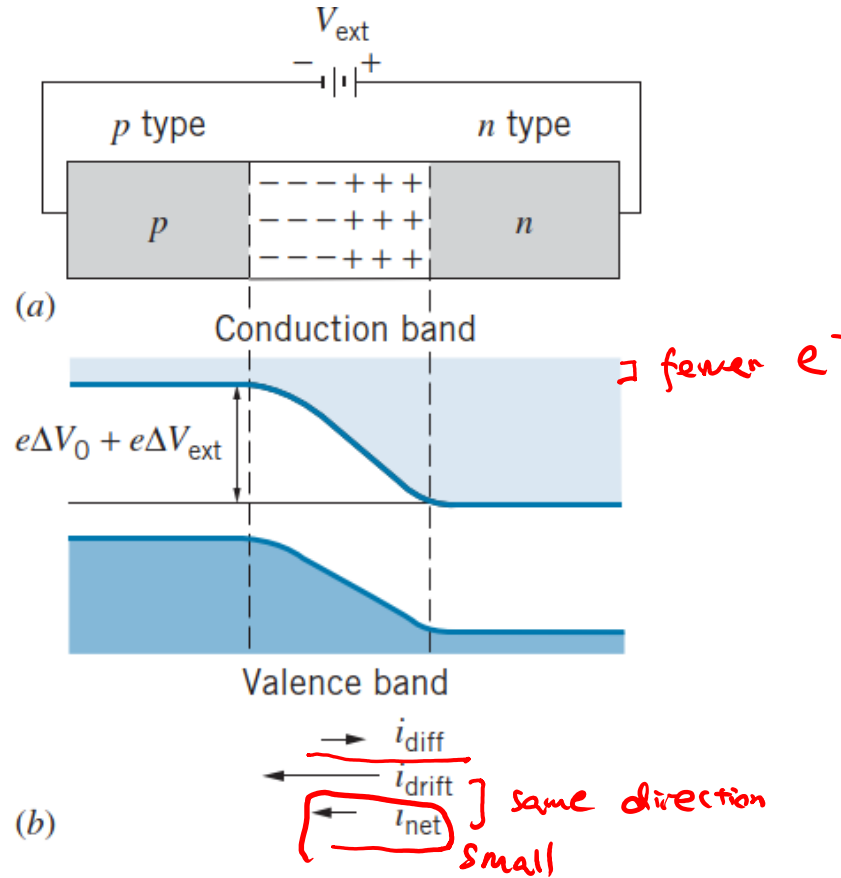
Drift (thermal) current: e^- s jumps from
 valence band in p to conduction band

Applying bias on the p-n junction

Forward bias



Reverse bias



- forward bias:
- ① pull e^- from p. put into n
 - ② depletion region narrower. $\Delta E \downarrow$
 - ③ more e^- can contribute to diffusion current, $i_{diff} \uparrow$
 - ④ i_{drift} unchanged

At equilibrium, diffusion current is proportional to the number of electrons above the energy E_c

E_c is the energy level at the bottom of conduction band in the p-type region

$$f(E) = \frac{1}{e^{(E-E_f)/kT} + 1} \quad \text{fraction of occupied states}$$

At equilibrium, $i_{\text{drift}} = i_{\text{diffusion}}$. Both diffusion and drift current are proportional to N_1 .

$$N_1 = n e^{-(E_c - E_f)/kT} \quad n \text{ is a proportionality factor} \quad \downarrow \text{ \# of electrons}$$

With bias, the number of electrons above the energy $E_c - e\Delta V_{\text{ext}}$

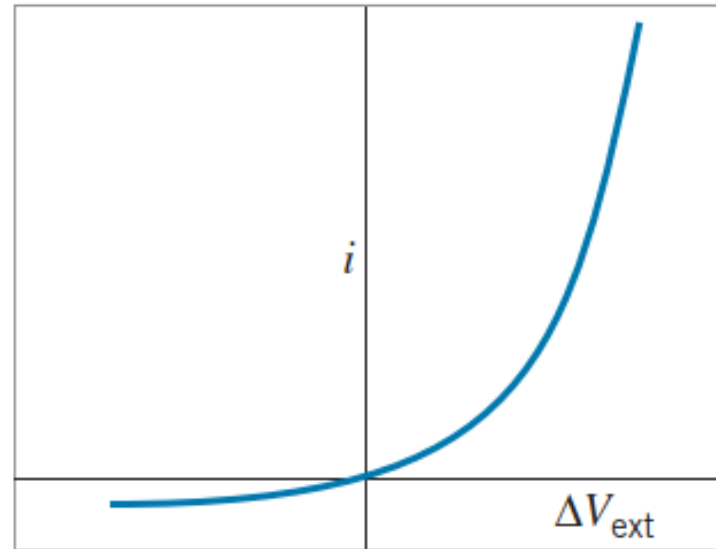
$$N_2 = n e^{-(E_c - e\Delta V_{\text{ext}} - E_f)/kT}$$

$$i_{\text{diffusion}} \propto N_2, \quad i_{\text{drift}} \propto N_1$$

$$i_{\text{net}} \propto N_2 - N_1 = n e^{-(E_c - e\Delta V_{\text{ext}} - E_f)/kT} - n e^{-(E_c - E_f)/kT} = \underline{n e^{-(E_c - E_f)/kT}} (e^{e\Delta V_{\text{ext}}/kT} - 1)$$
$$= i_0 (e^{e\Delta V_{\text{ext}}/kT} - 1)$$

Diode

$$i = i_0(e^{e\Delta V_{\text{ext}}/kT} - 1)$$



Diode

